



1 **Uncertainty Quantification for Atmospheric Motion Vectors with** 2 **Machine Learning**

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5 **Abstract.** Wind-tracking algorithms produce Atmospheric Motion Vectors (AMVs) by tracking clouds or water vapor
6 across spatial-temporal fields. Thorough error characterization (also known as uncertainty quantification) of wind-
7 tracking algorithms is critical in properly assimilating AMVs into weather forecast models and climate reanalysis
8 datasets. Uncertainty quantification should yield estimates of two key quantities of interest: bias, the systematic
9 difference between a measurement and the true value, and standard error, a measure of variability of the measurement.
10 The current process of specification of the errors input into inverse modelling is often cursory and commonly consists
11 of a mixture of model fidelity, expert knowledge, and need for expediency. The methods presented in this paper
12 supplement existing approaches to error specification by providing an error-characterization module that is purely
13 data-driven and requires few tuning parameters. This paper proposes an error-characterization method that combines
14 the flexibility of machine learning (random forest) with the robust error estimates of unsupervised parametric
15 clustering (using a Gaussian Mixture Model). Traditional techniques for uncertainty quantification through machine
16 learning have focused on characterizing bias, but often struggle when estimating standard error. In contrast, model-
17 based approaches such as k-means or Gaussian mixture modelling can provide reasonable estimates of both bias and
18 standard error, but they are often limited in complexity due to reliance on linear or Gaussian assumptions. In this
19 paper, a methodology is developed and applied to characterize error in tracked-wind using a high-resolution global
20 model simulation, and it is shown to adequately capture the error features of the tracked wind.

21 **1. Introduction**

22 Reliable estimates of global winds are critical to science and application areas, including global chemical transport
23 modeling and numerical weather prediction. One source of wind measurements consists of feature-tracking based
24 Atmospheric Motion Vectors (AMVs), produced by tracking time sequences of satellite-based measurements of
25 clouds or spatially distributed water vapor fields (Mueller et al., 2017; Posselt et al., 2019). The importance of global
26 measurements of 3-dimensional winds was highlighted as an urgent need in the NASA Weather Research Community
27 Workshop Report (Zeng et al., 2016) and was identified as a priority in the 2007 National Academy of Sciences Earth
28 Science and Applications from Space (ESAS 2007) Decadal Survey and again in ESAS 2017. For instance, wind is
29 used in the study of global CO₂ transport (Kawa et al., 2004), numerical weather prediction (NWP; Cassola and
30 Burlando, 2012), as inputs into weather and climate reanalysis studies (Swail and Cox, 2000), and for estimating
31 current and future wind-power outputs (Staffell and Pfenninger, 2016).

32 Thorough error characterization of wind-track algorithms is critical in properly assimilating AMVs into forecast
33 models. Prior literature has explored the impact of ‘poor’ error-characterization in Bayesian-based approaches to



34 remote sensing applications. Nguyen et al. (2019) proved analytically that when the input bias is incorrect in Bayesian
35 methods (specifically, optimal estimation retrievals), then the posterior estimates would also be biased. Moreover,
36 they proved that when the input standard error is ‘correct’ (that is, it is as close to the unknown truth as possible), then
37 the resulting Bayesian estimate is ‘efficient’; it has the smallest possible error. Additionally, multiple active and
38 passive technologies are being developed to measure 3D winds, such as Doppler wind lidar (DWL) and radar and
39 infrared/microwave sensors that derive AMVs using feature-tracking of consecutive images. Therefore, an accurate
40 and robust uncertainty quantification methodology will allow for more accurate assessments of mission impacts, and
41 the eventual propagation of data uncertainties for these instruments.

42 Velden and Bedka (2009) and Salonen et al. (2015) have shown that height assignment contributes a large component
43 of uncertainty in AMVs tracked from cloud movement and from sequences of infrared satellite radiance images.
44 However, height assignment is not the dominant portion of the error in AMVs obtained from water vapor profiling
45 instruments (e.g., infrared and microwave sounders). As such, this study will focus on errors in the AMV estimates at
46 a given height. Previous work has demonstrated several different approaches for characterizing AMV vector error.
47 One common approach is to employ quality indicator thresholds, as described by Holmund et al (2001), which
48 compare changes in AMV estimates between sequential timesteps and neighboring pixels, as well differences with
49 model predictions, to produce a quality indicator to which a discrete uncertainty is assigned. The Expected Error
50 approach, developed by Le Marshal et al. (2004), builds a statistical model using linear regression against AMV-
51 radiosonde values to correct AMV observation error.

52 In this study, we detail a data-driven tool for building an AMV uncertainty model using observing system simulation
53 experiment (OSSE) data. We build on the work by Posselt et al. (2019) in which a water vapor feature-tracking AMV
54 algorithm was applied to a high-resolution numerical simulation, thus providing a global set of AMV estimates which
55 can be compared to the reference winds produced by the simulation. In this case, a synthetic “true” state is available
56 with which AMVs can be compared and errors are quantified, and it is shown that tracking errors in AMV estimates
57 are state dependent. Our approach will use a conjunction of machine learning (random forest) and unsupervised
58 parametric clustering (Gaussian mixture models) to build a model for the uncertainty structures found by Posselt et al.
59 (2019). The realism and robustness of the resulting uncertainty estimates depend on the realism and representativeness
60 of the reference dataset. This work builds upon the work of Bormann et al. (2014) and Hernandez-Carrascal and
61 Bormann (2014), who showed that wind tracking could be divided into distinct geophysical regimes by clustering by
62 cloud conditions. This study supplements that approach with the addition of machine learning, which, compared with
63 traditional linear modeling approaches, should allow the model to capture more complex non-linear processes in the
64 error function.

65 Traditional techniques for uncertainty quantification through machine learning have focused on characterizing bias
66 but often struggle when estimating standard error. By pairing a random forest algorithm with unsupervised parametric
67 clustering, we propose a data-driven, cluster-based approach for quantifying both bias and standard error from
68 experimental data. According to the theory developed by Nguyen et al. (2019), these improved error characterizations



69 should then lead to improved error characteristics (e.g., lower bias, more accurate uncertainties) in subsequent analyses
70 such as flux inversion or data assimilation.

71 The rest of the paper is organized as follows: In Section 2, we give an overview of the simulation which provides the
72 training data for our machine learning approach and motivate and define the specific uncertainties this study aims to
73 characterize. In Section 3, we describe the error characterization approach with the specifics of our error
74 characterization model, including both the implementation of and motivations for employing the random forest and
75 Gaussian mixture model. In Section 4, we provide a validation of our methods, attempting to assess the bias of our
76 predictions. In Section 5, we discuss the implications of our error characterization approach, both on AMV estimation
77 and data assimilation more broadly.

78 **2. Experimental Set-up**

79 **2.1 Simulation and Feature-Tracking Algorithm**

80 While our methodology in principle could be used to quantify uncertainties in any measurements used in data
81 assimilation, in this paper we devote special emphasis to the use case of wind-tracking algorithms. In particular, we
82 trained our model on the simulated data used by Posselt et al. (2019), in which they applied an AMV algorithm to
83 outputs from the NASA Goddard Space Flight Center (GSFC) Global Modeling and Assimilation Office (GMAO)
84 GEOS-5 Nature Run (G5NR; Putman et al. 2014). The Nature Run is a global dataset with ~ 7 km horizontal grid
85 spacing that includes, among other quantities, three-dimensional fields of wind, water vapor concentration, clouds,
86 and temperature. The AMV algorithm is applied on four pressure levels (300hPa, 500hPa, 700hPa, and 850hPa) at 6-
87 hourly intervals, using three consecutive global water vapor fields spaced one hour apart, and for a 60-day period from
88 07/01/2006 to 08/30/2006. The water-vapor fields from GEOS5 were input to a local-area pattern matching algorithm
89 that approximates wind speed and direction from movement of the matched patterns. The algorithm searches a pre-
90 set number of nearby pixels to minimize the sum-of-absolute-differences between aggregated water vapor values
91 across the pixels. Posselt et al. (2019) describes the sensitivity of the tracking algorithm and the dependency of the
92 tracked winds on atmospheric states in detail.

93 It is important to note that the AMV algorithm tracks water vapor on fixed pressure levels. In practice, these would be
94 provided by satellite measurements, whereas in this paper we use simulated water vapor from the GEOS-5 Nature
95 Run. The height assignment of the AMVs is assumed to be perfectly known (or, at the very least, the pressure level
96 uncertainty is captured by the satellite measurement uncertainty rather than the AMV estimate). As such, we focus
97 solely on observational AMV error and not on height assignment error.

98 A snapshot of the dataset at 700hPa is given in Figure 1, where we display the true water vapor from Nature Run (top
99 left panel), the true wind speed from Nature Run (top right panel), the tracked wind from the AMV-tracking algorithm
100 (bottom right panel), and the difference between the true and tracked wind (bottom left panel). Note that the wind-
101 tracking algorithm tends to have trouble in region where the true water vapor content is close to zero. It is clear that



102 while the wind-tracking algorithm tends to perform well in most regions (we can classify these regions as areas where
103 the algorithm is skilled), in some regions the algorithm is unable to reliably make a reasonable estimate of the wind
104 speed (unskilled). We will examine these skilled and unskilled regimes (and their corresponding contributing factors)
105 in the section 3.

106 2.2 Importance of Uncertainty Representation in Data Assimilation

107 Proper error characterization for any measurement, including AMVs, is important in data assimilation. Data
108 assimilation often uses a regularized matrix inverse method based on Bayes' theorem, which, when all probability
109 distributions in Bayes' relationship are assumed to be Gaussian, reduces to minimizing a least-squares (quadratic) cost
110 function Eq (1):

$$111 \quad \mathbf{J} = (\mathbf{x} - \mathbf{x}_b)\mathbf{B}^{-1}(\mathbf{x} - \mathbf{x}_b) + ((\hat{\mathbf{y}} - \mathbf{a}) - \mathbf{H}[\mathbf{x}])^T \mathbf{R}^{-1}((\hat{\mathbf{y}} - \mathbf{a}) - \mathbf{H}[\mathbf{x}]) \quad (1)$$

112 where \mathbf{x} represents the analysis value, \mathbf{x}_b represents the background field (first guess), \mathbf{B} represents the background
113 error covariance, \mathbf{y} represents the observation, and \mathbf{H} represents the forward operator that translates model space into
114 observation space. This translation may consist of spatial and/or temporal interpolation if \mathbf{x} and \mathbf{y} are the same variable
115 (e.g., if the observation of temperature comes from a radiosonde), or may be far more complicated (e.g., a radiative
116 transfer model in the case of satellite observations). \mathbf{R} represents the observation error covariance, and \mathbf{a} represents
117 the accuracy, or bias, in the observations. The right-most part of Eq. (1) can be interpreted as a sum of the contribution
118 of information from the data ($\mathbf{y} - \mathbf{H}[\mathbf{x}] - \mathbf{a}$) and the contribution from the prior ($\mathbf{x} - \mathbf{x}_b$), which are weighted by their
119 respective covariance matrices. In our analysis, the AMVs obtained from the wind-tracking algorithm is used as 'data'
120 in subsequent analysis. That is, the tracked wind data $\hat{\mathbf{y}}$ is a biased and noisy estimator of the true wind \mathbf{y} , and might
121 be assumed to follow the model Eq. (2):

$$122 \quad \hat{\mathbf{y}} = \mathbf{y} + \epsilon \quad (2)$$

123 where ϵ is an error term, commonly assumed to be Gaussian with mean \mathbf{a} and covariance matrix \mathbf{R} (i.e., $\epsilon \sim \mathcal{N}(\mathbf{a}, \mathbf{R})$),
124 which are the same two terms that appear in Equation (1). As such, for data assimilation to function, it is essential to
125 correctly specify the bias vector \mathbf{a} and the standard error matrix \mathbf{R}^{-1} . Incorrect characterizations of either of these
126 components could have adverse consequences on the resulting data assimilation analyses with respect to bias and/or
127 the standard error (Nguyen et al., 2019).

128 3 Methodology

129 3.1 Generalized Error Characterization Model

130 An overview of our approach is outlined in Figure 2. Given a set of training predictors \mathbf{X} , training responses $\hat{\mathbf{Y}}$, and
131 the true response \mathbf{Y} , our approach begins with two independent steps. In one step, a Gaussian mixture model is trained



132 on the set of X , \hat{Y} , and Y . This clustering algorithm identifies geophysical regimes where the nonlinear relationships
133 between the three variables differ. In the other step, a random forest is used to model Y based on X and \hat{Y} . This step
134 produces an estimate of the true response (we call this \tilde{Y}) using only the training predictors and response. We then
135 employ the Gaussian mixture model to estimate the clusters which the set of X , \hat{Y} , and \tilde{Y} pertain to. Subsequently, we
136 compute the error characteristics of each cluster of X , \hat{Y} , and \tilde{Y} in the training dataset. Therefore, given a new point
137 consisting solely of X and \hat{Y} , we can assign it to a specific cluster and ascribe to it a set of error characteristics. This
138 forms the basis for our error characterization model.

139 What follows in this paper is an implementation of the error characterization model obtained for a subsample of the
140 GEOS-5 Nature Run at a fixed height of 700hPa. In particular, we trained the error characterization on a random
141 sample from the first 1.5 months of the Nature Run, and show the results obtained when applying it to a test sample
142 drawn from the subsequent 0.5 months of the Nature Run.

143 3.2 Error Regime

144 When examining the relationship between AMVs and simulated true winds in Figure 3, it is clear that there are two
145 distinct ‘error-regimes’ present in the dataset. The majority of AMV estimates can be categorized as ‘skilled’, wherein
146 their estimate lies clearly along a one-to-one line with the simulated true wind. However, there is also clearly an
147 ‘unskilled’ regime, for which the AMV estimate is very close to zero when there are actually high or mid-level true
148 wind values present. Our goal is to provide unique error characterizations for each error regime, because the error
149 dynamics are different within each regime. Furthermore, when we analyze this error and its relationship to water
150 vapor, we see that ‘unskilled’ regime correlates highly with areas of low water vapor in Figure 4. This matches the
151 error patterns discussed in Posselt et al. (2019).

152 3.3 Gaussian Mixture Model

153 These distinct regimes present an opportunity to employ machine learning. Bormann et al. (2014) and Hernandez-
154 Carrascal and Bormann (2014) demonstrated that cluster (also called regime) analysis is a successful approach for
155 wind-tracking error characterization, and so we aim to train a clustering algorithm that is capable of determining
156 whether any individual AMV estimate belongs in the ‘skilled’ or ‘un-skilled’ cluster. In particular, we use a clustering
157 algorithm that can take advantage of the underlying geophysical dynamics, since we see the relationship between the
158 error-regimes and water vapor content. To this end, we employ a Gaussian mixture model, a clustering algorithm
159 based on estimating a training set as a mixture of multiple Gaussian distributions. A mathematical overview follows:

- 160 1. Define each location containing simulated true winds, water vapor, and AMV estimates as a random
161 variable x_i
- 162 2. Define θ as the population that consists of all x_i in the training dataset
- 163 3. Model the distribution of the population $P(\theta)$ as:



164
$$P(\theta) = \sum_j^K \pi_j N(\mu_j, \Sigma_j) \quad (3)$$

165 Where $N(\mu_j, \Sigma_j)$ is the normal distribution with mean μ_j and covariance Σ_j ,

166 K is the number of clusters, and π_j is the mixture proportion.

167 3. An Expectation–Maximization Algorithm determines π_j, μ_j, Σ_j for K clusters

168 4. Density estimation gives us $P(x_i \in k_j) = p_{ij}$

169 5. Maximum p_{ij} is the assigned cluster for point x_i

170 The mixture model clustering is based on the R package ‘Mclust’ developed by Fraley et al. (2012), which builds upon
171 the theoretical work of Fraley and Raftery (2002) for model-based clustering and density estimation. The process uses
172 an Expectation-Maximization algorithm to cluster the dataset, estimating a variable number of distinct multivariate
173 Gaussian distributions from a sample dataset. Training the Gaussian mixture model on this dataset provides a
174 clustering function which outputs a unique cluster for any data point with the same number of variables.

175 In one dimension, a Gaussian mixture model looks like the distributions depicted in Figure 5: instead of modelling a
176 population as a single distribution (Gaussian or otherwise), the GMM algorithm fits multiple Gaussian distributions
177 to a population. A key aspect is that this algorithm has the capability of assigning a new point to the most likely
178 distribution. For example, in the 1-D figure, a normalized AMV estimate with a value of 10 would be more likely to
179 originate from the broad cluster ‘2’ than the narrow cluster ‘4’. In this case, we model the population as a Gaussian
180 mixture model in five-dimensional space, which consists of two simulated true wind vector components (u and v),
181 two AMV estimates of these wind components (\hat{u} and \hat{v}), and the simulated water vapor values, all of which have
182 been standardized. Each cluster has a 5-dimensional mean vector for the center and a 5x5 covariance matrix defining
183 their multivariate Gaussian shape. The estimation of a covariance matrix allows for the characterization of the
184 relationships between the different dimensions within each cluster, and as such the gaussian mixture model approach
185 provides greater potential for understanding the geophysical basis of error regimes than other unsupervised clustering
186 approaches.

187 In Figure 6, we applied the Gaussian mixture model to true u and v wind data using 9 clusters. Although Figure 4
188 indicates that the data tends to separate roughly into ‘skilled’ and ‘unskilled’ regimes, we opted to choose 9 clusters
189 in the Gaussian mixture model after several sensitivity tests across all pressure levels found 9 to be the minimum
190 number of clusters needed to ensure the separation into these separate regimes, as well as allowing for further
191 stratification of sub-regimes within the skilled and unskilled regimes

192 By re-analyzing the AMV estimate in relation to the simulated true winds, separated into the cluster that each point
193 has been assigned to (Figure 6), we find that the clustering approach successfully separates the AMV estimates
194 according to their ‘skillfulness’. Essentially, we repeat Figure 3 but divide the AMV estimates by cluster. We see that,



195 for example, clusters 4, 5, and 7 clearly represent cases in which the feature-tracking algorithm provides an accurate
196 estimate of the true winds, with very low variance around the one-to-one line (i.e., low estimate errors). Clusters 1, 2,
197 3, and 9 are somewhat noisier than the low-variance clusters, with error characteristics similar to those of the entirety
198 of the dataset. Clusters 6 and 8, on the other hand, are clearly unskilled in different ways. Cluster 6 is a noisy regime,
199 which captures much of the more extreme differences between the AMV estimates and the simulated true winds.
200 Cluster 8, on the other hand, represents the low AMV estimate, high true wind regime. This cluster is returning AMVs
201 with values of zero where the true wind is clearly non-zero because of the very low water vapor present. We see that
202 the clustering algorithm succeeds in capturing physically interpretable clusters without having any knowledge of the
203 underlying physical dynamics. We further see the stratification of the regimes when analyzing the absolute AMV error
204 in relation to the water vapor content (Figure 7). We see that clusters that have similar behaviors in the error pattern
205 (such as 1, 2, and 3) represent different regimes of water vapor content.

206 **3.5 Random Forest**

207 The clustering algorithm requires the true wind vector component values (u and v) in order to classify the AMV error.
208 When applying the algorithm in practice to tracked AMV wind from real observations, the true winds are unknown.
209 Therefore, we develop a proxy for the true winds using only the AMV estimates and the simulated water vapor itself.
210 This is an instance in which the application of machine learning is desirable, since machine learning excels at learning
211 high-dimensional non-linear relationships from large training datasets. In this case, we specifically use random forest
212 to create an algorithm which predicts the true wind values as a function of the tracked wind values and water vapor.

213 Random forest is a machine learning regression algorithm which, as detailed by Breiman (2001), employs an ensemble
214 of decision trees to model a nonlinear relationship between a response and a set of predictors from a training dataset.
215 Here, we chose random forest specifically because it possesses certain robustness properties that are more appropriate
216 for our applications than other machine learning methods. For instance, random forest will not predict values that are
217 outside the minimum and maximum range of the input dataset, whereas other methods such as neural networks can
218 certainly exceed the training range, sometimes considerably so. Random forest, due to the sampling procedure
219 employed during training, also tends to be robust to overtraining in addition to requiring fewer tuning parameters
220 compared with methods such as neural networks.

221 We trained a random forest with 50 trees on a separate set of tracked winds and water vapor values to predict true
222 winds using the ‘randomForest’ package in R. While the random forest estimate as a whole does not perform much
223 better than the AMV values in estimating the true wind (2.89 RMSE for random forest vs 2.91 RMSE for AMVs), as
224 shown in Figure 8, it does not display the same discrete regimentation as the AMV estimates in Figure 3. Relative to
225 the AMV estimates, the error in each of the random forest estimates is closer to the mean of error of the entire dataset.
226 As such, the random forest estimates can act as a proxy for true wind values in our clustering algorithm — they remove
227 the regimentation which is a critical distinction between the AMV estimates and the true wind values.



228 3.6 Finalized Error Characterization Model

229 The foundation of the error characterization approach is to combine the random forest and clustering algorithm. We
230 apply the Gaussian mixture model, as trained on the true winds (in addition to the AMVs and water vapor), to each
231 point of water vapor, AMV estimate, and associated random forest estimate. This produces a set of clusters which,
232 when implemented, require no direct knowledge of the actual true state (Figure 9). We see that the algorithm manages
233 to separate the AMV estimates into appropriate error clusters. Once again, clusters 6 and 8 manage to capture unskilled
234 regimes, and clusters 4 and 5 remain extremely skillful. While there is some degradation in the performance relative
235 to the classification algorithm on the training set, we see in Figure 9 and Figure 10 that the error characterization still
236 discretizes the testing data set into meaningful error regimes.

237 By taking the mean and standard deviation of the difference between AMV estimates and true winds in each cluster,
238 we develop error characteristics for each cluster (Figure 11); these quantities are precisely the bias and uncertainty
239 that we require for the cost function J in Eq (1). We see that the unskilled clusters have very high standard errors and
240 they correspond roughly to the areas of unskilled regimes in Figure 3. Since each cluster now has associated error
241 characteristics (e.g., bias and standard deviation), it is then straightforward to assign the bias and uncertainty for any
242 new tracked wind observation by computing which regime it is likely to belong to.

243 3.7 Experimental Set up

244 In this section we will describe our experimental setup for training the data and testing its performance on a withheld
245 dataset. We divide the dataset into two parts: a training set consisting of the first 1.5 months of the GEOS-5 Nature
246 Run, and a testing set consisting of the last 0.5 month of the Nature Run. Our training/testing procedure for the
247 simulation data and tracked wind is as follows:

- 248 1. Divide the simulation data and tracked wind into two sets: training set of 1,000,000 points from the first 1.5
249 months of the Nature Run and a testing set of 1,000,000 points from the final 0.5 months of the Nature Run.
- 250 2. Using the ‘density.Mclust’ function, we train a Gaussian Mixture Model on a normalized random sample of
251 observations from the training dataset of true winds (u and v direction), tracked winds (u and v direction),
252 and water vapor with $n=9$ clusters.
- 253 3. We train two separate random forests on a different random sample of 750,000 observations from the training
254 dataset. We use tracked wind (u and v direction) and water vapor to model, separately, true winds in both the
255 u and v directions.
- 256 4. We apply the random forests to the dataset used for the Gaussian Mixture Model. This provides a random
257 forest estimate for each point, which is used as a substitute for true wind values in the next step.
- 258 5. Using the ‘predict.Mclust’ function, we predict the Gaussian mixture component assignment for each point
259 of water vapor, tracked winds, and random forest estimate.



- 260 6. We compute the mean and standard deviation of the difference between the tracked winds and the true winds,
261 per direction, for each Gaussian mixture model cluster assignment. This provides a set of error characteristics
262 that are specific to each cluster.
- 263 7. We can apply the random forest, and then the cluster estimation, to any set of water vapor and tracked AMV
264 estimates. Thusly, any set of tracked AMV estimates and water vapor can be mapped to a specific cluster,
265 and therefore its associated error characteristics.

266 4 Results and Validation

267 In this section, we compare our clustering method against a simple alternative, and we quantitatively demonstrate
268 improvements that result from our error characterization. Recall that in Section 3, we divided the wind-tracking
269 outputs into 9 regimes, which range from very skilled to unskilled. For each regime, we can quantify the uncertainty
270 via a 95% confidence interval, which in the Gaussian case can easily be constructed as $[x_i - 2 \sigma_i, x_i + 2 \sigma_i]$, where x_i
271 the predicted mean and σ_i is the predicted standard deviation of the i -th cluster. To test the bias of our confidence
272 interval, we divide the dataset described in Section 2 into a training dataset (first 1.5 month) and a testing dataset (last
273 0.5 month). Having trained our model using the training dataset, we apply the methodology to the testing dataset, and
274 we compare the performance of the predicted confidence intervals against the actual wind error (tracked winds - true
275 winds). This is a type of probabilistic forecast assessment, and in this paper we assess the quality of the prediction
276 using a scoring rule called continuous ranked probability score, which is defined as a function of a probabilistic
277 forecast F (here represented by our confidence interval) and an observation x as follows:

$$278 \quad \text{CPRS}(F, x) = \int_{-\infty}^{\infty} (F(x) - \mathbb{1}(y - x))^2 dy \quad (4)$$

279 Where $\mathbb{1}(\cdot)$ is the Heaviside step function and denotes a step function along the real line that is equal to 1 if the argument
280 is positive or zero, and it is equal zero if the argument is negative. The continuous rank probability score here is strictly
281 proper, which means that the function $\text{CPRS}(F, x)$ attains the maximum if the data x is drawn from the same probability
282 distribution as the probabilistic forecast F . That is, if the data x is drawn from F , then $\text{CRPS}(F, x) \leq \text{CRPS}(G, x)$ for
283 all $G \neq F$.

284 The alternative error characterization method that we test against is a simple marginal mean and marginal standard
285 deviation of the entire track - true wind datasets. This is essentially equivalent to an error characterization scheme that
286 utilizes one regime, and its confidence interval similarly could be constructed as $[x - 2 \sigma, x + 2 \sigma]$, where x and σ are
287 the marginal mean and marginal standard deviation of the residuals (i.e., tracked wind minus true winds). Here, we
288 use a negatively oriented version of the CRPS (i.e., Eq.(4) without the minus sign), which implies that lower is better,
289 to evaluate the performance of our methodology against the naive error characterization method. We plot the histogram
290 of the scores in Figure 12.



291 The relative behavior of the CRPS is consistent between u and v winds. The CRPS tends to have a wider distribution
292 when applied to the regime-based error characterization. Compared to the alternative error characterization scheme,
293 our methodology produces a cluster of highly accurate predictions (low CRPS scores), in addition to some cluster of
294 very uninformative predictions (high CRPS scores). These clusters likely correspond to the highly skilled cluster (e.g.,
295 Cluster 3) and the unskilled clusters (Cluster 5 and 8), respectively. Overall, the mean of the CRPS is lower for our
296 methodology than it is for the alternative method, indicating that as a whole our method produces a more accurate
297 probabilistic forecast.

298 Thus far we have shown that our method produces more accurate error-characterization than an alternative method
299 based on marginal means and variance. Now, we assess whether our methodology provides valid probabilistic
300 prediction; that is, we test whether the uncertainty estimates provided are consistent with the empirical distribution of
301 the validation data. To assess this, we construct a metric in which we normalize the difference between the true wind
302 and the tracked wind by the predicted variance. That is, we compute the normalized values for u and v using the
303 following equations:

$$304 \quad z_u = \frac{u - \hat{u}}{\sigma_u}$$
$$305 \quad z_v = \frac{v - \hat{v}}{\sigma_v} \quad (5)$$

306 Where u is the true u wind from the Nature Run data, \hat{u} is the tracked-wind, and σ_u is the error as assessed by our
307 model. The values for the v-wind are defined similarly. The residuals in Eq (5) can be considered as a variant of the
308 z-score, and it is straightforward to see that if our error estimates are valid (i.e., accurate), then the normalized residuals
309 in Eq. (5) should have a standard deviation of 1. In Figure 12, we display the histogram of the normalized residuals
310 z_u and z_v . It is clear that for both types of wind, our error characterization methodology produces highly accurate
311 uncertainties (std = 1.003 and 1.009 for u and v, respectively).

312 **5 Conclusion**

313 Uncertainty quantification, which is the quantification of an imperfect or incomplete state of knowledge within a
314 model, is an important component of data validation and scientific analysis. For wind-tracking algorithms, whose
315 outputs (tracked u and v) are often used as observations in data assimilation analyses, it is necessary to accurately
316 characterize the bias and standard error (e.g., see Section 2.2). Nguyen et al. (2019) illustrated that incorrect
317 specification of these uncertainties (a and R in Eq. (1)) can adversely affect the assimilation results –
318 mischaracterization of bias will assimilate an incorrect tracked wind, while an erroneous standard error could
319 incorrectly weight the cost function.



320 In this paper, we develop an error-characterization scheme based on random forest and mixture model clustering.
321 Here, the mixture of a parametric approach and a machine learning method allows us to combine the flexibility of
322 machine learning with the interpretability of mixture modelling in an entirely data-driven framework. In theory, the
323 fidelity of our method should scale with the number of training data observations, making the methodology well-
324 suited for the massive datasets that are typical within remote sensing applications. Our error function has been applied
325 to an AMV OSSE study using GEOS5 and its impact will be reported in a forthcoming paper.

326 We demonstrate that our methodology produces accurate error estimates (also called validity), and that it is able to
327 identify and remove the biases within the wind-tracking algorithm's outputs. Particularly, the methodology is able to
328 identify unskilled regimes that are physically meaningful — in our case, unskilled regimes related to regions of near-
329 zero water vapor content. We note that our methodology is able to find this dependence between unskilled regimes
330 and low water content without any prior knowledge or specification from the user, deducing the relationship from the
331 underlying multivariate distribution of water vapor, true wind, and tracked wind. While we position the methodology
332 as an error characterization tool, this property also makes it useful as an exploratory tool to aid in understanding the
333 distribution of multivariate and potentially complex data.

334 Our algorithm consists of two parts: an emulator and a clustering algorithm. In this implementation, random forest
335 and Gaussian mixture modelling are the approaches; in theory, these two steps could be accomplished using other
336 algorithms belonging to the appropriate class. Future research includes replacing random forest with other machine
337 learning methods such as neural networks or support vector machines, and investigating other methods of clustering,
338 such as self-organizing networks. We note that the issue of bias removal in data assimilation and in remote sensing is
339 certainly not limited to atmospheric motion vectors. The methods we have used to characterize uncertainties in AMVs
340 are general, and can be applied to other inverse problems as well.

341 **Author Contribution**

342 Teixeira and Nguyen conceived of the idea. Teixeira performed the computation. Wu provided the experimental
343 datasets. Posselt and Su provided subject matter expertise. All discussed the results. Teixeira wrote the manuscript.
344 All authors contributed to the subsequent draft.

345 **Competing Interest:** The Authors declare no conflict of interest.

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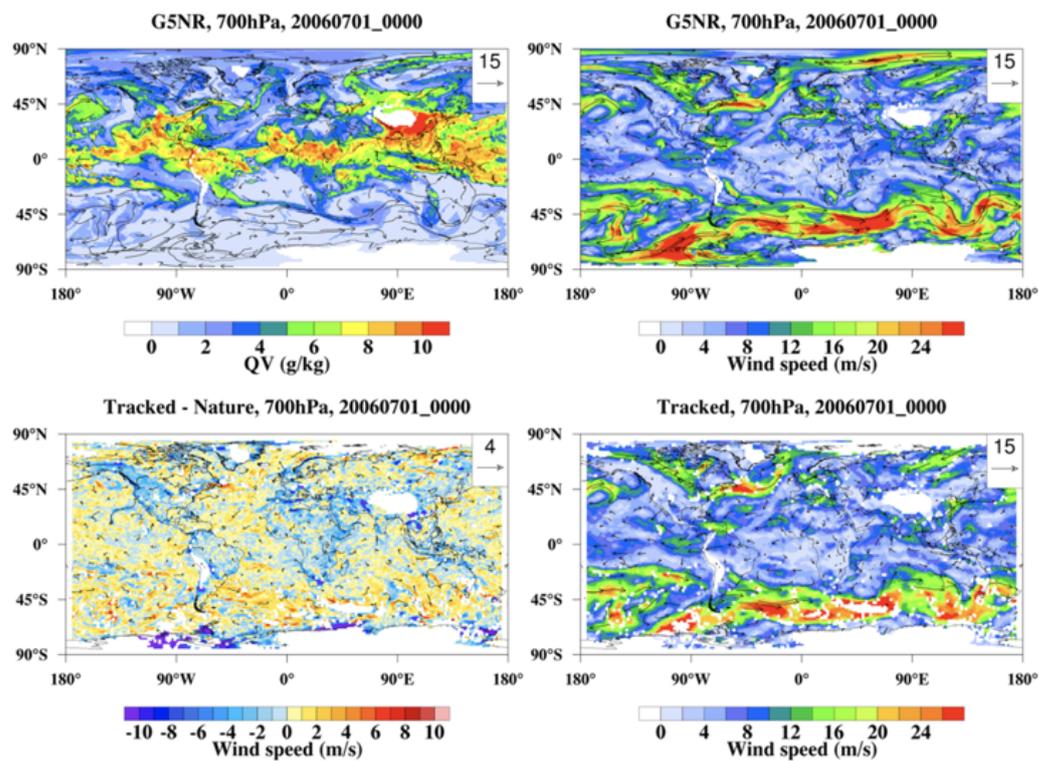
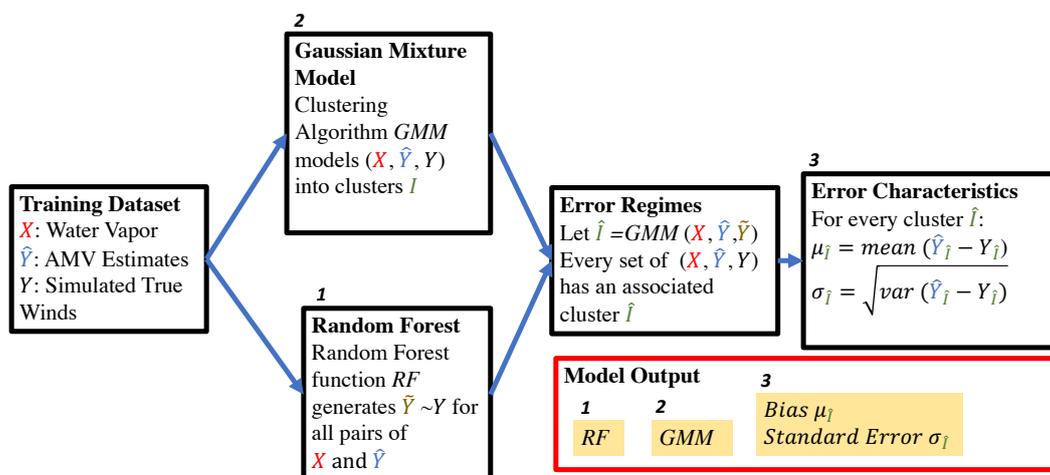


Figure 1: Map of Nature Run at one timestep at 700hPa (A): Water Vapor (B): True Wind Speed (C): Difference between True Wind Speed and AMV Estimate (D): AMV Estimate.

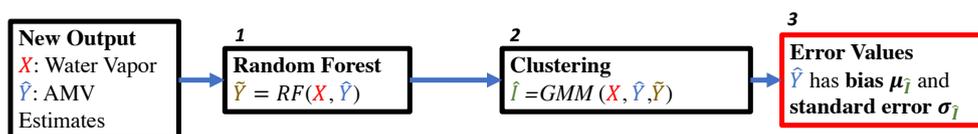


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1. Training

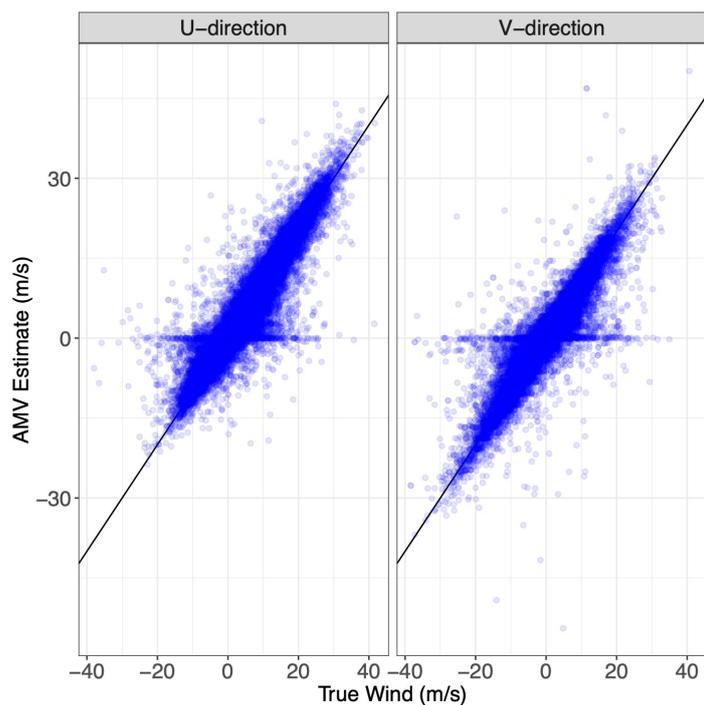


2. Implementation



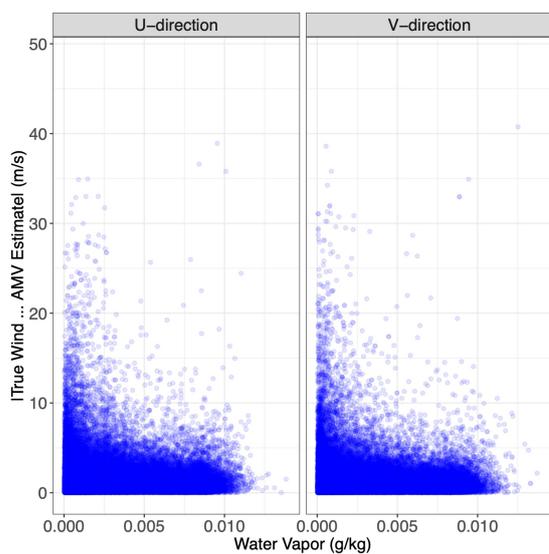
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405 **Figure 2: Diagram of Training Approach and Diagram of Implementation steps.**



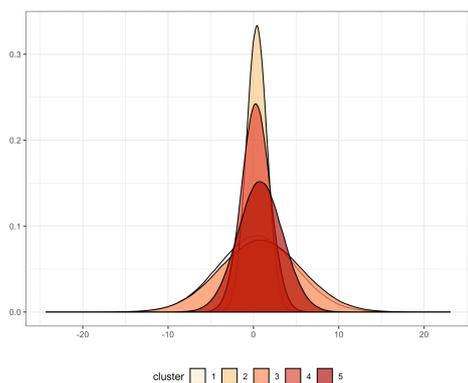
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407 **Figure 3: Scatter plot of the simulated true wind vs AMV estimates for u and v wind.**



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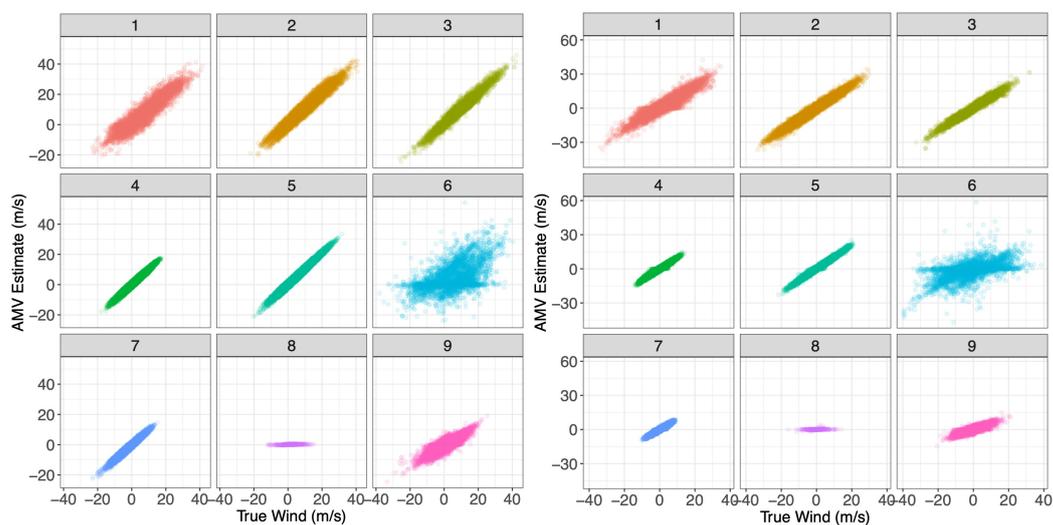
409 **Figure 4: Simulated water vapor vs the absolute value of the difference between true and tracked winds.**



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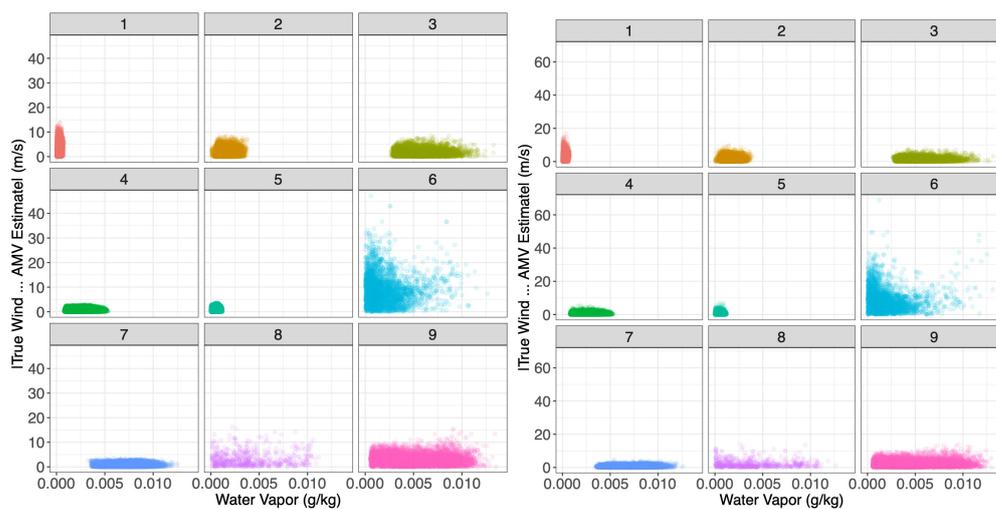
411 **Figure 5: Example of Gaussian Mixture Model in one dimension. Density Figures for the U-Direction AMV**
412 **Estimate dimension of fitted Gaussian mixture.**

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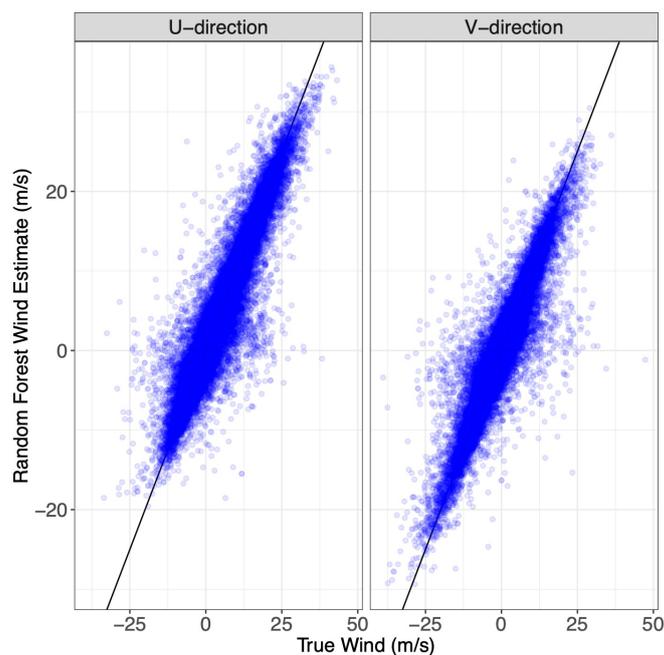
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415 **Figure 6: Scatterplot of simulated true wind vs AMV Estimates, each sub-panel corresponding to the specific**
416 **Gaussian mixture component to which each point has been assigned. (A): U-Direction Wind (B): V-Direction**
417 **Wind.**



418

419 **Figure 7: Scatterplot of Water Vapor vs Absolute Tracked Wind Error, each sub-panel corresponding to the**
420 **specific Gaussian mixture component to which each point has been assigned. (A): U-Direction Wind (B): V-**
421 **Direction Wind.**

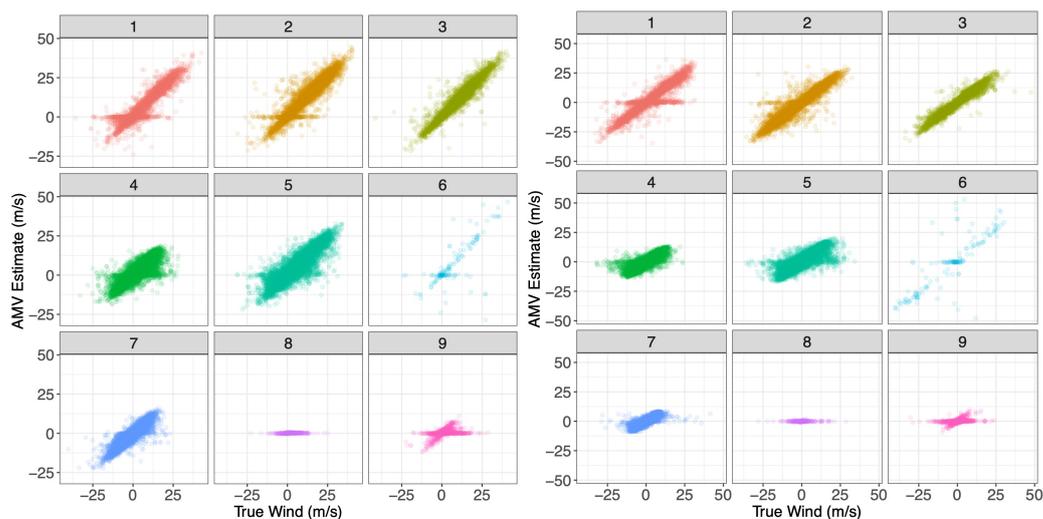


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423 **Figure 8: Scatterplot of true wind estimate vs random forest produced estimate. (A): U Direction (B): V**
424 **Direction**

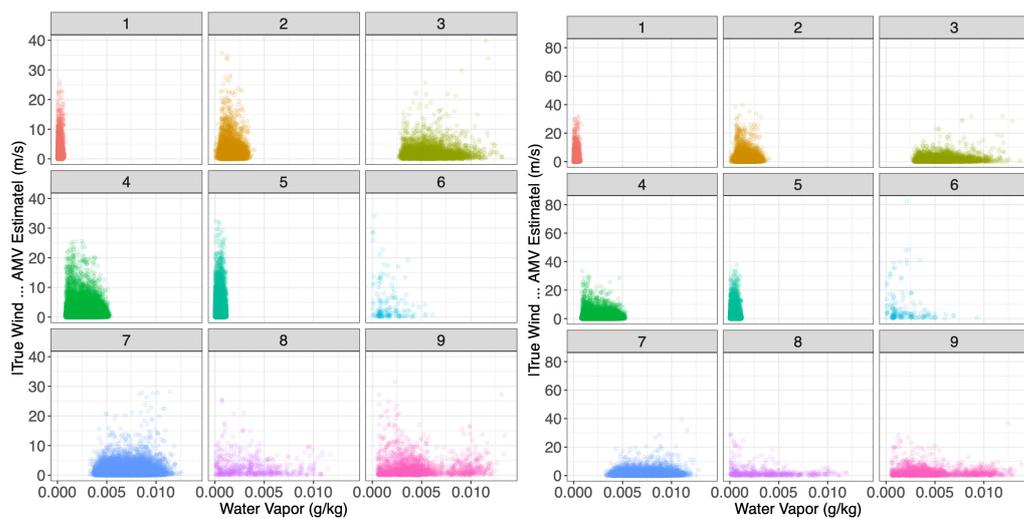


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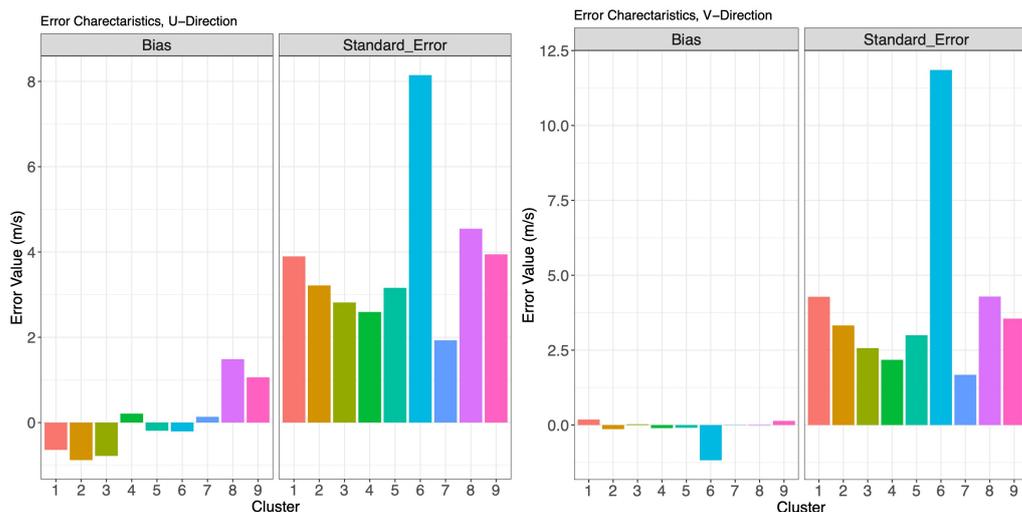
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427 **Figure 9: Scatterplot of simulated true wind vs AMV Estimates, each sub-panel corresponding to the specific**
428 **Gaussian mixture component to which each point has been assigned when the true wind value has been**
429 **substituted by the random estimate. (A): U-Direction Wind (B): V-Direction Wind**



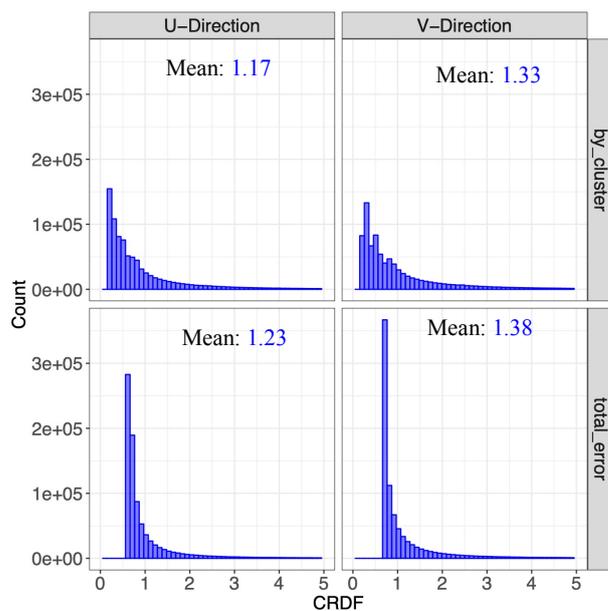
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431 **Figure 10: Water Vapor vs Absolute Tracked Wind Error, each sub-panel corresponding to the specific**
432 **Gaussian mixture component each point has been assigned when the true wind value has been substituted by**
433 **the random estimate. (A): U-Direction Wind (B): V-Direction Wind**



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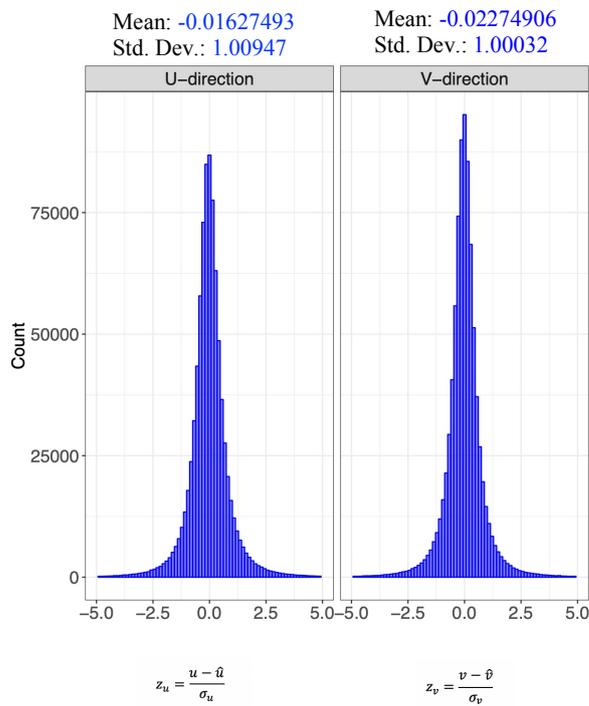
435 **Figure 11: (A): Bias (Left Panel) and Standard Error (Right Panel) for each Gaussian mixture cluster in**
 436 **figure 6, U direction. (B): Same as (A) for V-direction**



437

438 **Figure 12: CRSP applied to different error approaches. (A): Cluster Errors for U Winds (B): Total Errors**
 439 **for U Winds (C): Cluster Errors for V Winds (D): Total Errors for V Winds.**

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443 **Figure 13: U and V winds normalized using Error Clusters**

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