1 Response to Reviewer 1

We thank both reviewers for their comments and suggestions. We know this paper is technical work and requires valuable time for such reviews. We think text added to the manuscript as a response to reviewers has made improvements and helped clarify assumptions and interpretation.

**Review1 comment1:** See 2.4 -> did you account for the averaging kernel in calculating xco2? Im not sure how this varies geographically, but it may impose a different latitude gradient in xco2 than inferred from a simple pressure weighting.

Authors Response R1C1: We made the assumption that averaging kernel had a negligible effect on extracted seasonal cycles. No, we did not apply the GOSAT averaging kernel to our simulated XCO2 calculations. It is true that the averaging kernel can affect point-to-point comparisons (Wunch et al. 2011). By most accounts, the difference in XCO2 seasonal cycles forced by different DGVMs is quite large (magnitude and amplitude errors >> 1 ppm, and phase errors on order of weeks). By comparison, the effect of an averaging kernel on extracted seasonal cycles is on the order of 0.5 ppm (Lindqvist et al. 2015). Fig. 4: doi:10.1186/s40562-017-0074-7. Clarifying text was added as below to the method section 2.1 Satellite XCO2 data. Authors changes to text R1C1: A note that satellite data have uncertainties of their own based on instrument noise, version of retrieval algorithm used to filter atmospheric effects, and averaging kernels (Yoshida et al. 2011, Lindqvist et al. 2015). We made the assumption that averaging kernel has a minimal effect on extracted seasonal cycles and we did not apply averaging kernels to the simulation data in this study. A full quantification of uncertainty in satellite-derived seasonal cycles is beyond the scope of this study, but such an analysis could be useful for benchmarking purposes as models continue to reduce large biases (>> 1.0 ppm). Nevertheless, we make the assumption that lower biases are generally indicative of better model performance.

**Review1 comment2:** See 2.6.1 -> might be helpful to provide an example of time series with local minima/maxima and show how the algorithm differentiates these from seasonal mean values.

Authors Response R1C2: We provide demonstrations of the algorithm performance in the associated computer code for the algorithm, which is also heavily annotated. We added clarifying text as below in the section 2.6 Technical Description., to orient the reader to the additional resources.

Authors changes to text R1C2: The computer code is annotated and provides data used in this study with demonstrations for applying the algorithm to remove local minima or maxima, and the categorization of seasonal cycle segments.

**Review1 comment3:** See 2.7 -> Im confused about the method to estimate the latitude gradient using the average latitude of each TransCom region. Why not use the entire zonal average for each latitude band?

Authors Response R1C3: The seasonal cycle metrics from the land regions were sufficient to extract the relevant patterns for each latitude for addressing our main objectives. The main aim of our study is to evaluate the quality of terrestrial biosphere model (LPJ DGVM) simulations. Although the ocean fluxes also have seasonal variability but that can be considered a minor contributor to the XCO2 seasonal cycle, relative to the flux seasonal of land biosphere.

**Review1 comment4:** See 3.1, L290 -> the problem with using predefined transcom regions is the lack of coverage in critical sub-regions. I understand removing these regions from the analysis, but it seems archaic at this point to still use these regions. I will also point out that Eurasia Boreal has similar reduced coverage as NA Boreal (Fig S2), so its odd that only the former region is analyzed.

Authors Response R1C4: Yes, this is a good point. We do mention this is a caveat in the first paragraph of the discussion (section 3.1 Satellite coverage...). We had done a simple analysis using simulated XCO2 to assess the effect of data missing from sub-regions (Figure S5, in Supplement). In a few of the regions (i.e., Asia Tropical, Southern America Temperate) there were noticeable differences in seasonal cycles using co-location versus using all simulated data (so thining). Analysis on smaller sub-regions would be useful, yes. We think this analysis is a good first step for comparing the DGVMs. So much of this type of analysis, and attribution of errors or fluxes to XCO2, is still related to the convolution fluxes in the near and far fields. Analysis on smaller regions does not help us much in identifying general patterns if we don't know the contributing field.
Review comment 5: L316-318 -> this whole sentence is very confusing. Amplitude increases with latitude

Authors Response R1C5: Agreed, we simplified the sentence as suggested.

Authors changes to text R1C5: Seasonal amplitude varied predictably with latitude (Fig. 4).

Review comment 6: L318 -> Why is a range (0.74-0.77 ppm) for latitude slope reported? Convention is to report slope +/- uncertainty (e.g., 0.75 +/- 0.05 ppm). If referring to the upper and lower bounds due to errors in the slope, please specify.

Authors Response R1C6: We understand the confusion. We updated the text to include slope estimate with uncertainty as mean +/- SE.

Authors changes to text R1C6: There was an increase in amplitude of 0.74 +/- 0.13 ppm (mean +/- S.E.) for Rise Segments and 0.77 +/- 0.13 ppm for Fall Segments for every 10 degrees of latitude for GOSAT.

Review comment 7: Fig 4 -> The CO2amp and Period values in the figure dont make sense. Also why are there no points from 20-40N and between 40-50N? There is plenty of coverage according to Fig S2. I wonder if using zonal averaged to compute these altitude gradients would reduce this clumpiness.

Authors Response R1C7: We are not clear on why the CO2amp and Period values in Figure 4 do not make sense, could you clarify? The lack of data points in the latitudinal bands you suggest are because we used seasonal cycles from the transcon regions, taking the average latitude of the transcon region as the latitude for the analysis, plotted on the x-axes of Figure 4. This is the reason for the groupings of the data points.

Review comment 8: L321 -> It doesnt make sense to report a mean slope value (1.25 ppm / 10 deg lat) for a log-linear slope. Maybe just report the value for a certain latitude range (i.e., 30-40N)

Authors Response R1C8: Good point, this was overlooked. We updated accordingly and reported that the log-linear slope indicates larger gradients at higher than at lower latitudes. We then also reported the latitudinal range in amplitudes between Equator and 70N for comparison between surface samples and XCO2.

Authors changes to text R1C8: Whereas the XCO2 amplitudes exhibited a linear relationship with latitude, in-situ flask samples of CO2 exhibited a log-linear relationship with latitude (Fig. 5: R2 = 0.90, d.f.=45, p < 0.001), which indicates larger amplitude gradients at higher than at lower latitudes. The difference results in a latitudinal range (Equator to 70N) in seasonal amplitude of ~ 7 ppm for XCO2 (taken as 70 * [0.077 + 1.95*0.013], as the largest possible amplitude gradient in XCO2; u + 1.95*S.E.) and ~ 17 ppm for surface CO2. The dampened gradient in XCO2 amplitude suggests substantial north-south atmospheric mixing...

Review comment 9: L322-323 -> over what latitude range?

Authors Response R1C9: We specified that the latitudinal range in seasonal amplitude was compared between amplitude at the Equator and 70N for surface in-situ CO2 and XCO2 data. Text amended as in previous response R1C8.

Review comment 10: Sec 3.2 -> Why didnt you compare in situ observations to models?

Authors Response R1C10: Although in-situ comparisons also have their value (Peng et al. 2015 in GBC), we were more interested in model abilities to reproduce larger scale patterns than at point-level

Review comment 11: L 348 -> Should mention somewhere that phases are equal at 2N. The switch in asymmetry in northern latitudes, specifically the rapid spring and slow fall transition at high northern latitudes, is consistent with findings in Parazoo et al (2016), who suggest that poleward transport of southern signals, which experience earlier spring and later fall, cause delayed but rapid spring drawdown and early but prolonged fall senescence in northern latitudes (Parazoo, N. C. et al, 2016, Detecting regional patterns of changing co2 flux in Alaska, PNAS)
Authors Response R1C11: This is an interesting point. Yes, we mention the specific latitude at which the period in Rise and Fall segments are equal; we now clarify the text in this manner as below. We appreciate the reference as we had not seen this before. We think we understand what the reviewer is referring to. Long-range Transport analysis in Panazoo et al. (2016). Yes, we think that the latitude of equal phases (2N) should simply be thought of as an indicator of global activity. If the equal-phase latitude shifts north or south then one can infer that north-south mixing (i.e., poleward transport of signals) has changed substantially, and that, for example, northern seasonal cycle anomalies (in phase or amplitude) might have greater (or less) contribution from signals in the south. The procedure in Panazoo et al. (2016), which suggests zeroing fluxes by region to identify relative contribution of surface fluxes to regional signals, would be a good test to identify driving causes for potential shifts in the latitude of asymmetry inversion. We are also doing similar experiments to some extent, but think such analysis deserves its own focus. See changes added to the main text below.

Authors changes to text R1C11: The opposite gradient in period lengths of Rise and Fall segments implies that around 2N, the period of Rise and Fall segments are of equal duration. North of this point of inversion in asymmetry, the period lengths of Rise segments are greater than in Fall segments, with an increasing asymmetry as latitude increases... Nevertheless, a north or south shift in the latitude of inversion (i.e., 2N) would indicate that long-range transport of atmospheric signals, such as the poleward transport of southerly signals (Panazoo et al. 2016), has changed substantially. In which case, the relative contribution of long-range signals from southerly locations to seasonal cycle anomalies (in phase or amplitude, in northerly locations might be greater or less than expected.

Review 1 comment 12: L350-354 -> The question of whether the point of inversion changes over time due to biosphere activity could easily be answered with the model. Why not try this?

Authors Response R1C12: Yes, Reviewer 2 also asked us to clarify and we updated the text to make explicit our hypotheses. See Authors response to Reviewer 2 comment R2C7. We inferred that biosphere activity affects the point of inversion because the DGVMs simulated different points of inversion. The DGVMs themselves simulate different spatio-temporal patterns of biosphere fluxes, so it seems to reason that the biosphere activity affects the point of inversion. As for extracting more information about this inversion point by conducting simulations with a single model – yes, this would be interesting. We are trying something along these lines, but we have yet to conclude that line research.

Review 1 comment 13: L357-359 and Fig 4 -> OCO-2 is mentioned in text and caption but I dont see any values plotted, and there is not mention of this data in the methods

Authors Response R1C13: This was an error. We did not include OCO-2 in the analyses for this paper. The text has been updated accordingly.

Review 1 comment 14: Sec 3.4 -> A few comments: (1) The meaning of individual bars representing regional asymmetries in Fig 6 (10 bars total per region) is not explained in the text or the figure.

Authors Response R1C14: The figure legend has been updated as below.

Authors changes to text R1C14: Figure 6. Period asymmetries (A) and Amplitude asymmetries (B) in GOSAT XCO2 seasonal cycles. The bars represent differences in amplitude or period for consecutive Fall (F) and Rise (R) segments, taking the Fall segment as reference. For example, if the time series follows the sequence F1, R1, F2, R2, F3, R3, (i.e., 3 seasonal cycles), then the difference between the first segment (F1) and the second segment (R2) is calculated as ‘F1-R2’; a zero value would indicate that the metric (amplitude or period) were equal, whereas an asymmetry would be indicated by a positive (F1 > R2) or negative (F1 < R2) value. By definition, consecutive segments cannot be categorized as F-F or R-R. Asymmetry statistics are not traditional summaries, but nevertheless, they are characteristic and in some regions persistent patterns of the seasonal cycle that are undoubtedly influenced by biosphere activity.

We thank both reviewers for their comments and suggestions. We know this paper is technical work and requires valuable time for such reviews. We think text added to the manuscript as a response to reviewers has made improvements and helped clarify assumptions and interpretation.
2 Response to Reviewer 2

Review2 comment1: Determining the amplitude and phase of a time series is a notoriously difficult problem, especially a time series with a superimposed time dependent trend, normally requiring a lengthy time series to minimise the effects of edge effects. The GOSAT record runs from 2009 to present so I am curious while they curtailed their analysis at 2012.

Authors Response R2C1: We clarified in the methods section 2.1 Satellite XCO2 data that Satellite data was freely obtained and analyzed only for 2009-2012 because it corresponded to the overlapping timeframe of available simulation data.

Review2 comment2: Armed with only a few seasonal cycles the authors will find it difficult to properly remove the lower frequency variations, which will arguably pervade the column measurements more so than surface measurements. The authors have used a spectral method to remove short-term variations less than 80 days. It would be useful (for at this reader) to understand why they chose that value as a cut-off.

Authors Response R2C3: We used an 80-day cutoff value because it was specified as the standard value to remove short-term variations in seasonal cycle analyses when using the ESGR algorithm (Pickers and Manning 2015; also, described in https://www.esrl.noaa.gov/gmd/cgg/ubl/ergrf/crfit/crfit.html). To our understanding, and according to Thoning et al. (1989; pp 8558, 2nd para.; https://doi.org/10.1029/JD094iD06p08549), a low pass filter of 50 days was originally applied to remove shorter-frequency variations in the data that were unrelated to large-scale atmospheric mixing. That is, the intention of the low pass filter of 50-days was to retain month-scale variations in the atmospheric data. Apparently, the standard was since extended to 80-days for the short-term cutoff so that only variations that were evident, or maintained, for the time scale of 3-4 months were retained (3-4 month in the frequency domain is 4.50 cycles/yr). In the end, we thought such a cutoff was suitable for this analysis because seasonal-scale variations are of general interest to terrestrial carbon cycle scientists. We added the following clarifying sentence to the text. Authors changes to text R2C3: The cutoff for the short-term filter was set at the recommended value of 80 days (Thoning et al., 1989). The short-term cutoff of 80-days retains data variations that are evident, or maintained, for the time scale of 3-4 months (4.50 cycles/yr).

Review2 comment3: I thought that the math was presented in an unnecessarily complicated way. Surely, the second derivative and first derivative taken together are sufficient to determine the peak, trough and any saddle point found in the time series. Saddle points can be found in Arctic seasonal cycles, for instance.

Authors Response R2C3: Yes, we tend to agree. We had simplified the text description as much, but chose to also provide a mathematical description for those inclined towards symbols or for reproduction of the procedural steps of the algorithm without having to review the computer code. We would like to keep the mathematical level at this length, if there is no strong objection.

Review2 comment4: Nevertheless, the method appears to be sound. The authors appear to focus on model evaluation instead of using the method to improving understanding of the carbon cycle. Consequently, there is little in the way of physical interpretation of the metrics in sections 3.2 and 3.3.

Authors Response R2C4: Yes, good point; we struggled with this ourselves given space limitations in describing the algorithm, the evaluation, and subsequent interpretation of models. We tried to outline future approaches in the Discussion for such interpretations. The issue is that we deal with a convolution of near- and far-field surface fluxes. We think the methods and algorithm presented in this study are a step forward towards the attribution of variation in the seasonal cycle metrics.

Review2 comment5: How do the authors take into account the uncertainties associated with the column data?

Authors Response R2C5: We use the Level-2 product that contains only high-quality and bias-adjusted data points. With regards to additional uncertainties in the satellite column data, we assume that uncertainties are random and normally distributed around zero, such that they average-out when taking the mean of all data points within a region. Spatially-averaged column uncertainties can be minor for seasonal cycle analyses if only considering the effect of the averaging
kernel (0.15 ppm on average; Lindqvist et al. 2015 https://doi.org/10.5194/acp-15-13023-2015), but could amount to larger errors (1.5 ppm) if instrument noise, the main source of uncertainty, is also considered (Yoshida et al. 2011 https://doi.org/10.5194/amt-4-717-2011). We added the following caveat to the text in the methods section: Authors changes to text R2C5: Satellite data have uncertainties of their own based on instrument noise, version of retrieval algorithm used to filter atmospheric effects, and averaging kernels (Yoshida et al. 2011, Lindqvist et al. 2015). A full quantification of uncertainty in satellite-derived seasonal cycles is beyond the scope of this study, but such an analysis could be useful for benchmarking purposes as models continue to reduce large biases (>> 1.5 ppm). Nevertheless, we make the assumption that lower biases are generally indicative of better model performance.

**Review2 comment6:** For the model analysis, do the authors sample the model when/where there are observations?

Authors Response R2C6: Yes, we use a co-location method to sample the simulated data. Clarifying text was updated as below, ref. Guerlet et al. 2013 https://doi.org/10.1002/jgrd.50332

Authors changes to text R2C6: We then used co-location sampling of the ACTM XCO2 data to match the location and timeframe (13:00 hr local time) of observations, 5 days to account for (i.e., by averaging) sub-weekly transport errors (Guerlet et al., 2013).

**Review2 comment7:** Line 356: We suggest that the latitude of the inversion of period asymmetry is a characteristic indicator of global atmospheric dynamics and biosphere productivity. It would be useful for the reader to understand the origin of this suggestion.

Authors Response R2C7: We appreciate the suggestion. We replaced text and clarified as below: Authors changes to text R2C7: We hypothesize that the latitude at the point of inversion of period asymmetry is a characteristic indicator global atmospheric dynamics and biosphere productivity. Our rationale is that if (i) the primary driver of the period of drawdown (Fall) or release (Rise) in XCO2 seasonal cycles is the terrestrial biosphere, and (ii) DGVMs themselves simulate the terrestrial biosphere, then variation in the simulated point of inversion of asymmetry by different DGVMs suggests a strong influence of biosphere activity on this emergent pattern. The most obvious driver affecting the period being plant phenology. However, we already know that seasonal cycle in XCO2 is dominated by flux seasonality in land biosphere, with the ocean and fossil fuel emission seasonality plays only a secondary role.

**Review2 comment8:** Line 360: It may be possible to add this emergent pattern as a benchmark to evaluate models that attempt to reproduce more direct indicators of biosphere activity... How important is atmospheric transport in determining zonal variations in this emergent pattern?

Authors Response R2C8: The effect of transport on zonal variation of this emergent pattern is likely to be large (Fig. 13 in Basu et al.; doi:10.1029/2011JD016124). Please note that the transport model (JAMSTECSs ACTM) used in this study generally performs well while evaluated against SF6 measurements, a tracer of atmospheric transport (https://www.atmos-chem-phys.net/11/12813/2011/; doi:10.1038/nature13721).

**Review2 comment9:** For the reasons outlined in the (balanced and frank) discussion I am left wondering how the metric will be used to correct models given the uncertainties associated with emissions from fossil fuel combustion and cement production. Could similar patterns emerge from nature and models for different reasons?

Authors Response R2C9: We know contribution of fossil fuel and cement (FFC) emissions will be less influential in seasonal cycle metrics. This is not to say that seasonality in FFC emissions is absent, but more so that the biosphere imprints a much larger signal on these patterns (Fig. 4; doi:10.1186/s40562-017-0474-7). Yes, similar patterns could emerge from nature and models for different reasons, and we think that the time-stepping of simulated processes in most models does not lend itself to realistic timeframes of surface fluxes that, ultimately, influence seasonal patterns in XCO2. For instance, the timing of fire and deforestation has a strong seasonality in the tropics (burning and clearing during dry seasons) and is implicit in the satellite data, but such seasonal dependence is lacking in model schemes. In this sense, the idea that these benchmarks will help
correct models might be overstated. Perhaps it is better to suggest that models move toward these benchmark by first understanding the limitations in direct comparisons of modeled surface fluxes to atmospheric XCO2. While potentially of great value to modelers, global ecosystem models were never designed with goal of using large scale emergent patterns in XCO2 as benchmarks so there are some basic hurdles to overcome.
A segmentation algorithm for characterizing Rise and Fall segments in seasonal cycles: an application to XCO₂ to estimate benchmarks and assess model bias

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Abstract. There is more useful information in the time series of satellite-derived column-averaged carbon dioxide (XCO₂) than is typically characterized. Often, the entire time series is treated at once without considering detailed features at shorter timescales, such as non-stationary changes in signal characteristics - amplitude, period, and phase. In many instances, signals are visually and analytically differentiable from other portions in a time series. Each Rise (increasing) and Fall (decreasing) segment, in the seasonal cycle is visually discernable in a graph of the time series. The Rise and Fall segments largely result from seasonal differences in terrestrial ecosystem production, which means that the segment’s signal characteristics can be used to establish observational benchmarks because the signal characteristics are driven by similar underlying processes. We developed an analytical segmentation algorithm to characterize the Rise and Fall segments in XCO₂ seasonal cycles. We present the algorithm for general application of the segmentation analysis and emphasize here that the segmentation analysis is more generally applicable to cyclic time series.

We demonstrate the utility of the algorithm with specific results related to the comparison between satellite- and model-derived XCO₂ seasonal cycles (2009-2012) for large bioregions on the globe. We found a seasonal amplitude gradient of 0.74-0.77 ppm for every 10˚ degrees of latitude for the satellite data, with similar gradients for Rise and Fall segments. This translates to a south-north seasonal amplitude gradient of 8 ppm for XCO₂, about half the gradient in seasonal amplitude based on surface site in-situ CO₂ data (~19 ppm). The latitudinal gradients in period of the satellite-derived seasonal cycles were of opposing sign and magnitude (-9 days/10˚ latitude for Fall segments, and 10 days/10˚ latitude for Rise segments), and suggests that a specific latitude (~ 2˚ N) exists which defines an inversion point for the period asymmetry. Before (after) the point of asymmetry inversion, the periods of Rise segments are less (greater) than the periods of Fall segments; only a single model could reproduce this emergent pattern. The asymmetry in amplitude and period between Rise and Fall segments introduces a novel pattern in seasonal cycle analyses, but while we show these emergent patterns exist in the data, we are still breaking ground in applying the information for science applications. Maybe the most useful application is that the segmentation analysis allowed us to decompose the model biases into their correlated parts of biases in amplitude, period, and phase, independently for Rise and Fall segments. We offer an extended discussion on how such information on model biases and the emergent patterns in satellite-derived seasonal cycles can be used to guide future inquiry and model development.

KEYWORDS: GOSAT, DGVM, segmentTS, time series analysis, land use change, seasonal cycle
1. Introduction

Most of our understanding about atmospheric CO$_2$ dynamics has come from CO$_2$ sampled by in-situ flask samples or eddy-flux towers at Earth’s surface (Ciais et al., 2014). While these data streams have proved incredibly useful, the transient dynamics of fluxes simulated by global-scale terrestrial models have only been compared to a relatively few locations on Earth. In contrast to surface CO$_2$ samples, which sample CO$_2$ concentrations in the planetary boundary layer, satellite observations of CO$_2$ are made by downward-looking Fourier spectrometers from the top of the atmosphere and represent an integrated estimate of CO$_2$ concentrations in a full column of atmosphere, hereafter ‘XCO$_2$’ (Wunch et al., 2011; Crisp et al., 2012). Although fluxes from the surface have a large influence on the total column CO$_2$, the vertical and horizontal transport of air masses in higher atmospheric layers, each with different concentrations CO$_2$, also influences the CO$_2$ concentrations in the total column (Belikov et al., 2017), including that of the stratosphere (Saito et al., 2012).

The synoptic coverage and integrated nature of XCO$_2$ means that surface fluxes from around the globe impart information into the seasonal dynamics and inter-annual variability of regional seasonal cycles, which is both a confounding and useful property for evaluating large-scale models. The integrated nature of the data also means that even a few years of data will be sufficient to evaluate the simulated dynamics of global-scale models. We propose that if models can reasonably simulate the timing and magnitude of terrestrial surface fluxes in all bioregions, then we would expect that the simulated XCO$_2$ would match reasonably well with the seasonal dynamics from the benchmark satellite data. Such demonstrated ability could strengthen confidence in regional-to-global model simulations.

To gain insight into seasonal cycle dynamics of satellite XCO$_2$ and individual model behavior, we demonstrate a novel approach to extract more information from the seasonal cycle than is typically characterized. In evaluations of model performance, traditional performance statistics (root-mean-squared-error, correlation, standard deviation) are used to quantify bias in phase and amplitude of the seasonal cycle against a benchmark signal (Coupled Model Intercomparison Project (CMIP) Earth System Models in Glecker et al., 2008; DGVMs in Anav et al., 2015). In almost all applications, however, the entire time series is treated at once without considering detailed features at shorter timescales, such as non-stationary changes in amplitude, magnitude, period, or phase (Fig. 1). We suggest that traditional performance statistics be applied to categories of unique patterns in the seasonal cycle, and not to the entire time series, thereby characterizing the error structure in a manner that can relate temporal dynamics (amplitude, magnitude, phase) with unique underlying processes.

We extend and apply a time series segmentation method (Ehret and Zehe, 2011) to extract the Rise and Fall segments in seasonal cycles of satellite-derived and simulated XCO$_2$, based on a suite of terrestrial ecosystem models. The advantage of the segmentation approach is that it allows an error structure to be accurately characterized by separately calculating the errors in amplitude, period and phase for each segment type (Rise, Fall). For example, in a graph of a multi-year seasonal cycle of XCO$_2$ (Fig. 1), each increasing and decreasing segment is visually discernable and analytically differentiable from other portions in the seasonal cycle; hereafter, Rise refers to increasing segments and Fall refers to decreasing segments in a seasonal cycle. The Rise and Fall segments largely result from seasonal differences in the onset and cessation of terrestrial ecosystem production (Keeling et al., 1995),
which means that a segment’s signal characteristics (i.e., amplitude, period, phase) are likewise influenced by different stages of terrestrial ecosystem activity. By segmenting the time series into similar component signals, we can then test for differences in the signal characteristics of Rise and Fall patterns and provide insight into a model’s ability to recreate these features of the seasonal cycle over multiple years.

Our first aim was to simply characterize the satellite-derived XCO$_2$ seasonal cycles in terms of Rise- and Fall-type segment variation. Secondly, we evaluated if signal characteristics and model biases differed or were correlated among Rise and Fall segments, which would help provide information in the missing parts of the satellite-based time-series (i.e., at high latitudes during boreal winter and in the Tropics during the wet-season), which we demonstrate is possible. We also evaluated if model biases between Rise and Fall segments differed enough to provide information about the underlying model representation of terrestrial dynamics, which we underscore as possible but discuss the limits for inference in this regard. Lastly, we explored how a single modeled process (land use and land cover change; LUC) manifests in the different signal characteristics and biases in Rise and Fall segments. We offer discussion on how the segment-based model biases and emergent patterns in satellite-derived seasonal cycles can be used to guide future inquiry and model development.

2. Methods

2.1 Satellite XCO$_2$ data

Satellite observations of XCO$_2$ were obtained from the Greenhouse gases Observing SATellite (GOSAT; version 7.3). Onboard the satellite, a Fourier-transform spectrometer measures the thermal and near-infrared absorption spectra of the constituent atmospheric gases within the footprint of observation (~10 km). Satellite data was freely obtained and analyzed only for 2009-2012 because it corresponded to the overlapping timeframe of available simulation data. The data were downloaded from NASA Goddard Earth Sciences (GES) Data and Information Services Center (DISC) online repository (<https://oco2.gesdisc.eosdis.nasa.gov/data/GOSAT_TANSO_Level2/ACOS_L2_Lite_FP.7.3/>; accessed 25 April 2018). We used the Level-2 Lite data products, which include only high-quality and bias-adjusted data points, based on the Atmospheric CO$_2$ Observations from Space (ACOS) retrieval algorithm version 7.3 (Crisp et al., 2012; O’Dell et al., 2012).

A note that satellite data are subject to their own uncertainties based on instrument noise, version of retrieval algorithm used to filter atmospheric effects, and averaging kernels (Yoshida et al., 2011; Lindqvist et al., 2015). We made the assumption that averaging kernel has a minimal effect on extracted seasonal cycles and we did not apply averaging kernels to the simulation data in this study. A full quantification of uncertainty in satellite-derived seasonal cycles is beyond the scope of this study, but such an analysis could be useful for benchmarking purposes as models continue to reduce large biases (>> 1.0 ppm). Nevertheless, we make the assumption that lower biases are generally indicative of better model performance.

2.2 Simulated Terrestrial Fluxes from DGVMs
The Net Biome Exchange (NBP) from land-to-atmosphere was simulated by six terrestrial ecosystem models (Table 1) that were part of the TRENDY model inter-comparison project version 2 (Sitch et al., 2015; dgvm.ceh.ac.uk). We use the atmospheric convention and make fluxes to the atmosphere positive, and fluxes to the land negative. We assumed that the primary modes of seasonal variability in terrestrial NBP at large scales is described by three terms, Net Ecosystem Production (Net Primary Production – Heterotrophic Respiration), fluxes from fire, and land use change (LUC). The protocol for the DGVM inter-comparison standardized the (i) forcing data: gridded (0.5°) climate (air temperature, short- and long-wave radiation, cloud cover, relative humidity and precipitation), global annual mean CO$_2$; and the (ii) initial conditions for time-varying simulations for the past century (1860-2012). We used simulated NBP for two sets of model simulations, one where land use (natural vegetation, crop, and pasture fractional cover) is fixed at values from the year 1860 (‘S2’ scenario described in Sitch et al., 2015), and another simulation where land use change is simulated according to the HistorY Database of the global Environment (HYDE v3.1; Goldewijk et al., 2011) (‘S3’ scenario as described in Sitch et al., 2015); both simulation types were forced with time-varying climate and CO$_2$.

2.3 Fossil Fuel and Ocean Fluxes

The modes of variability (trend, seasonality, intra- and inter-annual variability) in XCO$_2$ are also influenced by fluxes from oceanic exchange, fossil fuel consumption and cement production. We used a simplified model of oceanic CO$_2$ exchanges from Takahashi et al. (2009), and monthly-mean fossil fuel emissions from the European Commission’s Emissions Database for Global Atmospheric Research (EDGAR v. 4.2), based on country-level reporting and emissions factors, and the Fossil Fuel Data Assimilation System (http://edgar.jrc.ec.europa.eu/).

2.4 Simulated XCO$_2$ using an Atmospheric Model

Simulations of atmospheric CO$_2$ were conducted for the period of 2009-2012 using the land, ocean, and fossil fuel fluxes. We used the Center for Climate Systems Research/National Institute for Environmental Studies/Frontier Research Center for Global Change (CCSR/NIES/FRCGC) AGCM-based chemistry transport model (ACTM) (Patra et al., 2009). The ACTM was run at a horizontal resolution of T106 (~1.125° X 1.125°), and 32 sigma-pressure vertical levels. The simulated XCO$_2$ values were obtained by taking the sum of the pressure-weighted CO$_2$ concentrations over all vertical layers, equivalent to the column-averaged observations. We then used ‘co-location’ sampling of the ACTM XCO$_2$ data to match the location and timeframe (13:00 hr local time) of observations, ± 5 days to account for (i.e., by averaging) sub-weekly transport errors (Guerlet et al., 2013). We obtained the simulated XCO$_2$ for each component flux (land, fossil fuel, ocean) and finally summed the components to get the XCO$_2$ used in bias evaluations.

2.5 Extraction of XCO$_2$ Seasonal Cycles

We first estimated the mean of daily XCO$_2$ values by averaging gridded values within each of the 11 TransCom region (Fig. 2), for both the observed and modeled XCO$_2$. This procedure was as straight forward as written above, and the accompanying computer code (software: R for Statistical Computing) is provided as additional
Supplementary Material. We then applied a digital filtering algorithm (ccgcrv by Thoning et al., 1989; https://www.esrl.noaa.gov/gmd/ccgg/mbl/crvfit/crvfit.html) to the mean time series to extract the long-term trend and seasonal cycles, fitted as a 2-term polynomial (linear growth rate was used because the time series spanned only 3 years) and a 4-term harmonic function to account to seasonal asymmetry. Temporal data gaps were linearly interpolated by the algorithm. After subtracting the long-term trend and seasonal cycle, the ccgcrv algorithm filters the residuals in the frequency domain using a Fast-Fourier Transform (FFT) algorithm to retain short- and long-term interannual variation (additional details in Nakazawa et al., 1997; Pickers and Manning 2015). The cutoff for the short-term filter was set at the recommended value of 80 days (Thoning et al., 1989). The short-term cutoff of 80 days retains data variations that are evident, or maintained, for the time scale of 3-4 months (4.56 cycles/yr). The cutoff for the long-term filter was set to a large number (3000), which is longer than the number of days in our time series (365 days/yr * 3 yr = 1095 days) because, with such a short time series, we needed to force the estimation of a linear trend with no interannual variation; otherwise, the algorithm would be too sensitive and derive variation in the trend without practical justification. For all analyses here forth, we combined the seasonal cycle with the digitally filtered short-term variation and used the derived data points along the smoothed seasonal cycle curves for analysis.

2.6 Technical description of algorithm: Segmentation of seasonal cycles

The purpose of this section is to describe the technical algorithms used in the analysis. These algorithms are based on concepts put forth by Ehret and Zehe (2011), translated herein to the R computing language (R Development Core Team, 2008). Where Ehret and Zehe (2011) focused on the single hydrological events, we modify and restructure the algorithm to accommodate much longer non-stationary cyclic time series for general application to seasonal cycle analyses. An R package for the segmentation algorithm is freely available at the GitHub repository <https://github.com/lcalle/segmentTS>. A permanent version of the code is available in the Dryad Digital Repository <doi:10.5061/dryad.vk8ms62>. The computer code is annotated and provides data used in this study with demonstrations for applying the algorithm to remove local minima or maxima and the categorization of seasonal cycle segments.

2.6.1 Categorize segments and isolate seasonal Rise and Fall cycles

We first determine the first derivatives numerically. The ccgcrv signal decomposition algorithm outputs a daily time series in the form of a multi-dimensional array, but we focus on a subset of the array, the 2-dimensional rectangular matrix representing points along the detrended seasonal cycle,

$$ B = \begin{bmatrix} b_{1.1} & b_{1.2} & b_{1.3} \\ \vdots & \vdots & \vdots \\ b_{n.1} & b_{n.2} & b_{n.3} \end{bmatrix} $$

(1)

where the first column is the row index, the second column are dates, the third column is the detrended XCO₂ ppm with the short-term variation added back-in, the rows are the triplets of the index, time in the x-direction, and magnitude (XCO₂ ppm) in the y-direction.

We can numerically determine the first derivative in the y-direction at each point via differencing, as in,

$$ \nabla b_{t.2} = b_{t.2} - b_{t-1.2} $$

(2)
We then classifying each row in first column \((b_{i,2} \ldots b_{n,2})\) into one of the following categories below and expand \(B\) to a \(n \times 4\) matrix to store the classified values. The main objective is to classify the endpoints (Trough, Peak) of the Rise and Fall segments:

\[
\forall i \in \{1 \ldots n\}, \quad b_{i,4} = \begin{cases} 
Trough, & (\forall b_{i,2} < 0) \land (\forall b_{i+1,2} > 0) \\
Rise, & (\forall b_{i,2} < 0) \land (\forall b_{i+1,2} < 0) \\
Fall, & (\forall b_{i,2} > 0) \land (\forall b_{i+1,2} > 0) \\
Peak, & (\forall b_{i,2} > 0) \land (\forall b_{i+1,2} < 0) \\
Null, & otherwise
\end{cases}
\]  

(3)

We then take the subset of endpoints \((S)\) in the classified matrix \(B\),

\[
S \subset B = \{B | b_{i,3}: Trough, Peak\}
\]  

(4)

where \(S\) retains the dimensions of the \(B\). A unique segment \((s)\) is defined as a set of two consecutive endpoints (rows) in \(S\) that alternate in their classification of Trough or Peak, meeting the condition:

\[
s \subset S = \{S_{i,4}: Trough \land S_{i+1,4}: Peak\} \lor \{S_{i}: Peak \land S_{i+1,4}: Trough\}
\]  

(5)

We identify local minima and maxima that are deviations in otherwise longer (seasonal) and more general Rise and Fall patterns based on two criteria below, and then reclassify the segments based on the class of the segment with the largest amplitude. The amplitude of a segment \((a_s)\) is defined as:

\[
a_s = |s_{i,2} - s_{i+2,2}|
\]  

(6)

, where \(s_{i,2}\) is the first endpoint in the second column (XCO\(_2\) ppm), either a Trough or a Peak, and \(s_{i+2,2}\) is the second endpoint for the specific segment, which, by definition the first endpoint must be classified \((s_{i,4})\) as one of Peak or Trough and must not have the same classification as the second endpoint \((s_{i,4})\).

The first criterion sets a minimum threshold for the amplitudes, redefining the set of endpoints defining the segments, as below:

\[
s^* \subset S = \{s | a_s > \text{minimum threshold}\}
\]  

(7)

Segments that represent local minima or maxima that are not of interest to the user can be identified by a comparison of amplitudes of consecutive segments, dropping the segment with the lowest amplitude, as below:

\[
s'' \subset s^* = \{s^* | s^* \neq \min(a_{s-1}, a_s, a_{s+1})\}
\]  

(8)

This procedure results in a new subset of segment endpoints \((s'')\) with consecutive elements that have similar classification (e.g., \(s''_{1,4} := Peak\), and also \(s''_{2,4} := Peak\)), which needs to be rectified. We keep the endpoints with the lowest Trough value and the largest Peak value,

\[
s[t]^* \subset \{s[t]_{1,2} + s[t + 1]_{1,2}, s[t+1]_{2,2} + s[t + 1]_{2,2}\} = \begin{cases} 
\min(s[t]_{1,2}, s[t+1]_{1,2}), & s[t]_{1,4} := Trough \land s[t + 1]_{1,4} := Trough \\
\max(s[t]_{1,2}, s[t+1]_{1,2}), & s[t]_{1,4} := Peak \land s[t + 1]_{1,4} := Peak \\
\end{cases}
\]  

(9)

where \(s[t]\) is a unique segment in the set of \(s\) segments, \(s[t + 1]\) is the following consecutive segment, \(s[\ldots]_{1,2}\) and \(s[\ldots]_{2,2}\) are the segment first and last endpoints, respectively, and \(s[t]^*\) is the updated segment with new endpoints \(s[t]_{1,2}^*\) and \(s[t]_{2,2}^*\), while segments \(s[t], s[t + 1]\) have been removed from the set of segments \((s)\).
A (subjective) limit can also be set to exclude or include segments based on temporal proximity. For example, consecutive minima (minima/maxima/minima) should not be considered local minima if separated by 365 days; these are probably real local minima driven by processes unique to different seasons. By contrast, local minima separated by 60 days may represent signals within the overall seasonal Rise and Fall pattern (e.g., due to fire). For this study, we are more interested in assessing the general seasonal patterns. We therefore estimate the temporal distance, in ‘days’ ($D_s$), between the first endpoints of consecutive segments and evaluate the condition as below,

$$ D_s = s[t + 1]_{1,3} - s[t]_{1,3}, \text{ given } s[t]_{1,4} \land s[t]_{4,1} \text{ are of the same class (Trough, Peak) }$$

(10)

$$ s^* < s = \{ s \mid D_s > \text{minimum threshold} \} \quad (11) $$

where $s[.]_{1,3}$ is the endpoint date in the $x$-direction, and the minimum threshold for distance between endpoints is set at a conservative 250 days (~8 months), ensuring that only the main Rise and Fall patterns within a given year are captured. This conditional evaluation also results in a new subset of segments ($s^*$) with consecutive elements with similar classification, as above, but Eq. 9 can be re-applied to select the endpoints which represent general Rise and Fall patterns.

Additional criteria can be applied to automate the removal of local minima/maxima that are not relevant to the user, but we caution that visual inspection of the signal is important to avoid unwanted reclassification of segments in the time series.

### 2.6.2 Human-assisted pattern recognition via visual inspection

The procedure outline in Sect. 2.6.1, above, is applied to both the reference ($R$) and modeled ($M$) seasonal cycle time series. In the best of cases, the procedure would result in matrices for $R$ and $M$, each with an equal number of segments and the same sequence of endpoint classes (Trough, Peak, Trough, Peak, ...). In practice, however, the number and sequence of segments in $M$ will not always equal the number or sequence of segments in $R$. When variability in the modeled seasonal cycle results in many local minima/maxima, and therefore many short Rise/Fall segments, there can be a mismatch between the indices of segments, wherein smaller/shorter segments in $M$ are matched to much larger/longer segments in $R$; this is simply an artefact from automation of the procedure outlined previously.

Although we have implemented automated procedures in the algorithm that reconcile these types of mismatches, we found that it was considerably quicker to (i) conduct a ‘blind’ run of the algorithm on the data, (ii) visually inspect the automated graphical plots of the seasonal cycles for mis-matching segments (Supplementary Material Fig. S1), (iii) identify the index of the mis-matching endpoints in $M$, and then finally (iv) re-run the algorithm specifying the index of the endpoint in $M$ for removal.

### 2.6.3 Segment signal characteristics and error statistics

The amplitude (Eq. 6) and period ($p$ in ‘days’) for all segments are first characterized, with the period defined as,

$$ p_s = s_n - s_0 \quad (12) $$

where $s_n$ and $s_0$ are the end and start dates of a segment, respectively. Then, for each segment in $M$ and $R$, a complementary vector $Mx$ and $Rx$ is created in the $x$-direction with a fixed number of, and equally-spaced, dates,

$$ x = (x_1 \ldots x_k) \quad (13) $$
Each element in $M_x$ corresponds, by index, to an element in $R_x$, such that a matching pair exists. Similarly, a complementary vector $M_y$ and $R_y$ is created in the y-directions, with the length of the vector matching the length of the vector in the x-directions ($k$). For each element in $M_y$ and $R_y$, we perform a linear interpolation of the values of XCO$_2$ ppm in $B(b,z)$ for the indices given by the dates in $M_x$ and $R_x$; fortunately, the linear interpolation is automated by the approx function in R, which makes this procedural step straightforward. The end result is, for every segment in $M$ and $R$, four vectors of equal length in $M_x, M_y$ and $R_x, R_y$, with the timing of the data and values of XCO$_2$ ppm that follow the corresponding seasonal cycles in $B$. We can then decompose the corresponding errors in phase and magnitude along the time series,

$$
\text{Timing error} = M_x - R_x \\
\text{Magnitude error} = M_y - R_y
$$

Although in this paper we focus only on errors in amplitude, period, and phasing of the segments, the time series of errors in timing and magnitude are an additional level of detail in the error structure that is evaluated by the segmentation algorithm.

### 2.7 Statistical summaries

For each of the Rise and Fall segments within a region, we summarized the characteristics by averaging the amplitude (ppm), period (days), and the phase, which we estimated in two ways based on the day of year for the first and last endpoint of the corresponding segment (DOYstart, DOYend, respectively). For model biases, we used the total sum of the component tracers (land + fossil fuel + ocean) and we summarized model biases as the region-average of segment-to-segment differences between model and observation. Although we aggregate the biases among segment types, and therefore lose information, we do this to demonstrate that there are distinct general patterns in the Rise and Fall segments, regardless of region. Of course, one might be more interested in one bioregion over another, and while this is indeed possible and suggested, such analysis is not the intent of this paper.

The latitudinal variation of amplitude and period length for Rise and Fall segments was evaluated by comparing the regionally-averaged metrics against the average latitude of each TransCom region. We sought to evaluate a model’s ability to reproduce the north to south gradient in seasonal cycle characteristics. We also use data from in-situ [CO2] flask samples for 2005-2015 (NOAA/ESRL/GMD CCGG cooperative air sampling network; https://www.esrl.noaa.gov/gmd/ccgg/flask.php) as a check to evaluate latitudinal variations of surface site seasonal amplitudes. Surface sites were selected if they had a minimum of five years of data between 2005-2015, with at least one flask sample per month. The peak-trough amplitude was then taken from monthly averaged data. Linear correlations were deemed statistically significant at levels of $p=0.05$.

The amplitude and period length asymmetries between Rise and Fall segments were calculated as in the following example. Given a sequence of data with segments of type \{Fall_1, Rise_1, Fall_2, Rise_2\}, representing seasonal cycles over two years, three asymmetries in amplitude and period length would be calculated for the sequence of segments, as (i) Fall_1 - Rise_1, (ii) Fall_2 - Rise_1, and (iii) Fall_2 - Rise_2. The asymmetries are referenced to Fall segments such that, for example, negative asymmetries mean that the amplitude (or period length) is greater in the Rise segment. The reason we calculated asymmetries between segments immediately before and
after the Fall segments is because we assumed that there is some degree of autocorrelation in the relational values that is both real and could provide useful information, but the underlying causal mechanisms are speculative at this point.

2.8 Application of approach

We applied the approach to evaluate the effect of LUC on XCO₂ by using the segment characteristics setting the ‘S2’ scenario as the reference time series and then following procedures outlined in Sect. 2.6 to match corresponding Rise and Fall segments in the S3 and S2 simulations. We then calculated the difference in the amplitude, period, and phase between matching segments, hereafter defined as the ‘LUC effect’. To evaluate the relative influence of the LUC effect on changes in amplitude, period and phase, we transformed the LUC effect to percentages by (a) dividing the LUC effect in amplitude by region-specific average amplitudes, and (b) dividing the LUC effect in the period length and phase (DOYstart, DOYend) by the region-specific average period lengths. We then pooled the absolute values of the standardized LUC effects for all regions, by model; the absolute values of LUC effect was used because we were more interested in any significant change, rather than a directional change in the metric values. We conducted an Analysis of Variance to test for significant differences among models and type of LUC effect (amplitude, period, and phase), in terms of the percent LUC effect, also setting significant differences at \( p=0.05 \). In this manner, we were able to determine the relative importance of LUC effect by metric and compare amongst models.

3. Results

3.1 Satellite coverage and XCO₂ seasonal cycles

The satellite data coverage had sufficient temporal density to extract smooth seasonal cycles (Fig. 3), except during Boreal Winter at high latitudes (> 50° N) and during the wet-season in Tropical Asia where there was clear evidence of linear interpolation over large data gaps (Supplementary Material Fig. S2-S4). We had to exclude North America Boreal and South America Tropical regions from all analyses because the data were too sparse and seasonal cycles could not be derived. The mean number of satellite retrievals per day in 5° bins was greater than 1 when averaged over a season, but the spatial distribution of the retrievals by month (Supplementary Material Fig. S2-S4) showed that only portions of the TransCom regions were being represented with satellite observations. The lack of a complete representative sample of satellite observations in a region suggests that the derived seasonal cycle will be biased towards the XCO₂ observations in those sub-regions with greater coverage. We take this finding as a caveat, but also demonstrate below that the derived seasonal cycles are a good representation of the general seasonal dynamics in the data.

There were noticeable deviations (local minimums) from otherwise consistent Rise and Fall patterns during a season (for example in North Africa in Fig. 3). We compared the seasonal cycles derived from DGVM XCO₂ co-located with GOSAT retrievals against DGVM seasonal cycles using all simulated XCO₂ and complete coverage (no-colocation). For the single DGVM studied in this side analysis, the local deviations were still evident in the seasonal cycles that used data with complete coverage (Supplementary Material Fig. S5). We believe that these
deviations are not artefacts of the spatial distribution of satellite retrievals, but instead are true patterns in the XCO$_2$ seasonal cycle. However, the co-location sampling did appear to have a greater effect on the amplitudes and periods in Southern Hemisphere regions, whereas the effect of co-location sampling was less influential in Northern Hemisphere regions.

The magnitude of the GOSAT seasonal cycle residual error, averaged over all regions, was $0.15 \pm 1.02$ ppm, which was not a small fraction relative to the average amplitudes when taking into account the standard deviation. However, the residuals, were normally and randomly distributed around zero (Supplementary Material Fig. S6), which we took to suggest that there was no systematic bias and that the daily spatial variation in data coverage averaged out, and what we derived was a realistic estimate of seasonal variation in XCO$_2$.

### 3.2 Latitudinal variation in XCO$_2$ seasonal cycle amplitudes

Seasonal amplitude varied predictably with latitude (Fig. 4). Latitude explained between 82-84% of the variation in seasonal amplitudes in GOSAT, with the range taken from linear models of Rise and Fall segments (Fig. 4). There was an increase in amplitude of $0.74 \pm 0.13$ ppm ($\mu \pm$ S.E.) for Rise Segments and $0.77 \pm 0.13$ ppm for Fall Segments for every 10 degrees of latitude for GOSAT. Whereas the XCO$_2$ amplitudes exhibited a linear relationship with latitude, in-situ flask samples of CO$_2$ exhibited a log-linear relationship with latitude (Fig. 5; $R^2 = 0.90$, d.f.=45, $p < 0.001$), which indicates larger amplitude gradients at higher than at lower latitudes. The difference results in a latitudinal range (Equator to 70°N) in seasonal amplitude of $\pm 7$ ppm for XCO$_2$ (taken as $70^\circ \ast [0.077 + 1.95*0.013]$), as the largest possible amplitude gradient in XCO$_2$; $\mu + 1.95*$S.E.) and $\pm 17$ ppm for surface CO$_2$. The dampened gradient in XCO$_2$ amplitude suggests substantial north-south atmospheric mixing, which is consistent with a previous study on the meridional versus zonal contribution to XCO$_2$ via atmospheric transport (Keppel-Aleks et al., 2012). In addition, the in-situ sampling stations are located in such a way that they sample the ‘background’ atmosphere, which reduces the influence of local to regional terrestrial fluxes, and instead they provide seasonal cycles representative of hemispheric- and continental-scales. The contrast between the latitudinal gradient in amplitude between XCO$_2$ in this study and in-situ surface samples may therefore be even greater than reported here (Olsen and Randerson, 2004; Sweeney et al., 2015).

Only LPX was able to simulate the GOSAT-derived latitudinal gradient (slope) in amplitude, but even in this model, the magnitudes of the amplitudes were consistently lower than GOSAT by $\pm 1.5$ ppm (Fig. 4). ORCHIDEE simulated the latitudinal gradient in amplitude reasonably well and CLM simulated a marginally stronger north-south gradient, whereas the gradient was much weaker in two models (OCN, VISIT) and there was no statistically detectable amplitude gradient in LPJ. The evidently enhanced meridional mixing of total column CO$_2$ complicates an interpretation of the finding that most models simulated a weaker gradient in XCO$_2$ seasonal amplitude (Fig. 4). It makes it difficult to determine why models do not reproduce the latitudinal gradient in amplitude very well – for example, are the magnitudes of the fluxes in certain regions too low or too high, such that they offset the seasonal amplitudes in the region of interest after atmospheric transport? We offer suggestions in the Discussion that might help answer these questions.

### 3.3 Latitudinal variation in XCO$_2$ seasonal cycle period
The period lengths of GOSAT XCO$_2$ seasonal cycles also varied predictably with latitude (Fig. 5) and there was no significant difference in the magnitude of the latitudinal gradients between Rise and Fall segments, although the direction of the gradient was positive for Rise segments and negative for Fall segments (Fig. 4). Latitude explained between 67-73% of the latitudinal variation in period lengths in GOSAT seasonal cycles. From South to North, the period lengths of Rise segments increased by 10 days per 10° of latitude for GOSAT. From South to North, the period lengths of Fall segments had negative gradient and decreased by -9 days/10° latitude for GOSAT. The opposite gradient in period lengths of Rise and Fall segments implies that around 2° N, the period of Rise and Fall segments of equal duration. North of this point of inversion in asymmetry, the period lengths of Rise segments are greater than in Fall segments, with an increasing asymmetry as latitude increases. We hypothesize that the latitude at the point of inversion of period asymmetry is a characteristic indicator global atmospheric dynamics and biosphere productivity. Our rationale is that if (i) the primary driver of the period of drawdown (Fall) or release (Rise) in XCO$_2$ seasonal cycles is the terrestrial biosphere, and (ii) DGVMs themselves simulate the terrestrial biosphere, then variation in the simulated point of inversion of asymmetry by different DGVMs suggests a strong influence of biosphere activity on this emergent pattern. The most obvious driver affecting the period being plant phenology. Furthermore, we already know that seasonal cycle in XCO$_2$ is dominated by flux seasonality in land biosphere, with the ocean and fossil fuel emission seasonality plays only a secondary role. Nevertheless, a north or south shift in the latitude of inversion (i.e., 2° N) would indicate that long-range transport of atmospheric signals, such as the poleward transport of southerly signals (Parazoo et al. 2016), has changed substantially. In which case, the relative contribution of long-range signals from southerly locations to seasonal cycle anomalies (in phase or amplitude) in northerly locations might be greater or less than expected. As of yet, however, it is unclear if this point of inversion is relatively stable over time or if, instead, the point shifts in latitude among years or decades depending on the relative influence of source-sink dynamics in biospheres in the Northern and Southern Hemispheres.

Most models correctly simulated the satellite-derived latitudinal gradient in period, but LPJ and VISIT did not simulate statistically significant gradients in either Rise or Fall segments, and LPX could only reproduce the gradient for Rise segments, but not for Fall segments (Fig. 4). For CLM, OCN and ORCHIDEE, the simulated gradients were statistically similar to GOSAT, although the absolute period lengths differed by up to 25 days. The latitudinal gradient in period of XCO$_2$ seasonal cycles is emergent from the underlying timing and duration of biosphere productivity, and as such, it serves as a high-level constraint on simulated dynamics. It may therefore be possible to add this emergent pattern as a benchmark to evaluate models that attempt to reproduce more direct indicators of biosphere activity, such as seasonal patterns in leaf area (Richardson et al., 2012), or primary production (Forkel et al., 2014).

3.4 GOSAT asymmetries in period and amplitude

The period asymmetry between Rise and Fall segments (Table 2) is clearer when comparing the periods of consecutive Rise and Fall segments (Fig. 6), taking the Fall segment as reference, as described in Sect. 2.7. The period asymmetries were in the same direction except for the Africa Northern, Africa Southern, and South America Temperate regions (Fig. 6A). The asymmetries exhibit stable patterns of consistent direction within many regions,
and they also display quite a bit of interannual variation in the magnitude (or direction in some cases) of the asymmetries themselves (Fig. 6A and 6B). For example, the standard deviation in period asymmetry averaged 11% of the region-averaged periods for GOSAT seasonal cycles, and it was greatest for the Africa Southern region (42%). For context, a 10% change amounts to a change in period asymmetry by 5-29 days, and as much as 73 days in the Africa Southern regions, which is certainly a remarkable change in the atmospheric signal. The period asymmetries can provide insight into the underlying terrestrial dynamics, for example, from interannual variation in the duration of the carbon uptake period (Xia et al., 2015; Fu et al., 2017), but it is yet unclear how changes in carbon uptake period manifest to affect these patterns of asymmetry. Furthermore, one DGVM (ORCHIDEE) was able to simulate period asymmetries, consistent in direction, with that of the GOSAT record when using co-location sampling. Albeit, the magnitude of the period asymmetry for ORCHIDEE was about half that of GOSAT, but it does suggest that the surface fluxes from this DGVM were more realistic in timing and magnitude. All other models had greater interannual variation in the direction of the asymmetry, with no other model reproducing the direction of asymmetry in all regions.

The amplitude asymmetries between consecutive Rise and Fall segments were more variable in the direction of the asymmetry for GOSAT (Fig. 6B). There was no consistent pattern in the direction or magnitude of the amplitude asymmetries within or among regions, but we did not investigate if there were annual patterns that were consistent among all regions. No model successfully reproduced the direction of asymmetry in amplitude across all regions in all years. As of yet, the relevance of interannual variation in the asymmetries is speculative, but we do know that such variation is not simply due to data coverage (Supplementary Material Fig. S5), so there may be more insightful information in the signal.

### 3.5 Correlated biases between Rise and Fall segments

The correlations of model biases differed more among Northern and Southern Hemispheres (NH and SH, respectively) than among regions, so we present the following analyses not by region, but by NH and SH. The NH regions were comprised of Africa Northern, Europe, Eurasia Temperate, North America Temperate; the SH regions were comprised of Africa Southern, Australia, and South America Temperate. These analyses required data on both Rise and Fall segments, which eliminated the Asia Tropical and Eurasia Boreal regions from these analyses.

Among Rise and Fall segments, and among all models and regions, the model biases in amplitude were nearly perfectly correlated (NH $R^2 = 0.99$, d.f. = 28, $t = 64.63$, p < 0.001; SH $R^2 = 0.99$, d.f. = 16, $t = 65.02$, p < 0.001; Fig. 7a and 7e). Except for ORCHIDEE and CLM, which exhibited the smallest amplitude biases, the other models all had amplitudes that were too low. In the SH, there was a similar pattern of negative amplitude biases (Fig. 7e), with exception that CLM simulated amplitudes that were too large in two of three SH regions. The strong correlations suggest that knowing the amplitude biases in one part of the seasonal cycle is sufficient to gain information about amplitudes in the missing part of the seasonal cycle. This might be particularly useful for constraining estimates of XCO$_2$ seasonal cycle patterns during timeframes that have poor satellite coverage (Boreal Winter, Tropical Wet Season). Furthermore, it is revealing that models which simulate amplitudes that are too low do so almost equally for both Rise and Fall segments, which is suggestive of a systematic bias in the sensitivity of the models to seasonal
changes in climate. Such systematic biases can be due to simulated fluxes that are overall lower in magnitude, or due to a pattern of spatio-temporal fluxes that end up offsetting or cancelling each other in the atmospheric domain, but we cannot yet definitively attribute the bias of individual models to one of these possible causes.

The average period biases of Rise and Fall segments were also strongly correlated, with a greater strength of correlation in the NH ($R^2 = 0.77$, d.f. = 22, $t = -8.53$, $p < 0.001$) than in the SH ($R^2 = 0.82$, d.f. = 21, $t = -9.87$, $p < 0.001$). In the NH, almost all models simulated periods that were too short in Rise segments and too long in Fall segments, in approximately equal and opposing amounts (Fig. 7b). In the SH, the period biases spanned both positive and negative values for both of the Fall and Rise segments, but also in approximately equal and opposing amounts of bias (Fig. 7f). There were only a few data points where the periods within a region were either biased (a) too short for Rise segments and also too short for Fall segments, or (b) where the Rise segment was biased too long and the Fall segment also biased too long. These patterns are suggestive of underlying constraints that compensate for biases in periods, such that situation (a) and (b), from above, rarely occur. Such constraints are likely associated with the underlying drivers of the period of Rise and Fall segments. For instance, models that simulate growing seasons that are too long will likely simulate Fall-segment periods that are also too long, and as a consequence, the dormant season will be shortened, as will the periods of associated Rise segments. Within a given model, the magnitude of compensating biases varied by region, so it is possible that biases in biosphere activity varied similarly by region. To incorporate such insights will require direct manipulation of the phenology represented by models, but improving the emergent patterns in period to better match the satellite-derived XCO$_2$ seasonal cycles will bolster confidence in the model’s ability to represent both fine-scale dynamics and the emergent large-scale atmospheric patterns.

3.6 Application of Approach: LUC effects on amplitude, period and phase metrics were non-trivial

We describe the LUC effect as the percent change in the Rise and Fall segment amplitude, period, and phase (DOY$_{start}$, DOY$_{end}$) when LUC processes are included in model simulations, relative to seasonal cycle metrics when LUC was not included in simulations. Among all models and Rise and Fall segments, the average LUC effect was largest on amplitude (mean 13.4%, or 0.37 ppm), but there were also non-trivial changes in the period (7.2%, or 13.2 days), and phase metrics of the DOY$_{end}$ (6.5%, or 11.4 days) and DOY$_{start}$ (6.2%, or 11.4 days). An Analysis of Variance suggested that the LUC effects did not significantly differ between Rise and Fall segments ($F = 0.006$, d.f. = 1, $p = 0.941$), and that the specific model explained 16% of the variation ($F = 15.183$, d.f. = 5, $p < 0.001$) and the metric explained only 5% of the variation ($F = 7.815$, d.f. = 3, $p < 0.001$). LPJ was an outlier in that it simulated larger LUC effects in every metric (mean LUC effect = 18%), approximately 8% greater than other models. The remaining variation in LUC effect was explained by the larger LUC effect on amplitude in LPX and VISIT (Fig. 8), whereas OCN simulated only marginally greater LUC effects than CLM and ORCHIDEE. The LUC effects were of similar magnitudes as the baseline interannual variation for these metrics, in terms of percent change, or greater in the case of the LUC effect on amplitude (Table 3).

The importance of the LUC effect on the amplitude of Rise and Fall segments was somewhat expected because LUC directly affects the type of land cover simulated in the models, for example, by converting forest to pasture or
pasture to forest and thereby influencing the magnitude of surface fluxes directly (Arneth et al., 2017). However, the effect of LUC on the temporal metrics of the seasonal cycle (period, phase) is typically understated in the literature. The LUC effects on period and phase are of the same relative magnitude as is observed in two-decades of advancement in the start and end dates of the carbon uptake period based on atmospheric inversion studies (Fu et al., 2017). It should not be a surprise then that LUC can affect the timing of surface fluxes, but this facet is often overlooked when the focus is solely on variability at annual or decadal timescales. At the very least, this work shows that land-surface modelers should consider the impact of LUC on the timing and duration of surface fluxes, in addition to its effect on the magnitude of the fluxes.

4. Discussion

4.1 Utility of a segment analysis for analyzing cyclic time series

We demonstrated that a segmentation analysis of satellite-derived XCO₂ seasonal cycles can generate direct estimates of amplitude, period, and phase at global and hemispheric scales, and that it can reveal stable patterns in the metrics which can be used as benchmarks to evaluate simulation models. There is obvious value in using standard statistics (RMSE, S.D., R², etc.) to characterize a time series and evaluate it against simulated reproductions (e.g., ‘Taylor diagrams’; Taylor, 2001; Supplementary Fig. S7). We do this too, but we argue that applying statistical measures of goodness-of-fit over the entire time series misses an opportunity to extract valuable information from observational data and provide more direct measures of bias. Studies that have evaluated amplitude and period biases directly have been based on the mean harmonic of the seasonal cycle (Peng et al. 2015), which lacks interannual variation, and therefore does not fully represent the modeled biases. Furthermore, the metrics for the asymmetric Rise and Fall patterns in seasonal cycles are not typically estimated, nor evaluated for bias. In the Europe region, for example, the interannual variation in amplitude (1.25 ppm) and period (25 days) is certainly not trivial (Supplementary Fig. S8), and if excluded in evaluations it would cause a biased assessment of what the models can and cannot do well, limiting the potential of such assessments to inform potential improvements.

Our study focused on the Rise and Fall segments in XCO₂ seasonal cycles, corresponding to periods when terrestrial ecosystems generally release and uptake carbon dioxide, respectively. Other studies might be more interested in shorter-term, pulse-type signals, such as the ability of models to simulate the effect of large scale fires or volcano eruptions in an atmospheric time series. In either case, the segmentation algorithm could help standardize and decompose model bias into its component parts of amplitude, period and phase biases.

4.2 Asymmetries provide new insights into the interannual variation of atmospheric signals

By definition, the asymmetries (Fig. 6) are not anomalies, but similarly, the amplitude asymmetries are directly related to underlying processes generating the imbalance in the amplitude and period between Rise and Fall segments. Most likely, the asymmetries reflect the difference in the magnitude or in the timing of fluxes during the growing season for Fall segments and phenological dormancy for Rise segments (Randerson et al., 1997). Whereas the signature of the terrestrial biosphere may be a more dominant driver of the period asymmetries, the amplitude
asymmetries may also be influenced by processes that the models simply do not simulate well, or in any sufficient manner in some cases, such as sub-seasonal representation of Fire and LUC (Earles et al., 2012) or volcano eruptions (Jones and Cox, 2001). The interannual variation in XCO₂ period and amplitude asymmetries are directly related the activity of terrestrial ecosystems, but questions remain – are the annual asymmetries in amplitudes or periods evident of a global response to large-scale climate phenomena, such as the El Niño-Southern Oscillation? Do some regions dominate and influence the signal more than others? To what degree do the asymmetries in one region provide information about asymmetries in other regions, and can we infer dynamics in Boreal regions, for example, by analyzing atmospheric signals in regions where satellite coverage is more complete? The asymmetries offer a new level of information on atmospheric dynamics that is ripe for exploring.

4.4 The effect of LUC on seasonal cycles is in addition to the effect on the long-term trend

Much focus has been put on accurately characterizing component fluxes from land use and land cover change simulated by DGVMs (Pongratz et al., 2014; Calle et al., 2016), but we also show that LUC influences the atmospheric seasonal cycle period and phase at a level that is comparable to the reference rates of interannual variation in those metrics (Table 3). This underscores a complex problem of trying to simultaneously resolve the contribution of LUC fluxes to the long-term trend in atmospheric CO₂ (Le Quéré et al., 2018), and also to represent realistic LUC effects on seasonal-scale biosphere activity (Betts et al., 2013; Bagley et al., 2014). For instance, when land is converted from forest to pasture, the dominant land cover will affect the duration and timing of the surface fluxes (Fleishcher et al., 2016) and this seems obvious on its own standing. However, DGVMs were not developed during the era of satellite XCO₂ observations, and so the main issue of trying to resolve the effect of large-scale changes in land use on both the long-term trend and seasonal cycle dynamics is not easily solved. But now that these data are available, perhaps a new approach is necessary to take advantage of these large-scale benchmarks.

The inclusion of LUC in the simulations, after including the contribution from fossil fuels and ocean, resulted in a combined long-term trend estimate which was too large, by 0.07 to 1.72 ppm yr⁻¹, compared to the long-term trend of GOSAT XCO₂ (2.16 ± 0.01 ppm yr⁻¹) (Supplementary Fig. S9). The GOSAT estimate is comparable to an independent estimate of the long-term trend of XCO₂ from SCIAMACHY for the 2000s (1.95 ± 0.05 ppm yr⁻¹; Schneising et al., 2014). If we assume that this study’s simulated long-term trends of fossil fuel fluxes (4.44 ± 0.008 ppm yr⁻¹) and those of the ocean (-0.66 ± 0.0006 ppm yr⁻¹) are better constrained than the trends from the land fluxes, then according to the GOSAT benchmark, the simulated land sink is too weak. Despite the possibility that these simulated LUC fluxes are too high, the DGVM versions applied in this study do not simulate a suite of land management processes (shifting cultivation, wood harvesting, pasture harvest, agriculture mgmt.) that have been shown to increase the annual LUC flux by 20-60% (Arneth et al., 2017), further pointing to a simulated land sink that is too weak. DGVM-based estimates of the terrestrial land sink have been compared against a residual term in the global carbon budget that is taken as the average flux over a decade (Le Quéré et al., 2018), but perhaps we are overlooking something here. The cumulative fluxes simulated by the models in this study (from 2002-2012) resulted in a long-term trend that is at odds with the satellite record, and it is unclear why. We must therefore attempt to reconcile biases in both the long-term trend and seasonal cycle dynamics if we are to use XCO₂, or other
integrated atmospheric measurements to constrain model dynamics, and not simply assess these patterns independently.

4.5 Caveats, limitations and ways forward

The \( \text{XCO}_2 \) gradient in amplitude is approximately half the gradient in amplitude of in-situ surface \( \text{CO}_2 \). The dampened \( \text{XCO}_2 \) gradient suggests the presence of strong meridional mixing, which complicates accurate attribution of model biases to any specific bioregion. In effect, the \( \text{XCO}_2 \) seasonal cycle is comprised of the fluxes from all regions to varying degrees (Olsen and Randerson, 2004; Sweeney et al., 2015; Lan et al., 2017). Given this, simulating the atmospheric transport of the surface fluxes from all regions at once would allow us to both, (a) obtain useable estimates of model bias and (b) to provide attribution to those biases. Indeed, the model biases were fully described, but only in terms of \( \text{XCO}_2 \), not in terms of terrestrial surface fluxes themselves. An approach for attribution of model bias in \( \text{XCO}_2 \) might be laid out similar to Liptak et al. (2017), wherein the surface fluxes from each region (by year) undergo independent atmospheric transport. In a framework similar to this study, such simulations might prove instrumental in determining the fractional contribution of each region’s fluxes the \( \text{XCO}_2 \) seasonal cycle characteristics while also providing better guidance for model development.

Model evaluations also showed that few models have low bias in all seasonal cycle metrics of amplitude, period, and phasing of simulated \( \text{XCO}_2 \). An inherent requirement for reproducing the \( \text{XCO}_2 \) signal is that the land-to-atmosphere fluxes are reasonable in magnitude, duration and timing in all land regions, or at the very least, in land regions with large vegetative areas that might disproportionately dominate the signal. Even though such requirement may be necessary to simulate the amplitude asymmetries, this is an extreme level of proficiency that, simply, the models do not currently exhibit.

Lastly, the relative contribution of land, ocean and fossil fuel fluxes to the seasonal cycle differs by region, latitude, and time period (Randerson et al., 1997). This poses some concern because fossil fuel and cement fluxes are considered to have low uncertainty, but they may be biased too high in some regions (Saeki and Patra 2017), affecting our interpretation of the contribution of simulated land fluxes to the seasonal cycle amplitudes, especially if the fossil fuel seasonal cycle signal is additive to (or offsets) the signal from the land fluxes. Other land uncertainties were not addressed in this study as it was not our intent to determine which DGVM had zero bias. Instead, we sought to extract unique patterns in the observed signals so that they may inform model development and subsequent evaluations in the future. Model improvements in their representation of important land processes such as forest demography, wetland and permafrost dynamics, agriculture and land management, and a greater diversity of functional plant diversity are all on the horizon (Pugh et al., 2016; Fisher et al., 2018) and may further improve simulated atmospheric signals. The patterns in \( \text{XCO}_2 \) seasonal cycles are emergent from surface fluxes over the globe, and we foresee that a segment-based analysis of atmospheric seasonal cycles as a way to extract emergent patterns in the reference data to help guide future development and an improved understanding of the terrestrial biosphere.

Acknowledgements
We thank Ehret and Zehe (2011) for their initial foray into alternative approaches to automate pattern matching in time series, which inspired this study. We thank the TRENDY Version 2 DGVM modelling community for their extensive efforts in continuing to advance model representation and making simulation data freely available. We acknowledge the developers at NOAA ESRL that have maintained the C program of the ccgcrv algorithm and made it freely available. LC was supported by a National Aeronautics and Space Administration Earth and Space Science Fellowship (NASA ESSF 2016-2019). PKP acknowledges support from the Tougou (Theme B) project of the Ministry of Education, Culture, Sports, Science and Technology.

Author Contribution

LC, BP, and PKP conceived of the study. PKP conducted the atmospheric simulations. LC prepared and analyzed simulated and satellite data. LC developed the code for the segmentation algorithm. LC prepared the manuscript with contributions from all co-authors.

Data Availability

Data used in the analysis and code for the segmentation algorithm is freely-available from the GitHub repository <https://github.com/lcalle/segmentTS>. The permanent version of the algorithm is archived and freely available at the Dryad Digital Repository <doi:10.5061/dryad.vk8ms2>.

References


Bonan, G. B.: Forests and climate change – forcings, feedbacks, and the climate benefits of forests. Science, 320,


Table 1. Terrestrial ecosystem models from the TRENDY v.2 model inter-comparison used to simulate terrestrial Net Ecosystem Exchange.

<table>
<thead>
<tr>
<th>Model</th>
<th>Abbrev.</th>
<th>Spatial Resolution</th>
<th>Land Surface Model</th>
<th>Fire Simulation</th>
<th>C-N coupled cycle</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>Community Land Model v.4.5</td>
<td>CLM</td>
<td>2.5 X 2.5</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Lawrence et al. (2011)</td>
</tr>
<tr>
<td>Lund-Potsdam-Jena</td>
<td>LPJ</td>
<td>0.5 X 0.5</td>
<td>No</td>
<td>Yes</td>
<td>No</td>
<td>Sitch et al. (2003)</td>
</tr>
<tr>
<td>Land-surface Processes and exchanges</td>
<td>LPX</td>
<td>1.0 X 1.0</td>
<td>No</td>
<td>Yes</td>
<td>Yes</td>
<td>Prentice et al. (2011)</td>
</tr>
<tr>
<td>ORganizing Carbon and Hydrology in Dynamic EcosystEms</td>
<td>ORCHIDEE</td>
<td>3.74 X 2.5</td>
<td>Yes</td>
<td>Yes</td>
<td>No</td>
<td>Krinner et al. (2005)</td>
</tr>
<tr>
<td>ORCHIDEE with coupled C-N cycling</td>
<td>OCN</td>
<td>1.0 X 1.0</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Zaehle and Friend (2010)</td>
</tr>
<tr>
<td>Vegetation Integrative SImulator for Trace gases</td>
<td>VISIT</td>
<td>0.5 X 0.5</td>
<td>No</td>
<td>Yes</td>
<td>Yes</td>
<td>Kato et al. (2013)</td>
</tr>
</tbody>
</table>
Table 2. Signal characteristics for Rise and Fall segments of the GOSAT-derived XCO$_2$ seasonal cycles (2009-2012) by TransCom region. The timeframe of one Rise plus one Fall segment approximately equates to one year. North America Boreal and South America Tropical regions were excluded for lack of observations to derive signals for Rise or Fall segments.

<table>
<thead>
<tr>
<th>Region</th>
<th>Segment</th>
<th>Period (days)</th>
<th>Amplitude (ppm)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Fall</td>
<td>Rise</td>
</tr>
<tr>
<td>Africa Northern</td>
<td>1,2</td>
<td>118</td>
<td>241</td>
</tr>
<tr>
<td></td>
<td>3,4</td>
<td>130</td>
<td>229</td>
</tr>
<tr>
<td></td>
<td>5,6</td>
<td>135</td>
<td>232</td>
</tr>
<tr>
<td></td>
<td>7</td>
<td>135</td>
<td>NA</td>
</tr>
<tr>
<td>Africa Southern</td>
<td>1,2</td>
<td>174</td>
<td>216</td>
</tr>
<tr>
<td></td>
<td>3,4</td>
<td>131</td>
<td>131</td>
</tr>
<tr>
<td></td>
<td>5,6</td>
<td>218</td>
<td>147</td>
</tr>
<tr>
<td>Asia Tropical</td>
<td>1,2</td>
<td>NA</td>
<td>194</td>
</tr>
<tr>
<td></td>
<td>3,4</td>
<td>NA</td>
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<td></td>
<td>5,6</td>
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<td>190</td>
</tr>
<tr>
<td>Australia</td>
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<td>140</td>
<td>225</td>
</tr>
<tr>
<td></td>
<td>3,4</td>
<td>136</td>
<td>209</td>
</tr>
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<td></td>
<td>5,6</td>
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<td>228</td>
</tr>
<tr>
<td>Europe*</td>
<td>2,1</td>
<td>115</td>
<td>236</td>
</tr>
<tr>
<td></td>
<td>3,4</td>
<td>131</td>
<td>239</td>
</tr>
<tr>
<td></td>
<td>5,6</td>
<td>132</td>
<td>244</td>
</tr>
<tr>
<td>Eurasia Temperate*</td>
<td>2,1</td>
<td>109</td>
<td>248</td>
</tr>
<tr>
<td></td>
<td>3,4</td>
<td>108</td>
<td>255</td>
</tr>
<tr>
<td></td>
<td>5,6</td>
<td>118</td>
<td>253</td>
</tr>
<tr>
<td>Eurasia Boreal</td>
<td>1,2</td>
<td>102</td>
<td>NA</td>
</tr>
<tr>
<td></td>
<td>3,4</td>
<td>100</td>
<td>NA</td>
</tr>
<tr>
<td></td>
<td>5,6</td>
<td>104</td>
<td>NA</td>
</tr>
<tr>
<td>North America Temperate</td>
<td>1,2</td>
<td>129</td>
<td>235</td>
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<td></td>
<td>3,4</td>
<td>126</td>
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</tr>
<tr>
<td></td>
<td>7</td>
<td>129</td>
<td>NA</td>
</tr>
<tr>
<td>South America Temperate</td>
<td>1,2</td>
<td>232</td>
<td>91</td>
</tr>
<tr>
<td></td>
<td>3,4</td>
<td>238</td>
<td>137</td>
</tr>
<tr>
<td></td>
<td>5,6</td>
<td>234</td>
<td>154</td>
</tr>
</tbody>
</table>

* the first differentiable segment is a Rise segment, starting approximately ~100+ days after the first segment in other regions because the initial drawdown (Fall segment) in the region is a partial or incomplete segment.
Table 3. The interannual variation (IAV) in XCO₂ seasonal cycle metrics, presented as the relative standard deviation (i.e., RSD or coefficient of variation) and the LUCEffect, defined as the change in the XCO₂ seasonal cycle metrics when land-use change is included in simulations, relative to simulations with only natural vegetation. The values for IAV and LUCEffect presented below are first calculated for each region and segment type (Rise, Fall), and then averaged over all regions, and models (for LUCEffect). The values for the phasing metrics (day of year, ‘DOY’) are calculated using the period as the divisor.

<table>
<thead>
<tr>
<th>metric</th>
<th>GOSAT IAV (%)</th>
<th>LUCEffect (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>amplitude</td>
<td>12.3</td>
<td>14.2</td>
</tr>
<tr>
<td>period</td>
<td>14.5</td>
<td>7.5</td>
</tr>
<tr>
<td>DOYstart</td>
<td>9.3</td>
<td>6.5</td>
</tr>
<tr>
<td>DOYend</td>
<td>7.5</td>
<td>6.8</td>
</tr>
</tbody>
</table>
Figure 1. Conceptual diagram for the segmentation analysis. (A) Interannual variation in seasonal cycle amplitudes (vertical, solid colored lines) and periods (horizontal, dashed colored lines); such interannual variation may also differ among Rise and Fall segments. (B) A reference (black) and a modeled seasonal cycle (red) are compared using the Root Mean Squared Error (RMSE), which is taken as the difference in magnitude at the same exact time in reference and modeled seasonal cycles; in out-of-phase signals, the RMSE misrepresents bias; the segmentation approach matches segments in the reference and modeled seasonal cycles, Rise-to-Rise and Fall-to-Fall, so that the errors in magnitude and phase can be decomposed and directly represented (C).
Figure 2. TransCom region map.
Figure 3. Detrended XCO₂ seasonal cycles by TransCom region. Simulated seasonal cycles are the sum of transported fluxes from DGVM, Fossil Fuel and Ocean, but only the DGVM model name is listed.
Figure 4. Latitudinal variation in amplitude and period in Rise and Fall segments among TransCom regions, using the average latitude for each region. Linear regressions shown when significant ($p < 0.05$). Regression statistics and equation only given for GOSAT.
Figure 5. Latitudinal variation in the amplitude for detrended in-situ surface CO$_2$ samples. Data are the average of peak-trough amplitudes for 2005-2015, only including sites with a minimum of 5 years of data. Points are labeled according to the three-letter code of the sampling station. South Pole (spo), Mauna Loa (mlo), and Barrow Island (brw) are highlighted in red for reference as these sites are commonly referenced in literature. The latitudinal range in surface site CO$_2$ seasonal amplitudes (~19 ppm), is more than 2 times the latitudinal range in seasonal amplitudes of XCO$_2$. 

$R^2 = 0.90$  $F(1,45)=410.5$  $p < 0.001$

$log(CO_2 \text{ amp}) = 1.55 + 0.022^{*}\text{Latitude}$
Figure 6. Period asymmetries (A) and Amplitude asymmetries (B) in GOSAT XCO₂ seasonal cycles. The bars represent differences in amplitude or period for consecutive Fall (F) and Rise (R) segments, taking the Fall segment as reference. For example, if the time series follows the sequence F₁, R₁, F₂, R₂, F₃, R₃, (i.e., 3 seasonal cycles), then the difference between the first segment (F₁) and the second segment (R₂) is calculated as 'F₁-R₂'; a zero value would indicate that the metric (amplitude or period) were equal, whereas an asymmetry would be indicated by a positive (F₁ > R₂) or negative (F₁ < R₂) value. By definition, consecutive segments cannot be categorized as F-F or R-R. Asymmetry statistics are not traditional summaries, but nevertheless, they are characteristic and in some regions persistent patterns of the seasonal cycle that are undoubtedly influenced by biosphere activity.
Figure 7. Emergent correlations among biases for Rise (x-axes) and Fall (y-axes) segments model biases, using GOSAT XCO₂ as reference, for TransCom regions in the Northern Hemisphere (top row) and Southern Hemisphere (bottom row). Data points are the average bias by model (unique symbols, not shown) for a particular region. Data for the Eurasia Boreal and Asia Tropical regions were excluded for lack of data in both Rise and Fall segments. Diagonal black lines are the 1:1 correspondence lines, blue lines are significant linear correlations.
Figure 8. Land Use Change effect on amplitude, period, and day of year (DOY). The percentages were calculated from the difference in the metrics between simulations (S3-S2), scaled relative to amplitude and period of Rise and Fall segments for each region and model; DOY was scaled against the period.