Response to editor’s comments on:  
*On the information content in linear horizontal gradients estimated from space geodesy observations*

by Gunnar Elgered, Tong Ning, Peter Forkman, and Rüdiger Haas

**Introduction**

We are grateful for the many good ideas proposed as well as making us aware of a couple of mistakes. Most of them are accepted and implemented as suggested. In a few cases, we have made compromises. The details are described below where the editor’s comments are in black text and our responses are in red text.

**General comments:**

Goal of the study: it is stated in the Abstract and in the Introduction that the goal is to assess the quality of the GPS gradient estimates based on comparisons with independent data: ECMWF model, WVR and VLBI observations. State more clearly which scientific questions you are addressing and justify the study scenario (why you test several specific processing options) and the use of each of the data sources (how each of the data sources helps you to address part of the questions). The specific advantages/disadvantages and the complementarity of the reference data sources and their uncertainties should be introduced as well.

A new subsection at the end of Section 3 includes formal uncertainties and specifies the comparisons made over different time scales. In Section 4 we focus on comparisons between total gradients from GPS and ECMWF data with a temporal resolution limited to 6 h. Because the ECMWF offer both wet and hydrostatic gradients we also study them separately as monthly means (Figure 9) and the trends (Table 8). In Section 5 we focus on comparisons of wet gradients from GPS and the WVR with a temporal resolution of 15 min. One exception is in Section 5.3 where we use the CONT14 VLBI campaign as a case study, although the temporal resolution of the VLBI data is 6 h.

My feeling is that the study would be better presented as an inter-comparison/inter-validation rather than an assessment of GPS gradients because the gradients from the various reference data sources don’t agree very well... I think understanding properly the uncertainties and limitations of all the data sources used in this study is the main point of the paper and it needs to be enhanced. In this respect, I suggest that you also compare the ECMWF wet gradients to the WVR data in Section 5.1. Probably this sub-section should be split in two (as also suggested by one of the reviewers) and the GPS processing tests and the other tests (GPS vs. WVR and ECMWF vs. WVR) might be addressed separately.

We agree that it is difficult to state that any one of the different data sources is superior in accuracy. The word “assessment” is interpreted differently by different persons whereas a comparison is just a comparison. With this in mind we have changed the wording (avoiding the word assessment except in a couple of places and also added motivations for the work in the Introduction. The former Section 5.1 is now also split into two sections as suggested. The ECMWF gradients did not add any information when compared to the VLBI and the WVR data (Subsection 5.3). In Subsections 5.1 and 5.2 we focus on the 15-minute data from the WVR and GPS. However, we added the Table 7 with ECMWF results for the 5 stations in Subsection 4.2 and the trends in Subsection 4.3.

Section 4. Comparisons with ECMWF at seasonal scale: two features in the ECMWF gradients are highlighted at ONSA station: 1) the persistent NS hydrostatic gradient and its seasonal variation (with winter maxima); 2) the increased EW wet gradient in summer. The hydrostatic feature is attributed to the influence of the Icelandic low pressure. I think the Icelandic low is not the only pressure system influencing the surface pressure variations in the region and it is located quite a distance to
the West from the study area, so its direct influence would rather be in the EW direction. If the main seasonal changes are in the NS gradient, there must be influence of other centres (e.g. Arctic Oscillation), unless the gradients are of a more local nature. Can you elaborate be a bit more on the processes involved and their impact on the regional pressure field (e.g. inspect mean sea level pressure maps from ECMWF analyses and time series of observed surface pressure in Iceland and Sweden, etc.). This would help to better understand the information content in the GPS gradients.

Our interpretation is that the “Icelandic low” (documented already in 1944) is a phenomenon which is a component also in the North Atlantic Oscillation and the Arctic oscillation, see Thompson and Wallace (1998). The text is expanded by mentioning all three phenomena. When studying the mean sea level pressure distribution over Sweden there is mainly a north-south component in the winter. We now, in Section 4.2, mention the ERA-40 Atlas (openly available via internet), which shows this north-south winter gradient in the mean sea level pressure very clearly.

Regarding the 2nd feature, sea breeze circulation is hypothesized which is a rather local phenomenon driven by a temperature and pressure gradient between sea and land. Again, can you be a bit more descriptive and quantitative about the local pressure, temperature, and humidity gradients in the vicinity of the GPS stations to support this assumption? Note that all these variables are available from the ECWMF analyses.

We have rewritten this part to stress that this is one possible explanation. For this paper we do not have the expertise in meteorological high-resolution models available to verify which large east gradients that clearly are associated with sea breeze conditions. (Also, we do only right now have access to the ECWMF gradients calculated by the Vienna group.) We believe that a separate study is needed in order to obtain good and reliable results. It is therefore mentioned as future work in the conclusions section.

You wrote that the results for the four other stations are identical (except KIR0, so rather write “for the three nearby stations MAR6, SPT0, and VIS0”). However, I would not expect that the changes in the wet gradients are identical because sea breeze is a local feature which depends on the orientation of the coastline (and not all coastlines in your study area are identically oriented). Please reformulate and be more specific on which features are seen and explained at the other sites.

This was a mistake. The text has been rewritten. Now we first state that the results are similar, rather than identical, and then we comment on the differences, the drier air in Kiruna and the sea breeze, or other coastline phenomena, at the Onsala site.

In Figure 10, the dispersion of the results for each month (which I interpret as interannual variability) is much larger in the GPS series than in the ECMWF series. Can you comment on this feature? Is GPS over-estimating the gradients and their variability or is ECMWF underestimating them?

It is impossible to say. However, the issue of gradient sizes estimated from GPS data is now further illuminated with the new Table 11. Based on this, one may guess that if we would have used a 3° cutoff angle also in the 11-year study, the GPS gradients would have been approximately 20 % lower.

Section 5 now includes a lot of new material but the objectives and methods become a bit blurred. Please add a short rationale at the beginning of each sub-section and/or before you comment the results. E.g. What is the purpose of including systematically the two collocated GPS stations ONS1 and ONSA in all graphs? Why do you compare both total gradients and wet gradients in this section? (wouldn’t be better to separate hydrostatic and wet gradients? Or focus only on wet gradients?). The reason to include both ONSA and ONS1 is because of the different antenna environments. We now state that in the beginning of Section 5.

It does not really matter if one studies wet or total gradients over these short time scales.

Nevertheless, to make it less confusing for the reader, we now focus on total gradients in Section 4.
and wet gradients in Section 5 (where we only use ECMWF hydrostatic gradients to infer the wet
gradients from GPS and VLBI).

Water Vapour Radiometer results: the WVR gives much larger wet gradients. Your interpretation is
that this is due to the absence of constraints between estimates. I don’t understand how the
increased variability would increase the amplitude of the mean gradients. Or in the opposite
situation, why would adding constraints in the processing change the monthly means? I think it
would only reduce the short-term variability. Probably the contamination from liquid water in the
measurements is a better explanation (but I am not an expert in these measurements). Could they
explain the spikes in Fig. 15 and 17? Did you check the results after a more severe editing of the WVR
data?
You are correct, it is only over short time scales that the absence of constraints is relevant.
We carried out a test when editing away all data when the liquid water content > 0.3 mm. The
impact on overall gradient sizes was insignificant. This finding is added to the text in a list with
possible explanations, e.g. Table 11 showing the impact on the estimated gradient amplitude for the
different cutoff angles.

P20L29: I think the uncertainty due to the mapping function is still critical. The 17% reported by
Kacmarik 2018 which you mention would explain about half of the bias seen in Fig. 11. There might
also be a similar uncertainty associated with the mapping function used in the estimation of the WVR
gradients. Can you comment on this? (btw, the type of mapping function is not specified in Section
3.2).
We made an error in this discussion. Both the WVR and GPS use the Bar-Sever gradient mapping
function. The mapping function for the WVR is now stated in Section 3.2. As mentioned above we
now list possible explanations for differences in the gradient size from WVR and GPS data.

You conclude that the results for a cutoff angle of 3° are the best, though the difference with a cutoff
angle of 10° is very small. Is this difference statistically significant?
The changes are from 0.66 to 0.68 in the east and 0.62 to 0.64 in the north component.
The 95 % confidence interval for correlations of these sizes, and approximately 80,000 data pairs is
±0.004, so yes, in a statistical sense the differences are significant. The confidence interval is now
specifically mentioned.

P21: “The solution giving the best agreement, when comparing gradients from ONSA and ONS1 data
with each other, is the one with elevation dependent weighting, whereas the comparisons with the
WVR, for both ONSA and ONS1 give the best agreement without weighting.” This result merits
further comments and interpretation.
The following text is added:
“The choice of elevation cutoff angle is a compromise between having a good geometry and avoiding
the effects of signal multipath. Our interpretation is that the gradients from ONSA and ONS1 are
estimated based on very similar observational directions and have common error sources, such as
orbit errors, resulting in correlations around 0.9. In order to increase an already high correlation the
observations at the lowest elevation angles are not that important, since multipath effects will be
more and more different the closer to the horizon the observations are made. When ONSA and ONS1
gradients are compared to those from the WVR the situation is different because these gradients are
independent and the geometry of the GPS observations becomes more important in order to
estimate a more accurate gradient, although we note that the correlation is here reduced to around
0.6.”
Specific comments:
Please be consistent in the denomination of the gradients throughout the paper. In some places you write “linear horizontal gradients” (e.g. captions of Table4), or “linear gradients” (P18L10), and most of the time “gradients”. I think the latter is fine.
Now we just have “linear horizontal gradients” in the title and when first mentioned in the abstract and in the introduction, just to be clear about which type of gradients we study. Thereafter, we just use “gradients”.

Abstract: P14-5: “GPS gradients confirm known seasonal effects both in the hydrostatic and the wet components” this sentence suggests that GPS is used to confirm the seasonal feature, but maybe you rather want to write that “GPS is able to reproduce / detect / monitor” the known seasonal effects since the purpose here is to assess GPS... By the way, I have 2 more comments: 1) I am not sure the seasonal effects in delay gradients in this region is something well known (the fact that it is well represented in the ECMWF model doesn’t mean that it is well known) and 2) GPS cannot confirm the hydrostatic and wet components because GPS is measuring the total gradients... So this sentence needs be reformulated.
The sentence in the abstract is rewritten without using the “well known” wording and instead noting that effects due to wet and hydrostatic components are detected.

Section 2: I think the basic definitions and modelling of gradients from the paper by Davis et al., 1993, don’t need to be repeated here. If you need to refer to specific equations and variables you can cite them from Davis’ paper, or alternatively move the equations in an Appendix. In this section, mainly Equation (6) and some text from paragraph P4L7-17 might be kept and moved to the beginning of the section. Additional references worth mentioning because they describe atmospheric processes that can be sensed by the GPS gradients are given below (Koulali Idrissi et al., 2011, and Nahmani et al., 2019).
The equations were added in the previous revision as an introduction to the model, Equation (6), where the latter was requested by the referees. They would be helpful for the less experienced reader but as the manuscript now also is much longer we agree, and keep only Equation (6) now Equation (1). We also added the definition of gradient amplitude.
The two suggested references are now complementing the previous ones.

Figure 1 is a very simplified version of the reality. I suggest that you remove it as also suggested by a reviewer. Furthermore, the numerics that are given in the caption are not used in the text.
We think that the figure is a nice introduction to make the reader aware of the different volumes being averaged. On the other hand the manuscript is now much longer — see previous comment — and the figure is removed.

Figure 2: add latitude and longitude ticks.
Corrected in the new figure.

Table 2: add the information on elevation depending weighting
Footnote “b” of the table is updated. This is now Table 1. The previous Table 1 has been moved to the end of Section 3.

Section 3.2: how many observations are available in each estimation batch? What is the mapping functions used for the ZWD and gradient parameters?
This information is added to the caption of the new Figure 5. (100 observations in 15 minutes result in 10,000 observations per day, see Figure 6.)
In order to avoid ground-noise pickup the WVR provides observations of the wet delay in the different directions above 20°. Therefore a simple sin(EL) mapping function is used to relate these
slant wet delays to the equivalent ZWD. The model for gradient estimation uses the Bar Sever
gradient mapping function. This is now described in the text.

P9L20: “adjacent” -> “successive”?
We now use “successive”, also in Section 5 (confirmed by a native English speaker).

Section 3: it would be interesting to compare the formal errors for the estimated parameters (ZWD
and gradients) from the 3 techniques (GPS, WVR, VLBI).
We have added Subsection 3.5 in which Table 4 presents the typical formal errors for the remote
sensing techniques.

Figure 9: not easy to see something… Maybe plot just one year for the 6-hourly data. The monthly
values are more or less shown in Fig. 10, and the SD values should be given in a table similar to Table
5 (see comment below).
The figure was added in the previous revision due to a referee comment that we had not shown that
the hydrostatic gradients were less variable compared to the wet. We see this figure as introductory
material (similar to the photos of the GPS antenna installations and the WVR) since it is our input
data calculated by the Vienna group. It visualizes the differences for six hourly and monthly values
for the hydrostatic and wet gradients and is now referred to in the beginning of Subsection 4.3. One
can argue that one year is sufficient because the different years look very similar, on the other hand,
showing the four years illustrates the small differences from year to year, so we prefer to show the
full four years for the Onsala site, which is later studied in Section 5.

Figure 10: I guess each symbol in the plots is for one year, but why are more than 11 symbols plotted
for some of the months? Are the two stations ONSA and ONS1 superposed maybe?
A mistake was made in the GPS plot, including monthly data from before 2006, when no ECMWF
data were available. A correct plot is inserted.

Section 4.2: could focus on wet gradients only
Add a scatter plot of GPS and ECMWF wet gradients (similar to Fig. 13) to compare the range of
values from the two data sources.
The range of values can now be compared using the new Table 7 (ECMWF data) and Table 6 (GPS
data). For the monthly mean values also the upper two plots in Figure 9 is meaningful in this sense.
We produced a couple of scatter plots but decided that they did not add any additional information
to the two tables.

P18L8: “We assess the data quality…” If you mean the quality of GPS data, this assumes that ECMWF
is of higher quality which is probably not the case (this point should be discussed).
Correct, a better wording is “We study the differences …”

P18L15-20: Regarding the positive impact of microwave absorbing material at ONSA and SPT0,
statistical significance of the differences between correlation coefficients in Table 4 should be tested
to have an objective basis for this statement as the differences are very small. Moreover, it would be
good to include results for ONS1 here as it is claimed later (P24-25) that thanks to the different
mechanical structure at station ONS1, there is no need for microwave absorber. This has an
important practical implication.
The 95 % confidence interval for the correlation coefficient of 0.90 at ONSA is now explicitly stated.
The significance of the larger value at SPT0 (compared to the other 3 stations) is less but still
approximately at the 95 % level.
ONS1 data are only available for four of the years studied and since the statistical significance for the 11 years is just above what is required, 4 years of data will not be convincing. This issue should be revisited after a few years from today.

P19: Long term trends: did you estimate linear trends directly from the gradient components or from their anomalies? I guess even if the seasonal cycle is small, it should be removed. You don’t write if you analyse the GPS gradient trends only. How do they compare to the ECMWF trends? How do the trends for the hydrostatic and wet components differ? We did not remove a seasonal cycle. It would only make sense for the amplitude, but no trend is detected — the “signals” are too small.
Table 8, summarizing the estimated trend values from both ECMWF and GPS, has been added.

P19L8: “Given that horizontal gradients in general are small and that the larger values typically occur for a short time” how short a time do you mean here? Give numbers and associated processes.
New text: “Given that gradients in general are less than 1 mm and that the larger values typically occur over time scales from minutes to a few hours…”

P19L9-10: “An estimated gradient has a direction and from a time series we estimate trends for the east and the north gradients. Combining these two trends … offers the possibility to also search for trends in the total amplitude value of the gradient at the station” => “From the time series of the NS and EW gradient components we can compute trends for the two components but also for the amplitude of the gradient vector (refer to an equation that can be given in section 2 or in the Appendix)”. The text is modified and an equation defining the gradient amplitude is added in Section 2 as suggested.

P19L11-12: “total amplitude value of the gradient” and “total amplitude”… => Remove “total” (amplitude or magnitude involves both components by definition). Instead use “total” when you refer to the sum of the hydrostatic and wet components. But is it really useful to show the amplitude instead of the two components here as in all other sections the two components are shown
We changed the wordings as suggested. Yes, we think it is meaningful to here show the trends for both the components and the amplitude. It relates to the next comment. New text: “There can be a trend in the amplitude, even if there is no trend neither in the east nor in the north components. The amplitude is by definition never negative. A trend of larger east gradients can be balanced by a similar trend in larger west gradients resulting in no net trend in the east gradient component, but a trend in the gradient amplitude.”

P19L12-15: I don’t understand how a trend in amplitude can happen if there is not a trend in the EW or NS components… See previous comment. The text is now (hopefully) more understandable.

P19L15: the discussion is not easy to follow. It would help if you could include the trend estimates in Table 5.
We have changed the wording but did not find it easy to expand the table mixing trends and correlations. Instead the new Table 8 was added (see above).

Table 5: “horizontal wet gradient” -> “wet gradient”
I suggest that you add a similar table but with the ECMWF results. This would help to further document the consistency/differences between the two data sources at regional scale and at different time scales.

Done — this is now Table 7.

Section 5.1: the title could be changed to “test of GPS processing variants” or something similar

We have split the previous Section 5.1 into two (as suggested). The 1st one of these is now titled: “Test of GPS processing variants relative to WVR data”.

P20L29-30: “The uncertainty of the estimated gradient amplitude, to which the assumption of a linear model for the atmosphere is also contributing, is significantly larger.” I guess by “a linear model for the atmosphere” you mean a piece-wise linear function of time? However, I don’t understand the general meaning of the sentence (what is larger than what? and why?).

This part of text is totally rewritten and the new Table 11 is used instead to show the averaging effect for different elevation cutoff angles.

P21 and Fig. 11: “wet total gradient” same comments as above => “amplitude of the wet gradient”

Done!

Fig. 11: here you could also plot the standard deviations of the 15 min data for each month for the 3 data sources. I am wondering how different the standard deviations are (I guess WVR SDs are much larger). Another option would be to plot the SDs for the 2 components (NS and EW) in a separate Figure in the same format as Fig. 14.

The SD plots are added.

In the captions of Fig. 11: are all these correlation numbers really useful? Here we don’t have other stations to compare with (like in Table 4) and other results (Table 5) are given for EW and NS components. I suggest that you remove the numbers. From the figure it is quite clear that the 2 GPS series are in better agreement with each other than with the WVR series.

Yes, we agree and removed these sentences.

Fig. 12 and 13 could be merged.

These are now Figures 11 and 12. Figure 11 includes all simultaneously estimated original total gradients from ONSA and ONS1 whereas Figure 12 depicts the wet gradients and only includes the results when WVR data are available at the same time as ONSA or ONS1 data. Therefore, we prefer to have them separated and to present both of them. Then we can also make the point (in the text) about lower correlations between ONSA-ONS1 for wet gradients compared to the total gradients.

Fig. 13: use the same x and y limits in all plots.

Done!

P24, Fig. 14 shows the results for 4 years. Can you comment on the similarities/differences between years?

Could the month-to-month and year-to-year variability in the correlation coefficients shown in Fig. 14 be due to occasional spurious values in the WVR time series?

In October 2015, yes as already mentioned in the caption.

For the other months with low correlations the reason was simply that no large gradients occurred for that component during that month. This is now explicitly stated in the text.

Fig. 14: here you could add the SDs for the 2 components (NS and EW) to support the idea that the variability in the wet refractivity is larger in summer (P24).
We tried, but the plots became too “busy”. With the added SDs in Figure 10 we have shown the correlations between ZWD, its SD, and the wet gradient amplitudes over the seasons.

Section 5.2: The title doesn’t include ECMWF.
Why do you compare total gradients in Fig. 15? I think it is sufficient to show the hydrostatic gradients in Fig. 16 (very small variability) and compare only wet gradients in Fig. 15. However, it is difficult to distinguish the different data sources in Fig. 15. Maybe consider using different colours, or removing one GPS series, or split in two figures.
We have done the change and now study primarily the wet gradients in the whole Section 5. We increased the height of the figure (relative to the width) to improve the visibility, and included also the ZWD (as suggested below).

P27L4-5: “The left plot in Figure 8 may explain why the north gradient has a larger uncertainty at this specific time”. I am not sure I understand the explanation. Can you be more specific? This discussion was not conclusive and has been removed. Surprisingly, in spite of the fact that the hydrostatic gradients were relatively small during CONT14, the results for just the wet gradients became a bit different, which is seen when comparing the new Table 12 with the old Table 8.

Table 8: total gradients? 6-hourly data? Please add VLBI-ECMWF.
The ECMWF gradients do not add any information to the case study. Except that the hydrostatic gradients in Figure 14 are used to calculate wet gradients from the VLBI and the GPS data. The CONT14 session is too short to provide meaningful statistics. We prefer to use this example as a case study (as well as pointing out that future VLBI data with more frequent observations should improve the accuracy of the VLBI gradients).

P27L16: Figure 17 and 18: case study of day 135-136: can you describe briefly the meteorological situation?
We now describe briefly the warm front passage with some additional information about wind at the ground. We also added some text relating ZWD variations to the gradients (see also comment below on Figure 17).

P28L4 “Figure 5.2” => Figure 18.
Sorry, but we do not understand this comment/request.

Figure 17: maybe only wet gradients are necessary here. Don’t connect the VLBI symbols (it gives the impression that the variation is mis-represented whereas it is just under-sampled).
Although we do not compare the ZWD time series the ZWD helps to get the picture of changing air masses which sometimes is the likely cause of the wet gradients. (This is more obvious in Figure 16 with a better temporal resolution on the x axis.) Of course, it would then have been sufficient with only one ZWD time series, but since they are available and consistent (given their uncertainties) we chose to include the WVR, and the GPS with the better temporal resolutions, but add also the VLBI gradients because the case study is defined by the VLBI experiment.
The lines between the VLBI symbols have been removed as suggested.

Fig. 17 could be merged with Fig. 15.
Done!
On the information content in linear horizontal delay gradients estimated from space geodesy observations

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Abstract. We assess the quality of study estimated linear horizontal gradients in the atmospheric propagation delay above ground-based stations receiving signals from the Global Positioning System (GPS). Gradients are estimated from 11 years of observations from five stations in Sweden. Comparing these gradients with the corresponding ones from the European Centre for Medium-Range Weather Forecasts (ECMWF) analyses shows that GPS gradients confirm known seasonal effects both in detect effects over different time scales caused by the hydrostatic and the wet components. The two GPS stations equipped with microwave absorbing material below the antenna in general show higher correlation coefficients with the ECMWF gradients compared to the other three stations. We also estimated gradients using GPS data from two collocated antenna installations at the Onsala Space Observatory. Correlation coefficients for the east and the north wet gradients from GPS estimated with a temporal resolution of 15 minutes from GPS data can for specific months reach up to 0.8 when compared to simultaneously estimated wet gradients from microwave radiometry. The best agreement is obtained when an elevation cutoff angle of 3° is applied in the GPS data processing, in spite of the fact that the radiometer does not observe below 20°. Based on the four years of results we note a strong seasonal dependence in the correlation coefficients, from 0.3 during months with smaller gradients to 0.8 during months with larger gradients, typically during the warmer, and more humid, part of the year. Finally, a case study using a 15-day long continuous Very Long Baseline Interferometry (VLBI) campaign was carried out. The comparison of the gradients estimated from VLBI and GPS data indicates that a homogeneous and frequent sampling of the sky is a critical parameter.

1 Introduction

Space geodetic techniques, where the fundamental observable is a radio signal’s time of arrival at a station on the surface of the Earth, are affected by variations in the propagation velocity in the atmosphere. Because time measurements avoid problems related to accurate calibration, which are common for systems measuring different types of emissions, it is a common view that Global Navigation Satellite Systems (GNSS) have a long term stability and are well suited for climate monitoring, e.g. in terms of the atmospheric water vapour content. Estimates of the total propagation delay above a GNSS station can be used to determine the integrated amount of water vapour. It is also common practice to estimate two-dimensional horizontal
linear gradients for each station in the GNSS data processing, because it improves the reproducibility of estimated geodetic parameters, see e.g. (Bar-Sever et al., 1998).

We **assess the quality of the study** estimated gradients primarily from GPS data from Swedish GNSS stations by comparing these gradients to independent measurements. An important site is the Onsala Space Observatory where a geodetic Very Long Baseline Interferometry (VLBI) telescope and a water vapour radiometer (WVR) are installed **collocated to and collocated with** GNSS receiver stations. The overall goal of this study **is to study** the usefulness of GPS-derived gradients in atmospheric and climate research. Previous studies have been carried out using GPS/GNSS data from Onsala. Comparing the **horizontal gradients** derived from VLBI, GPS, and a WVR, Gradinarsky et al. (2000) found that when varying the constraint for the gradient variability from 0.2 to 5.6 mm/√ht the weighted root-mean-square (**RMS**) difference compared to the WVR gradients varied between 0.8 and 1.0 mm for both the GPS and the VLBI gradients. Using multi-GNSS observations, Li et al. (2015) found a significant increase in the correlation coefficient to about 0.6 when compared to ECMWF gradients, while the one for the GPS only was typically below 0.5. In addition, they found that the RMS difference of the gradient is reduced to about 25–35 % by multi-GNSS processing.

In Section 2 we give a short background on the cause of horizontal gradients that are sensed by the space geodetic techniques and the model used to estimate them. In Section 3 instruments, techniques, and their data are described. The results are presented in two sections. First, in Section 4, we **use compare** 11 years of data to study the **total gradients** from five Swedish GNSS stations and assess their quality by comparing them to gradients originating from the European Centre for Medium-Range Weather Forecasts (ECMWF) analyses. **Here we study seasonal dependence as well as estimates of long term trends.** In Section 5, we use data from two collocated GNSS stations (with different antenna installations) and one WVR to assess the accuracy of the gradients during station performances and differences between different GPS processing variants. **We also study the seasonal dependence of the estimated wet gradients over a 4-year period.** Within this period we also carry out a comparison to gradients estimated from a Finally, within this 4-year period a 15-day long VLBI campaign – Finally, in occurred which we use as a case study. In Section 6 we present our conclusions and discuss possible future studies of gradients.

## 2 Cause of horizontal gradients and models

The delay of space geodetic signals propagating through the atmosphere depends of the refractive index. Because the values are typically just above 1 it is practical to define the refractivity, \( N = 10^6 (n - 1) \). A common expression used for the refractivity is (??)

\[
N = k_1 \frac{p_d}{T} + k_2 \frac{e}{T} + k_3 \frac{e}{T^2}
\]

where \( p_d \) is the partial pressure of the dry constituents of air in hPa, \( e \) is the partial pressure of water vapour in hPa (i.e., the total pressure \( P = p_d + e \)), and \( T \) is the absolute temperature in K. The values of \( k_1, k_2, \) and \( k_3 \) are estimated from laboratory
experiments. For space geodetic applications it is meaningful to combine the terms resulting in two refractivity components, often referred to the hydrostatic \( (N_h) \) and the wet \( (N_w) \) components (Davis et al., 1985):

\[
N = N_h + N_w = k_1 \frac{P}{T} + k_3' \frac{e}{T^2}
\]

In order to define the integrated horizontal delay—define one hydrostatic and one wet component (Davis et al., 1985). For a horizontally stratified atmosphere it is then common practise to use equivalent zenith values for these components. Additionally we may define a horizontal linear gradient, that can be inferred from ground-based observations, we follow Davis et al. (1993) and start by expressing the refractivity as a function of the height \( z \), the horizontal vector \( \mathbf{x} \) (Davis et al., 1993), consisting of one east and one north component, and the time \( t \):

\[
N(\mathbf{x}; z; t) = N_0(z; t) + \xi(z; t) \cdot \mathbf{x}
\]

where \( N_0(z; t) \) is the vertical profile of the refractivity at \( \mathbf{x} = 0 \) and \( \xi(z; t) \) is the vertical profile of the horizontal gradient at \( \mathbf{x} = 0 \):

\[
\xi_i(z; t) = \left. \frac{\partial N(\mathbf{x}; z; t)}{\partial x_i} \right|_{\mathbf{x}=0}
\]

where the index \( i = 1, 2 \) denotes the east and the north direction, respectively. This leads to the following expression for the integrated horizontal delay gradient:

\[
\Xi = 10^{-6} \int_0^\infty dz \: z \: \xi(z)
\]

Hence, the vector \( \Xi \) has one east and one north component, which in turn also can be separated, into one hydrostatic and one wet component according to Eq. (19). The atmospheric volume that is more or less homogeneously sampled by ground-based sensors such as a GNSS station, a VLBI station, or a WVR, is illustrated in Figure 3.

A sketch showing that the atmospheric volume determining the estimated atmospheric parameters is a cone originating at the upward pointing arrow. The typical scale heights, \( h_s \) of the hydrostatic refractivity and the wet refractivity are of the order of 8 km and 2 km, respectively, but vary a lot globally and in time according to Eq. (19). For the hydrostatic refractivity the diameter of the cone at the scale height is 91 km \( (D_{10^\circ}) \) and 44 km \( (D_{20^\circ}) \) for the elevation cutoff angles equal to 10 and 20, respectively. The corresponding diameters for the cones representing the wet refractivity are 23 km and 11 km, respectively. Note that the horizontal and vertical scales are different.

Hydrostatic gradients are usually dominated by pressure gradients and exist mainly over global and regional scales (e.g. synoptic scale weather systems). For example the north gradient has a clear dependence on latitude when averaged over long
Temperature and especially water vapour can show strong horizontal gradients over small (kilometre) scales and the temporal variability is typically also much higher than that of the hydrostatic gradients, see e.g. Li et al. (2015). Hence, the large local gradients over a station are mainly caused by the variability in water vapour and the wet refractivity. Gradients can be significant during a passage of a weather front, e.g. Kačmařík et al. (2018) report gradient amplitudes of up to 3–4 mm during the passage of an occlusion front over Germany. Nahmani et al. (2019) have studied gradients during the passage of mesoscale convective systems in West Africa and Kouali et al. (2012) have shown correlations between gradients and precipitation and moisture fluxes in Morocco. Other specific weather phenomena that can cause horizontal variability in the partial pressure of water vapour, and hence also the wet refractivity, are sea breeze (Craig et al., 1945; Miller et al., 2003), cloud rolls (Brown, 1970) and convection processes in general.

We note that none of the known processes is expected to be strictly linear, but the strength in the geometry, the distribution of the observations on the sky, and the GNSS data quality have so far not motivated makes it difficult to determine additional atmospheric parameters of higher order.

The atmospheric parameters that are normally estimated when processing space geodesy data are an equivalent zenith wet delay and linear horizontal delay gradients in the east and the north directions. The uncertainties of the estimates depend on the geometry of the observations and the accuracy of the so called mapping functions, used to describe the estimated parameters dependence on the elevation angle, given the specific weather conditions at the site, at the time, see e.g. Boehm et al. (2006) and Kačmařík et al. (2018). The common model used to relate the observed delay along the line-of-sight, $\Delta L(\alpha, \varepsilon)$, and the estimated parameters (IERS Conventions, 2010) is also used in this study, i.e.

$$\Delta L(\alpha, \varepsilon) = m_h(\varepsilon) \Delta L_{h,z} + m_w(\varepsilon) \Delta L_{w,z} + m_g(\varepsilon) \left[ \Xi_e \sin \alpha + \Xi_n \cos \alpha \right]$$

(1)

where $m_h$, $m_w$, and $m_g$ are the mapping functions, depending on the elevation angle $\varepsilon$, for the hydrostatic and the wet delays, and the horizontal gradients, respectively; $\Delta L_{h,z}$ and $\Delta L_{w,z}$ are the equivalent hydrostatic and wet delays in the zenith direction; $\alpha$ is the azimuth angle, measured clockwise from the north, implying that $\Xi_e$ and $\Xi_n$ are the horizontal delay gradients in the east and in the north directions.

In addition to the east and the north gradient components we will also study the gradient amplitude, defined as

$$|\Xi| = \sqrt{\Xi_e^2 + \Xi_n^2}$$

(2)

The gradient amplitude is defined for the hydrostatic, the wet, and the total gradients.
3 Instrumentation and data

Figure 1. The six GPS stations used in the study. ONSA and ONS1 are collocated together with the VLBI telescope and the WVR at the Onsala Space Observatory.

We compare horizontal gradients estimated from GPS observations acquired at five sites and six antenna/receiver installations: Kiruna (KIR0), Mårtsbo (MAR6), Onsala (ONSA and ONS1), Borås (SPT0), and Visby (VIS0), with respect to VLBI, WVR, and ECMWF estimates. These stations are also part of the EUREF network (Bruyninx et al., 2012). Their geographic locations are shown in Figure 1 and the used datasets are summarised in Table 3. In this section we first describe the different datasets. Thereafter, we summarise their use and characterise them in terms of formal errors, advantages, and disadvantages.

Summary of used datasets: Dataset Resolution Time period ONS1 ONSA SPT0 VIS0 MAR6 KIR0 GPS a 5 min 2006–2016 √ √ √ √ √ ECMWF b 6 h 2006–2016 √ √ √ √ √ GPS c 5 min 2013–2016 √ √ √ √ √ WVR 15 min 2013–2016 √ √ √ √ √ VLBI 6 h 6–20 May 2014 √
3.1 GPS

We used 11 years of GPS data (2006–2016) from the five Swedish GNSS sites mentioned above. Linear horizontal gradients in the east and the north directions were estimated with a temporal resolution of 5 min. Two GNSS stations are operating continuously at the Onsala Space Observatory, on the west coast of Sweden. The primary station, ONSA, was established already in 1987 and the other station, ONS1, was taken into operation in 2011. The six antenna installations are shown in Figure 2. The antennas of ONSA and ONS1 are located within 100 m from each other and should observe almost identical atmospheric gradients. For the time period 2013–2016 we compare gradients from these two stations with simultaneously estimated gradients using data from a WVR.

The analysis of the GPS data follows the same lines as described by Ning et al. (2013) and is summarised in Table 1. Specifically we mention that each day is analysed independently after adding 3 h of data from the previous day and 3 h from the following day, i.e. in total 30 h. The reason is to avoid discontinuities at midnight in the estimated time series.

Recent work by Kačmarík et al. (2018) compared estimated gradients with those from a numerical weather model using different gradient mapping functions and elevation cutoff angles. They found the best agreement for an elevation cutoff angle equal to 3°. They also showed that the Bar-Sever et al. (1998) gradient mapping function resulted in 17 % smaller gradient amplitudes compared to the Chen and Herring (1997) mapping function. For the 11-year study presented in the next section we use a 10° elevation cutoff angle only, whereas we use several different elevation cutoff angles in the comparison with the WVR data from the Onsala site for a 4-year period.

Based on the five-minute gradients we calculated mean values over 15 min, 6 h, 1 day, and 1 month in order to match the temporal resolution of the comparison data and to study the variability of the wet and the hydrostatic gradients over different time scales.

Examples of the sky coverage of the GPS observations are shown in Figure 3 for the Onsala site. At this latitude there is a significant part of the sky that is never sampled, just north of the zenith direction. It is reasonable to assume that this will have a negative impact on the estimated gradients, and especially in the north direction.
Figure 2. The six antenna installations used to acquire the GPS data. See Figure 1 for their geographical location.
Table 1. Processing of GPS data.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description / Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Processing software</td>
<td>GIPSY v6.2 (Webb and Zumberge, 1993)</td>
</tr>
<tr>
<td>Strategy</td>
<td>Precise Point Positioning (Zumberge et al., 1997) final orbit and clock products were provided by JPL obtained from the legacy GIPSY-OASIS software(^a)</td>
</tr>
<tr>
<td>Reference frame</td>
<td>IGS08</td>
</tr>
<tr>
<td>Mapping functions for ( \Delta L_z )</td>
<td>Vienna 1 2006 (VMF1) (Boehm et al., 2006)(^b)</td>
</tr>
<tr>
<td>Mapping function for ( \Xi )</td>
<td>Bar-Sever et al. (1998)</td>
</tr>
<tr>
<td>Elevation cutoff angle</td>
<td>10(^\circ)</td>
</tr>
<tr>
<td>Zenith delay</td>
<td>Estimated every 5 min, constraint 10 mm/( \sqrt{h} ) (Jarlemark et al., 1998)</td>
</tr>
<tr>
<td>Linear horizontal gradient</td>
<td>Estimated every 5 min, constraint 0.3 mm/( \sqrt{h} ) (Bar-Sever et al., 1998)</td>
</tr>
<tr>
<td>Ocean tide model</td>
<td>FES2004 (Lyard et al., 2006)</td>
</tr>
<tr>
<td>Antenna phase centre</td>
<td>igs08_1740.atx (Schmid et al., 2007)(^d)</td>
</tr>
<tr>
<td>Ambiguity resolution</td>
<td>Yes (Bertiger et al., 2010)</td>
</tr>
<tr>
<td>Ionosphere model</td>
<td>2nd order (IGRF)(^e) (Matteo and Morton, 2011)</td>
</tr>
</tbody>
</table>

\(^a\) For the 11-year dataset, for the 4-year dataset, the products were obtained from a new GipsyX software. We noted that the difference in the products due to the change of software is small (Sibois et al., 2017).

\(^b\) For the 11-year dataset, for the 4-year dataset also the weighted \((\sin(\varepsilon))\) VMF1 and the NMF (Niell, 1996) were used.

\(^c\) For the 11-year dataset, for the 4-year dataset also 3\(^\circ\) and 20\(^\circ\) were used.

\(^d\) For the 11-year dataset, for the 4-year dataset igs08_1869.atx were used.

\(^e\) International Geomagnetic Reference Field

Figure 3. Sky plots of GPS observations from 6 to 12 UT (left) and from 0 to 24 UT (right) on May 12, 2014. This particular day was chosen because results from this day are discussed in Section 5.3. The sky distribution of observations is very similar, although not identical, for all days.
3.2 Microwave radiometer

The microwave radiometer, shown in Figure 4, is designed in order to provide independent estimates of the wet propagation delays for space geodetic applications. It measures the emission from the sky, on and off the water vapour line at 22.2 GHz. Its specifications are summarised in Table 2 and the data processing is carried out as is described for another WVR by Elgered and Jarlemark (1998).

During the time period 2013–2016 the WVR was observing in a sky mapping mode as is illustrated in Figure 5. A disadvantage of a WVR is that the algorithm for calculation of the wet propagation delay fails for data acquired during rain or when large liquid drops are present in the sensed atmosphere. Typically such conditions imply large positive errors in the wet delay, and the water vapour content (Westwater and Guiraud, 1980). Therefore, data taken during rain, or when the estimated equivalent amount of liquid water in the zenith direction is $>0.7$ mm, are discarded from the gradient analysis. In addition there are also time periods when the WVR hardware has failed. The amount of analysed data are shown in Figure 6 as the number of individual observations per day. The first long data gap, in 2014–2015, was caused by a broken mechanical waveguide switch and the second long gap, in 2015–2016, was due to broken cables in the so called cable wrap. The cable wrap was redesigned.

In order to avoid ground-noise pickup the WVR provides observations of the wet delay in the different directions above $20^\circ$. Therefore a simple $\sin(\varepsilon)$ mapping function is used to relate these slant wet delays to the equivalent ZWD. The WVR gradients are estimated based on all observations carried out during a period of 15 min using the method of least squares and the Bar-Sever gradient mapping function. We used the so called a four-parameter model, fitting a zenith wet delay (ZWD), a ZWD rate, and an east and a north linear horizontal gradient to the data (Davis et al., 1993). This means that the estimated gradients are independent of the adjacent successive estimates, which is different from the gradients estimated from the space geodetic techniques, where temporal constraints are applied.
Table 2. Specifications for the Konrad WVR.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Frequencies</td>
<td>20.6 GHz and 31.6 GHz</td>
</tr>
<tr>
<td>Antenna type (one for each channel)</td>
<td>Conical horn with lens</td>
</tr>
<tr>
<td>Antenna beam FWHM(^a), E-plane, ch.1 / ch.2</td>
<td>2.9° / 2.0°</td>
</tr>
<tr>
<td>Antenna beam FWHM(^a), H-plane, ch.1 / ch.2</td>
<td>3.4° / 2.3°</td>
</tr>
<tr>
<td>Reference temperatures (both channels)</td>
<td>313 and 373 K</td>
</tr>
<tr>
<td>System noise temperatures, channel 1 / 2</td>
<td>450 / 550 K</td>
</tr>
<tr>
<td>RF bandwidth (double sideband)</td>
<td>320 MHz (both channels)</td>
</tr>
<tr>
<td>Absolute accuracy (weather dependent due to the quality of tip curves)</td>
<td>1–3 K</td>
</tr>
<tr>
<td>Repeatability</td>
<td>0.1 K</td>
</tr>
</tbody>
</table>

\(^a\) FWHM = Full Width Half Maximum
Figure 5. A measurement cycle of the WVR begins with two azimuth scans. In order to avoid emission from the ground the lowest elevation angle observed is $20^\circ$. Starting in the north, first at an elevation angle of $20^\circ$ clockwise to the north (excluding the azimuth angles of $40^\circ$ and $60^\circ$ due to a nearby radio telescope), and then counterclockwise at an elevation angle of $35^\circ$. Thereafter four tip curves are made over the zenith direction (implying four observations in the zenith direction during each cycle): from the north to the south, from the southwest to the northeast, from the east to the west, and from the northwest to the southeast. The cycle is about 8 min long and is repeated continuously, implying that almost two complete cycles are executed during the time, with a total of the temporal resolution $\approx 100$ observations are used when estimating gradients, i.e. every 15 min.
Figure 6. Number of data points per day observed by the WVR. During days without data loss, e.g. due to rain, each estimated gradient is based on approximately 100 observations in the directions illustrated in Figure 5. Observations close to the sun are removed from the raw data before the data analysis is carried out which causes the seasonal variation in the maximum number of observations per day. During the last year the measurement cycle was optimised by reducing some of the time delays inserted between samples but the observational sequence shown in Figure 5 was used during the whole period.
3.3 Very long baseline interferometry data

We have used the VLBI data from the CONT14 campaign coordinated by the International VLBI Service (Nothnagel et al., 2017). The IVS organises continuous (CONT) VLBI campaigns every third year in order to acquire state-of-the-art VLBI data over a time period of two weeks and to demonstrate the highest accuracy of which the current VLBI system is capable. The primary goal of these CONT campaigns is to support research concerning high resolution Earth rotation (Haas et al., 2017) reference frame stability, and daily to sub-daily site motions, but also other aspects. A concise overview of the IVS CONT campaigns is given by MacMillan (2017).

The CONT14 campaign was observed during May 6–20, 2014. The VLBI data were analysed with the calc/solve VLBI data analysis software (Ma et al., 1990). Station positions, ZWD, atmospheric horizontal gradients, relative clock parameters w.r.t. a reference station, as well as earth rotation parameters were estimated. The relative clock parameters were estimated as a piecewise linear continuous function every hour, with a constraint of \(5 \times 10^{-14}\) s/s between clock rate segments. The ZWD and atmospheric gradients were estimated as piecewise linear continuous functions (i.e. not stochastic processes) with a temporal resolution of 30 min and 6 h, respectively. Constraints for the variability of 15 mm/h for the ZWD rate segments, and 2 mm/day for gradient rates were applied. The NMF (Niell, 1996) mapping functions for ZWD and the Chen and Herring (1997) mapping function for gradients were used in the analysis, together with meteorological information recorded at the VLBI stations. An elevation cutoff angle of \(5^\circ\) was used, and no elevation-dependent weighting.

Figure 7 depicts the sampling of the sky for a 6 h period, which is the highest temporal resolution of the gradient estimates from VLBI, as well as all observations scheduled for a 24 h experiment. This schedule was repeated every day with only minor modifications.

![Figure 7. The directions of the VLBI observations for the time period from 6 to 12 UT (left) and from 0 to 24 UT (right), both on May 12, 2014.](image-url)
Figure 8. The ECMWF gradients for the Onsala (ONSA) site during the 4-year time period studied in Section 5. From the top: hydrostatic gradients every 6 h, their monthly averages, wet gradients every 6 h, and their monthly averages.

3.4 ECMWF data

The Technical University of Vienna provides horizontal hydrostatic and wet gradients based on ECMWF data for many space geodetic sites globally. Figure 1 depicts the five sites used here. Details are given by Boehm and Schuh (2007), so we just mention the characteristics that are most relevant for our comparisons. ECMWF provide profiles of hydrostatic and wet refractivities with a temporal resolution of 6 h, and a spatial resolution of 0.25° (~30 km). The profile closest to the site are used together with one profile to the east and one profile to the north to calculate the refractivity gradient profiles. These are thereafter integrated using Eq. (??) to give the integrated horizontal delay gradients. The data are available during certain time periods from the mid of 2005 and are more continuous from 2006. We decided to use the data from 2006 to 2016, resulting in a time series of 11 years.

As an introduction to the results, presented in the following sections, examples of the ECMWF hydrostatic and wet gradients are illustrated in Figure 8. Worth noting may be that the wet gradients dominate for the temporal resolution of 6 h and vary with the season, whereas the wet and the hydrostatic gradients show similar standard deviations (SD) for the monthly averages.
3.5 Summary of datasets

The results of comparisons between the gradients from these datasets are presented in the next two sections. The usage is defined in Table 3. In Section 4 GPS gradients estimated using the 10° elevation cutoff angle are compared to the ECMWF gradients. The temporal resolution is limited to 6 h in the ECMWF data. On the other hand the time series are 11 years long. The results in Section 5 focus on comparisons of the wet gradients at the Onsala site. Here we have a temporal resolution of 15 minutes when comparing to WVR data and the ECMWF data are only used to subtract the hydrostatic gradients from the total gradients estimated by the GPS and VLBI techniques. In Table 4 we summarise the typical formal errors of the remote sensing techniques. Worth noting is the larger formal error for the north GPS gradient, compared to the east gradient, using the elevation cutoff angle of 20°. Other important comments are that WVR gradients are not estimated during rain events and are not based on observations below 20° elevation angles, but have a more homogeneous sky coverage compared to the GPS and the VLBI observations. Gradients from GPS and WVR have a superior temporal resolution, 5 and 15 min, respectively, compared to the 6 h of the VLBI and the ECMWF gradients.

Table 3. Summary of used datasets.

<table>
<thead>
<tr>
<th>Dataset</th>
<th>Resolution</th>
<th>Time period</th>
<th>ONS1</th>
<th>ONSA</th>
<th>SPT0</th>
<th>VIS0</th>
<th>MAR6</th>
<th>KIR0</th>
</tr>
</thead>
<tbody>
<tr>
<td>GPS a</td>
<td>5 min</td>
<td>2006–2016</td>
<td>√</td>
<td>√</td>
<td>√</td>
<td>√</td>
<td>√</td>
<td>√</td>
</tr>
<tr>
<td>ECMWF b</td>
<td>6 h</td>
<td>2006–2016</td>
<td>√</td>
<td>√</td>
<td>√</td>
<td>√</td>
<td>√</td>
<td>√</td>
</tr>
<tr>
<td>GPS c</td>
<td>5 min</td>
<td>2013–2016</td>
<td>√</td>
<td>√</td>
<td>∼</td>
<td>∼</td>
<td>∼</td>
<td>∼</td>
</tr>
<tr>
<td>WVR</td>
<td>15 min</td>
<td>2013–2016</td>
<td>√</td>
<td>√</td>
<td>∼</td>
<td>∼</td>
<td>∼</td>
<td>∼</td>
</tr>
<tr>
<td>VLBI</td>
<td>6 h</td>
<td>6–20 May 2014</td>
<td>√</td>
<td>√</td>
<td>∼</td>
<td>∼</td>
<td>∼</td>
<td>∼</td>
</tr>
</tbody>
</table>

a The GPS data were processed with elevation cutoff angles equal to 10°.
b (Boehm and Schuh, 2007)
c The GPS data were processed with elevation cutoff angles equal to 3°, 10°, and 20°, different mapping functions, and elevation angle dependent weighting.
Table 4. **Formal errors of the remote sensing techniques**

<table>
<thead>
<tr>
<th>Data</th>
<th>Elev.</th>
<th>Formal error</th>
<th>Gradient</th>
<th>ZWD</th>
</tr>
</thead>
<tbody>
<tr>
<td>set</td>
<td>cutoff</td>
<td></td>
<td>Gradient</td>
<td>ZWD</td>
</tr>
<tr>
<td>angle</td>
<td>East</td>
<td>North</td>
<td>(°)</td>
<td>(mm) (mm) (mm)</td>
</tr>
<tr>
<td>GPS</td>
<td>3</td>
<td>0.14</td>
<td>0.13</td>
<td>1.7</td>
</tr>
<tr>
<td>GPS</td>
<td>10</td>
<td>0.19</td>
<td>0.20</td>
<td>2.3</td>
</tr>
<tr>
<td>GPS</td>
<td>20</td>
<td>0.35</td>
<td>0.43</td>
<td>4.0</td>
</tr>
<tr>
<td>WVR</td>
<td>20</td>
<td>0.04</td>
<td>0.04</td>
<td>0.2</td>
</tr>
<tr>
<td>VLBI</td>
<td>5</td>
<td>0.14</td>
<td>0.13</td>
<td>1.7</td>
</tr>
</tbody>
</table>
4 Comparison of gradients from GPS and ECMWF data 2006–2016

4.1 Seasonal variations of horizontal gradients

We start by investigating the characteristics of the gradients over the year. In Figure 9 we present the monthly mean gradients for the time period 2006–2016 estimated from ECMWF data and GPS data from the Onsala (ONSA) station.

We can clearly see negative north gradients in the winter, with a mean value around $-0.2 \text{ mm}$, both in the GPS and the ECMWF results. When the ECMWF gradients are separated into the hydrostatic and the wet components this variation appears in the hydrostatic component. We interpret this effect as the influence of the Icelandic low pressure system mentioned in Section 2.

Another feature is the winter feature is clearly seen in the analyses of the mean sea level pressure in the ERA-40 Atlas (https://software.ecmwf.int/static/ERA-40_Atlas/docs/section_B/parameter_mslp.html). The results for the other four stations (KIR0, MAR6, SPT0, and VIS0) show similar systematic features. One exception is KIR0, which is at a higher latitude and has a less humid climate. At KIR0 the average monthly wet gradients are much smaller except during the summer months. Furthermore, the influence of the Icelandic low pressure in the winter is not as large as it is at the other four stations. Another exception is seen in the ECMWF wet gradients for ONSA in Figure 9. They are larger in the summer when the wet refractivity is higher, and, at least according to the ECMWF data, this is also seen at the other stations, but at ONSA there is a tendency to of a positive east gradient in the summer. The ONSA GPS station is located a few hundred metres from the coastline, suggesting that the air on the average is more humid over land compared to over the sea.

A possible cause could be the sea breeze that occurs during the summer (Craig et al., 1945; Miller et al., 2003). The issue of wet gradients is studied further using a higher temporal resolution and comparisons with the WVR data in Section 5.2.

The results for the other four stations (KIR0, MAR6, SPT0, and VIS0) show identical systematic features except KIR0, which is at a higher latitude and has a less humid climate. At KIR0 the average monthly wet gradients are insignificant except during the summer months. Furthermore, the influence of the Icelandic low pressure in the winter is not as large as it is at the other four stations.
Figure 9. Monthly means of estimated gradients at the Onsala station for the period 2006–2016. The top graphs show the total gradients from ECMWF (left) and GPS (right). The graphs at the bottom show the ECMWF gradients when separated into the hydrostatic (left) and the wet gradient (right).
Table 5. Correlation coefficients for the total east and north linear horizontal gradients estimated from GPS data and compared to ECMWF data.

<table>
<thead>
<tr>
<th>Station</th>
<th>Six hourly East</th>
<th>Six hourly North</th>
<th>Daily East</th>
<th>Daily North</th>
<th>Monthly East</th>
<th>Monthly North</th>
</tr>
</thead>
<tbody>
<tr>
<td>Kiruna (KIR0)</td>
<td>0.55</td>
<td>0.53</td>
<td>0.76</td>
<td>0.75</td>
<td>0.77</td>
<td>0.82</td>
</tr>
<tr>
<td>Mårtsbo (MAR6)</td>
<td>0.58</td>
<td>0.51</td>
<td>0.75</td>
<td>0.72</td>
<td>0.83</td>
<td>0.80</td>
</tr>
<tr>
<td>Borås (SPT0)</td>
<td>0.58</td>
<td>0.58</td>
<td>0.74</td>
<td>0.74</td>
<td>0.88</td>
<td>0.85</td>
</tr>
<tr>
<td>Visby (VIS0)</td>
<td>0.55</td>
<td>0.56</td>
<td>0.71</td>
<td>0.75</td>
<td>0.84</td>
<td>0.81</td>
</tr>
<tr>
<td>Onsala (ONSA)</td>
<td>0.60</td>
<td>0.60</td>
<td>0.75</td>
<td>0.78</td>
<td>0.90</td>
<td>0.90</td>
</tr>
</tbody>
</table>

4.2 Comparing GPS and ECMWF gradients over different time scales at the five stations

We assess the data quality study the agreement, in terms of correlation coefficients, between the total GPS and ECMWF gradients estimated at the five GPS stations using data from 2006 to 2016. These are shown in Table 5.

The correlations seen in all cases confirm that an atmospheric signal in terms of linear gradients is detected by the GPS observations. We note that the correlation coefficients increase for longer averaging time periods. Our interpretation is that by long term averaging we compare a larger fraction of the gradient that is caused by large scale temperature and pressure gradients, which is better modelled by the ECMWF data. Unfortunately, the temporal resolution of 6 h in the ECMWF data is not sufficient to resolve neither rapid changes in the pressure related to moving weather systems nor many of the short lived small-scale gradients associated with the variability in the water vapour.

Another result worth noting is that the two stations with the highest correlation coefficients, especially for the monthly averages, are ONSA and SPT0. The 95% confidence interval is $+0.03/−0.04$ for the correlation coefficient of 0.90 obtained at station ONSA, based on 131 data points (12 months over 11 years). These two stations are the only ones that are equipped with microwave absorbing material below the antenna and above the metal plate used for the antenna mounting. This could reduce the impact from unwanted multipath effects. The phenomenon calls for further studies.

Assuming that the ECMWF hydrostatic gradients are reasonably accurate we have the possibility to subtract this hydrostatic gradient from the estimated total GPS gradient in order to compare the wet gradients at these five stations. In Table ?? we present the mean values and the standard deviation of these deviations of the gradients, for the three different temporal resolutions, are presented in Tables 6 and 7 from GPS and ECMWF data, respectively. For the 6-hour temporal resolution the GPS gradients estimated at the same time epoch as the ECMWF gradients are compared included in the calculations. The daily and monthly values are averages using all available data these 6-hour data. Comparing the two tables it is clear that the GPS gradients are always larger, but the relative differences between the sites, and for different averaging periods, are similar. We note that the standard deviations (SD) for the wet gradients obtained for the KIR0 station for 6 h and one day are significantly larger than for the other stations.
Table 6. Mean values and standard deviations (SD) over the 11 years of estimated horizontal wet total gradients from GPS data for different temporal resolutions.

<table>
<thead>
<tr>
<th>Station</th>
<th>ZWD&lt;sup&gt;a&lt;/sup&gt;</th>
<th>Horizontal gradient</th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Mean&lt;sup&gt;b&lt;/sup&gt;</td>
<td>Six hourly SD</td>
<td>Daily SD</td>
<td>Monthly SD</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>Mean (mm)</td>
<td>East (mm)</td>
<td>North (mm)</td>
<td>East (mm)</td>
<td>North (mm)</td>
<td>East (mm)</td>
<td>North (mm)</td>
<td>East (mm)</td>
<td>North (mm)</td>
</tr>
<tr>
<td>Kiruna (KIR0)</td>
<td>61 62</td>
<td>−0.20 −0.21</td>
<td>−0.02 −0.14</td>
<td>0.44 0.47</td>
<td>0.23 0.32</td>
<td>0.24 0.31</td>
<td>0.09 0.13</td>
<td>0.09 0.13</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Märtsbo (MAR6)</td>
<td>88 46</td>
<td>−0.22 −0.23</td>
<td>−0.02 −0.13</td>
<td>0.50 0.55</td>
<td>0.30 0.37</td>
<td>0.28 0.36</td>
<td>0.11 0.14</td>
<td>0.11 0.15</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Borås (SPT0)</td>
<td>87 45</td>
<td>−0.06 −0.24</td>
<td>−0.12</td>
<td>0.50 0.56</td>
<td>0.30 0.38</td>
<td>0.30 0.38</td>
<td>0.12 0.16</td>
<td>0.12 0.17</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Visby (VISO)</td>
<td>88 47</td>
<td>−0.06 −0.07</td>
<td>−0.10 −0.23</td>
<td>0.55 0.60</td>
<td>0.32 0.40</td>
<td>0.29 0.37</td>
<td>0.12 0.16</td>
<td>0.09 0.13</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Onsala (ONSA)</td>
<td>92 47</td>
<td>0.01</td>
<td>−0.08 −0.20</td>
<td>0.54 0.59</td>
<td>0.32 0.41</td>
<td>0.30 0.38</td>
<td>0.13 0.18</td>
<td>0.15</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<sup>a</sup> The Zenith Wet Delay (ZWD) is included to illustrate the amount of water vapour in the atmosphere above the station and its SD is based on the 6 h gradients.

<sup>b</sup> The mean gradient values are based on the 6 h gradients.

Table 7. Mean values and standard deviations (SD) over the 11 years of estimated total gradients from ECMWF data for different temporal resolutions.

<table>
<thead>
<tr>
<th>Station</th>
<th>Horizontal gradient</th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Mean&lt;sup&gt;a&lt;/sup&gt;</td>
<td>Six hourly SD</td>
<td>Daily SD</td>
<td>Monthly SD</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Mean (mm)</td>
<td>East (mm)</td>
<td>North (mm)</td>
<td>East (mm)</td>
<td>North (mm)</td>
</tr>
<tr>
<td>Kiruna (KIR0)</td>
<td>0.00 −0.14</td>
<td>0.28 0.26</td>
<td>0.20 0.19</td>
<td>0.07 0.07</td>
<td></td>
</tr>
<tr>
<td>Märtsbo (MAR6)</td>
<td>−0.22 −0.13</td>
<td>0.38 0.34</td>
<td>0.25 0.23</td>
<td>0.08 0.09</td>
<td></td>
</tr>
<tr>
<td>Borås (SPT0)</td>
<td>−0.00 −0.13</td>
<td>0.39 0.35</td>
<td>0.25 0.24</td>
<td>0.09 0.09</td>
<td></td>
</tr>
<tr>
<td>Visby (VISO)</td>
<td>−0.01 −0.14</td>
<td>0.42 0.37</td>
<td>0.26 0.25</td>
<td>0.08 0.08</td>
<td></td>
</tr>
<tr>
<td>Onsala (ONSA)</td>
<td>0.03 −0.14</td>
<td>0.43 0.37</td>
<td>0.27 0.25</td>
<td>0.10 0.09</td>
<td></td>
</tr>
</tbody>
</table>

<sup>a</sup> The mean gradient values are based on the 6 h gradients.

Smaller. This is likely a consequence of the lower humidity at the station. For monthly averages, however, all stations have comparable SD, indicating that at this level the hydrostatic gradient and other effects, e.g. instrumental, become important.

### 4.3 Long term trends
Given that horizontal gradients in general are small and that the larger values typically occur for a short time we expect that any long-term trends would be very small and therefore also difficult to detect because gradients in general are less than 1 mm and large values typically occur over time scales from minutes to a few hours. Examples of time series with a 6-hour and 15-minute temporal resolutions are seen in Figure 8 and in Subsection 5.3, respectively. An estimated gradient has a direction and from the time series we estimate trends for the east and the north gradients. Combining the east and north gradients offers the possibility to also search for trends in the total amplitude value amplitude of the gradient \( \sqrt{\Xi_e^2 + \Xi_n^2} \) at the station. A positive There can be a trend in the total amplitude can also occur if there is an increase in the variability at the station, which can happen amplitude, see Equation (2), even if there is no trend neither in the east nor in the north gradient. For these five stations we have estimated linear gradients in the east components. The amplitude is by definition never negative. A trend of larger east gradients can be balanced by a similar trend in larger west gradients, resulting in no net trend in the east gradient component, but a trend in the gradient amplitude. Table 8 presents the estimated gradient trends for the east and the north direction as well as for the total gradient directions and for the amplitudes over the 11 years. The trends we estimate and present the total gradient trends from GPS data. Wet gradient trends inferred from GPS can be calculated by subtracting the ECMWF hydrostatic gradients. These trends are indeed very small, typically well below 0.01 mm 10 µm/year. The highest value is –0.02 mm 19 µm/year for the wet total gradient in the north direction at the SPT0 station. If this trend originates from the atmosphere it is a local effect, because it is 65 times as large as the wet total north gradient trend at the nearby ONSA station. However, it is not seen in the ECMWF data which indicates that it is an instrumental effect related to the GPS station.

A typical formal 1-sigma uncertainty of 0.01 mm 3 µm/year is obtained if we assume that the deviations from the model is white noise, but 0.04 mm 40 µm/year is estimated by taking the short term temporal correlation of the deviations into account using the model presented by Nilsson and Elgered (2008). In addition to that the estimated trends are small relative to their uncertainties we cannot assume perfectly stable hardware at the station. For example, hardware problems giving a large impact on the estimated gradients have been reported by Douša et al. (2017). Given these circumstances it seems unlikely to detect any trends in gradients caused by the atmosphere unless there is a dramatic local effect of the weather conditions at the site.
Table 8. Gradient trends: 2006–2016. All values are in the unit μm/year.

<table>
<thead>
<tr>
<th>Station</th>
<th>ECMWF trends</th>
<th>GPS trends</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Hydrostatic</td>
<td>Wet</td>
</tr>
<tr>
<td>KIR0</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>MAR6</td>
<td>1</td>
<td>−1</td>
</tr>
<tr>
<td>SPT0</td>
<td>1</td>
<td>−2</td>
</tr>
<tr>
<td>VIS0</td>
<td>1</td>
<td>−1</td>
</tr>
<tr>
<td>ONSA</td>
<td>1</td>
<td>−1</td>
</tr>
</tbody>
</table>
Gradients

5.1 Wet-gradients from GPS and WVR

For the Onsala site we have will study total gradients from the two GPS stations, hydrostatic and wet gradients from ECMWF, and one VLBI station and wet gradients from the WVR for the time period 2013–2016. We will use the hydrostatic gradients from ECMWF to calculate wet gradients from GPS and VLBI total gradients. The designs of the two GPS stations are different, see Figure 2, which motivates to include both of them in the comparisons. Three different studies are made using these data: (1) assessment of the impact of using different processing of the GPS data, primarily varying the elevation cutoff angle, by comparison to the WVR gradients; (2) using the GPS gradients from the processing variant showing the best agreement with the WVR gradients, the seasonal variations in the wet gradient are characterised; and (3) a 15-day long period with VLBI data is used as a case study for comparisons with GPS and WVR wet gradients and the ZWD.

5.1 Test of GPS processing variants relative to WVR data

Gradients in the east and the north directions are estimated from the GPS data for five different solutions. We use three different elevation cutoff angles for the VMF1 zenith delay mapping functions. One additional solution is carried out with elevation dependent weighting \( \sin(\varepsilon) \) and in the fifth solution the VMF1 mapping functions are replaced by the NMF. As stated earlier the gradient mapping function presented by Bar-Sever et al. (1998) is used in all cases.

When we use the independent WVR data to assess the quality of the wet gradients together with the total gradients estimated for ONSA and ONS1, the hydrostatic gradients from ECMWF (see Figure 8), linearly interpolated to match the time epochs of the GPS gradients, are subtracted from the estimated total GPS gradients. Thereafter we form 15 min averages for the east and the north wet gradients from GPS and compare to the corresponding WVR results. An overview of the data is presented in Figure 10 in terms of monthly means of total gradient size and ZWD. The GPS solution is the one with a 3 elevation cutoff angle, no weighting, and the VMF1 mapping functions. Here we note that the WVR gives much larger gradients. This depends mainly on that no constraints are applied in the WVR data analysis. The WVR gradients for one 15-minute period do not depend on earlier or later estimates. The WVR is also less of an all weather instrument, being sensitive to liquid water in the sensed atmosphere. This is likely the cause for positive systematic errors in the ZWD as well as occasional overestimates of gradient amplitudes. In this context the 17 \% difference in gradient amplitude depending on mapping function used reported by Kačmářík et al. (2018) is less critical. The uncertainty of the estimated gradient amplitude, to which the assumption of a linear model for the atmosphere is also contributing, is significantly larger.

Time series of monthly means of wet total gradients, \( \sqrt{\varepsilon_{e,wet}^2 + \varepsilon_{n,wet}^2} \), (top) and ZWD (bottom) from GPS and WVR. When forming monthly means the correlation coefficients become high. The total wet gradients: WVR vs. ONSA/ONS1 are both 0.85 and ONSA-ONS1 is 0.99. For the ZWD: WVR vs. ONSA/ONS1 are both 0.97 and ONSA-ONS1 is 0.999. When correlating the wet total gradients with the ZWD we obtain 0.95 for the WVR, 0.93 for ONSA and 0.92 for ONS1.

The results for the different GPS solutions are summarised in Tables 9 and 10. Because of the different gradient amplitudes from the WVR and GPS, we present mean values and SD of the differences as well as correlations coefficients. Table 9 shows
the results when the total gradients from the stations ONSA and ONS1 are compared to each other. Table 10 shows the results when the wet gradients from ONSA and ONS1 are compared to the WVR gradients. We note that in both tables the best agreement between the gradients estimated is obtained for an elevation cutoff angle equal to 3°. The 95% confidence interval for correlation coefficients around 0.65 and approximately 80,000 data pairs is ±0.004. This confirms the results presented by Kačmarák et al. (2018) using a GNSS station network in central Europe. This result was not expected by us, given that the WVR has an elevation cutoff angle of 20° (in order to avoid ground-noise pickup) the GPS solution using the same cutoff angle would show a better agreement. One interpretation of this result Our interpretation is that for the temporal resolutions of 5–15 min the low elevation observations are important in order to distinguish the gradient parameters relative to other estimated parameters in the GPS analysis. A higher elevation cutoff angle will remove many observations towards the north, and especially for a cutoff angle of 20°, see Figure 3 and Table 4 with the formal errors.

The solution giving the best agreement, when comparing gradients from ONSA and ONS1 data with each other, is the one with elevation dependent weighting, whereas the comparisons with the WVR, for both ONSA and ONS1, give the best agreement without weighting. The choice of elevation cutoff angle is a compromise between having a good geometry and avoiding effects of signal multipath. Our interpretation is that the gradients from ONSA and ONS1 are estimated based on very similar observational directions and have common error sources, such as orbit errors, resulting in correlations around 0.9. In order to increase an already high correlation the observations at the lowest elevation angles are not that important, since multipath effects will be more and more different the closer to the horizon the observations are made. When ONSA and ONS1 gradients are compared to those from the WVR the situation is different, because these gradients are independent and the geometry of the GPS observations becomes more important in order to estimate a more accurate gradient. Although we note that the correlation is here reduced to around 0.6. Since the WVR provides independent gradients, we will in the following focus on the VMF 3° solution without elevation dependent weighting.
**Table 9.** Assessment of the different GPS solutions comparing total gradients from the two GPS stations ONSA and ONS1.

<table>
<thead>
<tr>
<th>GPS Solution</th>
<th>Difference&lt;sup&gt;a&lt;/sup&gt;</th>
<th>Standard Deviation</th>
<th>Correlation Coefficient</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>East (mm)</td>
<td>North (mm)</td>
<td>East (mm)</td>
</tr>
<tr>
<td>VMF 3°</td>
<td>−0.01</td>
<td>0.03</td>
<td>0.22</td>
</tr>
<tr>
<td>VMF 3°&lt;sup&gt;b&lt;/sup&gt;</td>
<td>0.03</td>
<td>0.02</td>
<td>0.15</td>
</tr>
<tr>
<td>NMF 3°</td>
<td>−0.01</td>
<td>0.05</td>
<td>0.23</td>
</tr>
<tr>
<td>VMF 10°</td>
<td>0.02</td>
<td>0.04</td>
<td>0.25</td>
</tr>
<tr>
<td>VMF 20°</td>
<td>0.33</td>
<td>0.36</td>
<td>0.39</td>
</tr>
</tbody>
</table>

<sup>a</sup> The mean difference is ONS1 − ONSA.

<sup>b</sup> Elevation dependent weighting, \( \sin(\varepsilon) \)

**Table 10.** Assessment of the different GPS solutions for the wet gradients from the two GPS stations ONSA and ONS1 relative to the WVR data.

<table>
<thead>
<tr>
<th>GPS Solution</th>
<th>Difference&lt;sup&gt;a&lt;/sup&gt;</th>
<th>Standard Deviation</th>
<th>Correlation Coefficient</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>East (mm)</td>
<td>North (mm)</td>
<td>East (mm)</td>
</tr>
<tr>
<td>ONSA</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>VMF 3°</td>
<td>0.23</td>
<td>−0.07</td>
<td>0.64</td>
</tr>
<tr>
<td>VMF 3°&lt;sup&gt;b&lt;/sup&gt;</td>
<td>0.21</td>
<td>−0.06</td>
<td>0.71</td>
</tr>
<tr>
<td>NMF 3°</td>
<td>0.22</td>
<td>−0.07</td>
<td>0.64</td>
</tr>
<tr>
<td>VMF 10°</td>
<td>0.20</td>
<td>−0.10</td>
<td>0.65</td>
</tr>
<tr>
<td>VMF 20°</td>
<td>−0.02</td>
<td>−0.28</td>
<td>0.75</td>
</tr>
</tbody>
</table>

| ONS1         |           |           |           |           |           |           |
| VMF 3°       | 0.22      | −0.04    | 0.64     | 0.58     | 0.68     | 0.64      |
| VMF 3°<sup>b</sup> | 0.24     | −0.02    | 0.71     | 0.63     | 0.58     | 0.55      |
| NMF 3°       | 0.21      | −0.02    | 0.64     | 0.58     | 0.68     | 0.63      |
| VMF 10°      | 0.22      | −0.04    | 0.66     | 0.59     | 0.66     | 0.62      |
| VMF 20°      | 0.36      | 0.15     | 0.79     | 0.73     | 0.49     | 0.42      |

<sup>a</sup> The mean difference is the offset referenced to the corresponding WVR time series.

<sup>b</sup> Elevation dependent weighting, \( \sin(\varepsilon) \)
Table 11. The impact of the elevation cutoff angle on the estimated GPS gradient amplitude

<table>
<thead>
<tr>
<th>Elev. cutoff angle (°)</th>
<th>Mean value of gradient amplitudes (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>~3°</td>
<td>0.51 0.50</td>
</tr>
<tr>
<td>~10°</td>
<td>0.58 0.59</td>
</tr>
<tr>
<td>~20°</td>
<td>0.75 0.70</td>
</tr>
</tbody>
</table>

5.2 Wet gradients from GPS and WVR

An overview of the data in terms of monthly means of the wet gradient amplitude and the ZWD is presented in Figure 10. The GPS solution with a 3° elevation cutoff angle, no weighting, and the VMF1 mapping functions are used. When forming monthly means the correlations are obvious, both between GPS and WVR estimates, and between the variability, in terms of the SD, and the gradient amplitudes and the ZWD. Here we also note that the WVR gives much larger gradients. Factors that can cause a difference in gradient amplitude are:

1. The WVR is sensitive to liquid water in the atmosphere. This is a cause for positive systematic errors in the ZWD as well as occasional overestimates of gradient amplitudes. We investigated this possibility by deleting all WVR observations implying a liquid water content larger than 0.3 mm. The impact was however insignificant. The average gradient amplitude decreased by 0.01 mm. The reason being that large liquid contents are rather infrequent, given that already data acquired during rain have been removed.

2. The WVR gradients for one 15-minute period do not depend on earlier or later estimates whereas the GPS gradients are estimated using constraints on the variability.

3. The fact that the WVR and the GPS gradients are averaged over different air masses also affect the estimated amplitude. The WVR did not observe at elevation angles below 20° due to the risk of picking up emission from the ground. However, this averaging effect can be seen in the estimated gradient amplitudes using the different elevation cutoff angles in the GPS solutions presented in Subsection 5.1. Table 11 summarise these results for ONSA and ONS1 for each year.

We conclude that the latter two issues are the likely explanation for the differences in gradient amplitudes estimated from GPS and WVR data.

Before studying the correlation between the GPS and the WVR gradients it is appropriate to study how well the gradients from the two GPS stations agree. A correlation plot for the total gradients from the VMF1 solution with a 3° elevation cutoff angle is shown in Figure 11. As in the previous section we see a slightly higher correlation for the east gradients, possibly
Figure 10. Time series of (a) monthly means of wet gradient amplitudes $\sqrt{\xi_{e,wet}^2 + \xi_{n,wet}^2}$, (b) their SD, (c) monthly means of the ZWD, and (d) the ZWD SD from GPS and WVR. The green stars denote WVR data. The ONSA and ONS1 data are denoted by red circles and black squares, respectively.
because of the poorer sampling on the sky north of the zenith direction due to the geometry of the GPS satellite constellation at this latitude (see Figure 3).

The two GPS stations share several error sources, such as clock and orbit errors of the observed satellites, and the use of the same mapping functions, meaning that the rather high correlation is overoptimistic due to a common mode suppression of errors.

**Figure 11.** Correlations between estimated total gradients from the GPS stations ONSA and ONS1 using all data with a 5 min resolution from the period 2013–2016.

Correlation plots for the wet gradients from ONSA, ONS1, and the WVR are presented in Figure 12. As expected, the correlations between the estimated gradients from the two GPS stations are significantly higher compared to when the GPS gradients are correlated with the gradients from the WVR. It is also not surprising that the correlation between the wet gradients from ONSA and ONS1 are slightly lower compared to the correlation between the total gradients (Figure 11). When subtracting the hydrostatic gradients, a common signal is removed and the dynamic range is reduced, which affects the correlation coefficients. There are several reasons why the correlation coefficients with the WVR are lower: the reasons for the lower correlation coefficients between the WVR and the GPS gradients are almost identical with the reasons above why the WVR gradient amplitudes are higher: (1) they do not have common sources of errors; (2) the WVR data suffer both from white noise and algorithm errors, especially when liquid water is present; (3) the WVR data for each 15-minute period are independent of the adjacent successive periods, whereas there are temporal constraints on the gradients estimated from the GPS data; (4) the sampling on the sky agrees also much better between the two GPS stations, assuming that in general the directions of the observations are towards the same satellites, whereas the WVR observations are evenly spread over the sky and above an elevation angle of 20°.

Concerning the sampling of the atmosphere, the use of a multi-GNSS constellation has been shown to improve the agreement between GNSS gradients with those estimated from a WVR (Li et al., 2015). In this context it should be noted that with many
more GNSS observations the optimum elevation cutoff angle may not be as low as 3° because of an improved sampling of the atmosphere.

**Figure 12.** Correlations between estimated wet gradients from the WVR, ONSA and ONS1 using all data from the period 2013–2016. The data in the graphs with ONSA and ONS1 (left) have the original 5 min resolution, whereas the GPS data are averaged over 15 min when compared to the WVR data (middle and right). Note the different scale on the axes for the graphs with WVR data. The correlation coefficients obtained when the east gradients from the WVR were correlated with the original total gradients from GPS were 0.633 for ONSA and 0.637 for ONS1. The corresponding values for the north gradients were 0.575 for WVR-ONSA and 0.571 for WVR-ONS1. This supports our assumption that the ECMWF hydrostatic gradients are reasonably accurate when carrying out a linear interpolation between the 6-hour samples.

We investigated if an average of the wet gradients from both GPS stations, ONSA and ONS1, estimated at the same time epoch, will improve the agreement with the WVR. We see an overall small improvement. For the east gradient the individual correlation coefficients were improved from 0.678 (ONSA) and 0.682 (ONS1) to 0.698. The corresponding values for the north gradient were increased from 0.639 (ONSA) and 0.635 (ONS1) to 0.666. Our interpretation is that by averaging the GPS gradients from ONSA and ONS1 the stochastic noise is reduced.

Correlation plots are shown in Figure 13 for each month of the four years. A clear seasonal dependence is seen, because the variability in the wet refractivity is larger during the warmer time periods, resulting in larger gradients and a larger dynamic range. In We note that during October 2014 there were problems with the WVR (see Figure 6). During most of the days there is a significant data loss, likely due to rain, which could be the reason for the low correlation during this month. The other months with low correlations are March 2015 for both the east and the north component, and January and February 2016 for the north component. In all these cases there were no large gradients detected and this has an impact on the correlations. In Figure 8 of Lu et al. (2016) a correlation coefficient of 0.52 was reported for the months March–May, 2014, between GPS and
WVR gradients. Here we show that the variability from month to month is large and therefore the choice of the time period for gradient comparison studies is a critical issue.

Comparing the results obtained for ONSA with those from ONS1 they are almost identical (in both Figures 12 and 13) meaning that in this case there is no obvious improvement from the absorbing material below the antenna on ONSA. This is different to the previous finding where ONSA and SPT0, with microwave absorbing material, showed a better agreement with ECMWF gradients compared to the KIR0, MAR6, and VIS0 stations. Our assumption is that the lack of a concrete pillar with a metal mounting plate just below the antenna on ONS1, or any other objects affecting the electromagnetic environment at the antenna, eliminates the need for an absorber (see Figure 2).

Figure 13. Correlations between estimated wet gradients from the WVR data and the GPS data from ONSA (solid lines) and ONS1 (dotted lines) averaged over 15 min when the hydrostatic gradients have been removed from the total GPS gradients for each month of the four years. The east gradients are presented with red lines and the north gradients with blue lines. We note that during October 2014 there were problems with the WVR (see Figure 6). During most of the days there is a significant data loss, likely due to rain, which could be the reason for the low correlation during this month.
5.3 GPS, VLBI, and WVR wet gradients during CONT14

The total wet gradients from the two space geodetic techniques GPS and VLBI were compared to each other and to the WVR during the CONT14 campaign. The GPS gradients were those obtained from the VMF1 solution, unweighted, with a 3° elevation cutoff angle. Observations from several earlier CONT campaigns have been analysed in terms of gradients with different results depending on the station and the time of the campaign (Teke et al., 2013). The estimated time series are shown in Figure 15. The addition of the ECMWF data, see Figure 14, is only used to subtract the hydrostatic gradients from ECMWF to the WVR wet gradients did not add any significant variability to the WVR gradients, see Figure 14 the total gradients estimated by VLBI and GPS. The time series are shown in Figure 15.

![Figure 14](image)

Figure 14. Time series of ECMWF hydrostatic and wet gradients during the CONT14 campaign.

Again we note that the size of the WVR gradients is larger compared to all other instruments. The VLBI gradients correlate with the gradients from the other instruments but their amplitudes are smaller. Given that the sampling of the atmosphere is much more sparse with the VLBI telescope, a short lived gradient in combination with the assumption of linear functions in 6-hour segments, will probably reduce the variability in the estimated amplitude.

Time series of estimated total gradients during the VLBI CONT14 campaign 6–20 May (days 126–140). The temporal resolution is 6 h for the VLBI gradients (blue circles connect with a solid line), 5 min for the GPS gradients for ONSA (red...
Figure 15. The wet gradients and the ZWD during the VLBI CONT14 campaign 6–20 May (days 126–140). The temporal resolution for the VLBI (blue circles) gradients is 6 h and the ZWD 30 min, 5 min for the GPS gradients for ONSA (red dots) and ONS1 (black dots), and 15 min for the WVR (green plus). Also included are the ECMWF total gradients with a 6 h resolution (cyan squares).
Table 12. Comparison of estimated linear wet gradients from VLBI relative to GPS and WVR data.

<table>
<thead>
<tr>
<th>Reference</th>
<th>Mean Difference(^a) (mm)</th>
<th>Standard Deviation (mm)</th>
<th>Correlation Coefficient</th>
</tr>
</thead>
<tbody>
<tr>
<td>Instrument</td>
<td>Instrument</td>
<td>Instrument</td>
<td>Instrument</td>
</tr>
<tr>
<td>East</td>
<td>North</td>
<td>East</td>
<td>North</td>
</tr>
<tr>
<td>ONSA</td>
<td>0.01</td>
<td>-0.03</td>
<td>0.22</td>
</tr>
<tr>
<td>ONS1</td>
<td>0.03</td>
<td>-0.08</td>
<td>0.22</td>
</tr>
<tr>
<td>WVR</td>
<td>0.23</td>
<td>0.30</td>
<td>-0.17</td>
</tr>
</tbody>
</table>

\(^a\) The mean difference is VLBI—reference instrument.

Time series of ECMWF hydrostatic and wet gradients during the CONT14 campaign.

Table 12 summarises the correlation coefficients for the east and the north VLBI wet gradients compared to those from the two GPS stations, ONSA and ONS1, and the WVR. Here we have correlated averages using data ±3 h around the VLBI gradient value every 6 h. In order to be consistent also the interpolated data from continuous VLBI segments are averaged in this way.

Again we note that the agreement, in terms of correlation coefficients, is better for the east component. The correlation coefficients are lower for the north component for all three comparisons, whereas the SDs are similar. The reason is that the size of the east gradients are larger compared to the north component. There is a specific example seen in Figure 15 during day 132 (May 12) where a large north gradient is not detected in the VLBI data. The independent wet gradients obtained from the WVR (plus the ECMWF hydrostatic gradient) confirm that this gradient was originating from the atmosphere. The left plot in Figure 7 may explain why the north gradient has a larger uncertainty at this specific time. Scatter plots (not shown) confirm what is indicated by the SDs, that the quality of the east and north components is similar.

We attribute the lower correlation coefficients obtained between VLBI-GPS and VLBI-WVR using 6 h averages during the CONT14 campaign compared to GPS-WVR 15 min averages for the month of May 2014 in Figure 13 to the sparse sequential sampling of the sky by the VLBI observations. On the other hand, averaging the WVR gradients over ±3 h reduces some of the noise seen in the 15 min values. The future use of the twin telescopes with faster slewing speeds at the site is likely to improve this situation. During CONT14 there were approximately 360 useful observations at Onsala per day. We expect this to increase by a factor of 6–7 when using the new VLBI Geodetic Observing System (VGOS) (Niell et al., 2018), which means that the use of twin telescopes could result in 200 observations per hour. This in turn makes it possible to improve the temporal resolution of the estimated atmospheric gradients.

Finally, we like to use this 15-day long time series for a discussion on gradient variability. Figure ?? shows the ZWD from the two GPS stations and the WVR. At the end of day 135, see the ZWD plot in Figure 15, more humid air is starting to enter over the site. We note a sudden short decrease, followed by a rapid increase. In Figure 16 we zoom in on the gradients and the
ZWD during this period. Here we have an example where wet gradients from GPS and WVR gradients occur when different air masses pass over the site. We believe that this when a warm front passage occurs in the evening of day 135. During this passage there is also a smaller drier air mass present causing a decrease followed by an increase in the ZWD. During this dip in ZWD the wind at the ground was from the west increasing from 7 m/s at 18 UT to 11 m/s at 24 UT. During the decrease in ZWD we see a clear positive east gradient and during the following increase in ZWD the east gradient has a negative peak. Also during the first few hours of day 136 a decrease in the ZWD corresponds to positive values for the east gradient, and the wind continued to come from the west. This is as expected, but there are also variations in the north gradient during this period, consistently detected by the WVR and the GPS data, showing that the wind at the ground was not fully representative for all altitudes. This example illustrates a situation where GPS/GNSS data in the future can be used to evaluate high resolution numerical weather models.

The zenith wet delay (ZWD) from ONSA (red dots), ONS1 (black dots), and WVR (green plus) during the CONT14 campaign.

Figure 16. Zoom in on the time series with gradients in Figure 15 and ZWD in Figure ?? The symbols are as before: VLBI gradients (blue circles connect with a solid line), GPS gradients for ONSA (red dots) and ONS1 (black dots), and WVR wet plus the ECMWF hydrostatic gradients (green plus), ECMWF total gradients with a 6 h resolution (cyan squares).
6 Conclusions

We have shown that estimated linear horizontal gradients from GPS data from five sites in Sweden can be understood based on meteorological phenomena. Averaging gradients in the east and the north direction over one month gives correlation coefficients of up to 0.9 when compared to gradients calculated from meteorological analyses of the ECMWF. Monthly averages of the gradients are dominated by the hydrostatic component.

No significant long-term trends were detected for the horizontal gradients. If small gradient trends are detected in the future we recommend to critically assess if they could be caused by station problems or confirmed by a nearby (or even collocated) station.

When studying gradients averaged over shorter time scales, e.g. 15 min, we find the wet component of the gradients to cause most of the variability. We confirm the result from Kačmářík et al. (2018), that an elevation cutoff angle of 3° implies a better agreement when comparing GPS gradients with those from a WVR, in spite of the fact that the WVR does not observe the atmosphere below elevation angles of 20°. Related to this is that by using a 3° elevation cutoff angle in the GPS processing will decrease the amplitude of the GPS gradients by approximately 20 % compared to a 20° cutoff angle. We interpret this result as the averaging of a larger air mass results in a similar decrease in gradient amplitudes as the averaging of gradients over longer time periods.

Correlation coefficients between wet gradients simultaneously estimated from GPS and the WVR data can for specific months reach up to 0.8. Based on the four years of results we note a strong seasonal dependence, from 0.3 during months with smaller gradients to 0.8 during months with larger gradients, typically during the warmer, and more humid, part of the year. Related to this we suggest further studies of large wet gradients estimated from GPS in combination with meteorological high-resolution models, both for evaluation of the performance of the model and for verification of the quality of the gradients.

In general we also note slightly higher correlation coefficients for the GPS derived gradients in the east compared to the north direction. We interpret this difference to be caused by an inhomogeneous spatial sampling on the sky, which is important when we assume that the model describing linear horizontal gradients has deficiencies. The different sampling on the sky is an important issue for any comparison between different techniques. This question remains unresolved and would have to be studied later.

Additional issues that deserve attention in future studies, in addition to similar studies in very different climates, e.g. the tropics, can include multi-GNSS observations. At latitudes similar to those in this study, the use of GNSS satellites with a higher orbit inclination will reduce the part of the sky not sampled by GPS.

For VLBI the use of VGOS (twin) telescopes will also dramatically improve the sampling of the atmosphere. When WVR data are used to evaluate gradients from the space geodetic techniques one may consider to also apply different constraints for the temporal variability of these estimates.
**Data availability.** The input GNSS data, in RINEX format, are available from EUREF, https://igs.bkg.bund.de/dataandproducts/browse. The input VLBI data are available from the IVS, ftp://ivs.bkg.bund.de/pub/vlbi/ivsdata/db/2014/. The ECMWF gradients are accessible from the Technical University of Vienna, http://vmf.geo.tuwien.ac.at/trop_products/GNSS/LHG/. The estimated gradients from GPS, VLBI, and WVR data have been registered and archived by the Swedish National Data Service (SND): doi:10.5878/nswt-yr39.

**Author contributions.** Gunnar Elgered coordinated and wrote the major part of the manuscript and together with Tong Ning planned the different GNSS data analyses during the COST Action ES1206. Tong Ning performed the GNSS data analyses, resulting in the estimated gradients. Peter Forkman and Rüdiger Haas carried out the same task for WVR and VLBI data, respectively. All authors contributed in the writing process, in particular to the sections presenting the results produced by each author and approved the entire manuscript before the submission.

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