Dear teacher:

Thank you very much for your guidance and advice. We carefully read your suggestions, and revised the manuscript in accordance with your comments.

1. The reviewer’s comment: The biggest concerns of mine is the sounding time for RS is 2000LT, which is roughly 6 hours before the CALIPSO nighttime overpass at Wuhan. The inter-comparison of BLH between CALIPSO and RS (Fig. 9) seems flawed. I guess that the authors hypothesize the PBL does not vary considerable over time during nighttime. At the very least, however, the authors should discuss this issue in detail.

The authors’ Answer: Thank you very much for your suggestion and guidance. As your said, due to the time of RS is not matched with the time of CALIPSO, the inter-comparison of BLH between CALIPSO and RS was unreasonable. Another reviewer also pointed out this issue and suggested we delete this comparison. Therefore, we delete the inter-comparison of BLH between CALIPSO and RS to avoid misleading readers. In addition, we increased the inter-comparison of BLH between CALIPSO and Lidar. The horizontal smoothing numbers of 1, 3, 6, 9, 12, and 15 (i.e., 1/3, 1, 2, 3, 4, and 5km in the along-track direction) are add to test the GDM algorithm. It can be seen in P, line (Fig.9).

2. The reviewer’s comment: In section 2 or section 3: Clarification for the averaging scheme for CALIPSO profiles by taking various horizontal smoothing number (i.e., 1, 3, 15 and 30) should be added. Also, to make the results more robust, the horizontal smoothing numbers of 1, 3, 6, 9, 12, 15, 18 and 30 (i.e., 1/3, 1, 2, 3, 4, 5, 6 and 10km in the along-track direction) are suggested to take. As a result, Fig. 9 can be expanded to take into account more sensitive results.

The authors’ Answer: Thank you very much for your suggestion and guidance. Due to the section 3 was used to describe the process of the GDM algorithm, we did not add
the various horizontal smoothing number (i.e., 1, 3, 15 and 30). According to your suggestion, the horizontal smoothing numbers of 1, 3, 6, 9, 12, and 15 (i.e., 1/3, 1, 2, 3, 4, and 5km in the along-track direction) are add to test the GDM algorithm. The new Fig.9 was shown below. Due to the correlation coefficient tends to be stable when the horizontal smoothing numbers was 12 and 15. So we did not analyze the comparison results when the horizontal smoothing numbers was 18 and 30.

![Graphs showing correlation coefficients between BLH derived from CALIPSO and ground-based Lidar under different horizontal smoothing numbers.](image)

The modification can be seen in the P6, line37-40 and P7, line 1-6. “Fig. 9 show the correlation coefficients between the BLH derived from CALIPSO and ground-based Lidar under the horizontal smoothing numbers of 1, 3, 6, 9, 12 and 15. The red and blue points represent the BLH calculated by GDM algorithm and MSD method, respectively. Figs. 9a, 9b and 9c show the comparison of BLH between CALIPSO and Lidar under the horizontal smoothing number of 1, 3 and 6. The correlation coefficients between the BLH derived by GDM algorithm and ground-based Lidar were 0.12, 0.14 and 0.47, respectively. Meanwhile, the correlation coefficients between the BLH derived by MSD method and ground-based Lidar were 0.1, 0.27 and 0.33. Figs. 9d, 9e and 9f show the comparison of BLH between CALIPSO and Lidar under the horizontal smoothing number of 9, 12 and 15. The correlation coefficients between the BLH derived by GDM algorithm and Lidar measurements were both 0.72, and the correlation coefficients between the BLH derived by MSD method and Lidar measurements were 0.54, 0.62 and 0.7, respectively.”
3. The reviewer’s comment: Page 1 Line 17-24: It will be better to move “The algorithm provided a reliable result when the horizontal smoothing number was greater than 5.” Before “This finding indicated…”. In addition, what is the logics for the threshold (i.e., 5) of horizontal smooth number claimed here, since you only analyzed the results by assuming “1, 3, 15 and 30” instead of “5”. From my understanding, Figs. 7 and 9 are not enough to draw this conclusion, and thus necessary clarification will be necessary.

The authors’ Answer: Thank you very much for your suggestion and guidance. According to your suggestion, we move the sentence to the specified location. In addition, we did more experiments and reanalyzed Fig.9. Based on the new results, the GDM algorithm can provide a reliable result when the horizontal smoothing number was greater than 9. Therefore, we modified the descriptions in the P1, line 23-25. “The algorithm provided a reliable result when the horizontal smoothing number was greater than 9. This finding indicated that the proposed algorithm can be applied to the CALIPSO satellite data with 3 and 5 km horizontal resolution.”

4. The reviewer’s comment: Page 1 Line 28-35: The literature review seems in disorder, which can be improved only be rewriting. For example, the authors emphasized twice the role of BLH in environmental health, but I did not find any references supporting it. On top of this issue, the role of PBL is well recognized to be associated with aerosol pollution, which should be mentioned here. Towards this end, the review paper by Li et al, 2017 can be cited here.

The authors’ Answer: Thank you very much for your suggestion and guidance. According to your suggestion, we rewrite the literature review in the P1, line 30-35. Moreover, the review paper by Li et al, 2017 was add in P1, Line 35. “Therefore, the boundary layer height (BLH) is essential to atmospheric aerosol pollution and must be accurately and continuously monitored (Li et al. 2017).” “Li, Z., Guo, J., Ding, A., Liao, H., Liu, J., Sun, Y., … & Zhu, B. (2017). Aerosol and boundary-layer interactions and impact on air quality. National Science Review, 4(6), 810-833.”
5. The reviewer’s comment: Page 2 Line 2: The acronym for “RS” refers to radiosonde? Given its first appearance in this manuscript, its full name should be spelled here.

The authors’ Answer: Thank you very much for your suggestion and guidance. In here, the RS refers to radiosonde. According to your suggestion, its full name was given in the P2, line 3.

6. The reviewer’s comment: Page 2 Line 7: …is usually TOO sparse...

The authors’ Answer: Thank you very much for your suggestion and guidance. According to your suggestion, we add the “too” in the P2, line 8. “Moreover, the spatial coverage of RS sites is usually too sparse to capture BLH spatial variability.”

7. The reviewer’s comment: Page 2 Line 10: ...can CONTINUOUSLY detect...

The authors’ Answer: Thank you very much for your suggestion and guidance. According to your suggestion, we add the “continuously” in the P2, line 11. “Lidar systems can continuously detect the BLH from the aerosol vertical profile.”

8. The reviewer’s comment: Page 2 Line 28: Guo et al. 2016 only focuses on the BLH retrieval from radiosonde in China rather than that from satellite measurements. This citation can be replaced with Zhang et al. 2016. Accordingly, Guo et al. 2016a can be considered to move to Page Line 7 “(Seibert et al. 2000; Sawyer et al. 2013; Guo et al., 2016a)”

The authors’ Answer: Thank you very much for your suggestion and guidance. According to your suggestion, this citation was replaced with Zhang et al. 2016. Moreover, Guo et al. 2016a was moved to P2, Line 1. “(Seibert et al. 2000; Sawyer et al. 2013; Guo et al. 2016a)”

9. The reviewer’s comment: Page 3 line 9: Liu et al. 2018a is missing in references. The authors can consider citing the following reference here:

10. The reviewer’s comment: Page 3 Line 12: not completely coincide WITH ground-based Lidar station? How about the distance between CALIPSO track and radiosonde site? The track of CALIPSO shown in Fig.1 should be for the nighttime, which deserves clarification.

The authors’ Answer: Thank you very much for your suggestion and guidance. About the matching principles of ground-based Lidar and CALIPSO, we have explained it in two aspects. First, the distance between CALIPSO and ground-based Lidar stations is within 50 km. Moreover, the ground-based Lidar data were obtained within 30 min of CALIPSO overpass times. According to your suggestion, we add the descriptions in in the P3, line “7”. “About matching principles of ground-based and space-borne Lidar, the distance between CALIPSO and ground-based Lidar stations is within 50 km. Meanwhile, the ground-based Lidar data were obtained within 30 min of CALIPSO overpass times.”

11. The reviewer’s comment: Page 3 Line 29:Necessary justification is required for the authors only applying nighttime CALIPSO measurements to estimate BLHs. One reason is that there is higher SNR in nighttime relative to daytime SNR (Winker et al. 2009; Guo et al., 2016b).

The authors’ Answer: Thank you very much for your suggestion and guidance. As your said, there is higher SNR in nighttime relative to daytime SNR. According to your suggestion, we add some descriptions in the P3, line 28-29. “Due to the nighttime data have a higher SNR relative to daytime data (Winker et al. 2009; Guo et al., 2016b).”

Many grammatical or typographical errors have been revised.
All the lines and pages indicated above are in the revised manuscript. Thank you for the kind advice.

Sincerely

yours, Boming Liu
Dear teacher2:

Thank you very much for your guidance and advice. We carefully read your suggestions, and revised the manuscript in accordance with your comments.

1. The reviewer’s comment: In the noise removal phase, how much points were removed in the end? If it is 100 data points, 60 are removed at once and only 40 valid points remain. Can the results be trusted? The authors should add some quality control, such as removing 10 or less, the best quality, 30 are not credible, etc. I did not see the description in the paper.

   The authors’ Answer: Thank you very much for your suggestion and guidance. In the last review comment reply, we have explained this point. In fact, the noise point is not eliminated under the noise removal phase, but is judged as a cluster which same with the neighboring particles. In this way, it won't lose height information. Meanwhile, the class misjudgment caused by noise point is corrected. Therefore, in the noise removal phase, it does not need to add quality control. But this point did not explain clearly in the manuscript. To avoid misleading readers, we add some descriptions in the P5 line 3. “According to the noise removal principle, the category of noise point was judged as a cluster which same with the neighboring particles.”

2. The reviewer’s comment: Figure 9, this study shows the comparison between the BLHs from CALIPSO at 0210LT and RS at 2000LT. But the BLH has strong diurnal variances, this comparison is unreasonable. I suggest that the author change to RS data at night, or delete this comparison.

   The authors’ Answer: Thank you very much for your suggestion and guidance. As your said, due to the time mismatch, the comparison between the BLHs from CALIPSO at 0210LT and RS at 2000LT was unreasonable. So according to your suggestion, we delete the comparison between CALIPSO and RS. In addition, to make the results more robust, more CALIPSO profiles by different horizontal smoothing number was added
in Fig.9. The horizontal smoothing numbers of 1, 3, 6, 9, 12, and 15 (i.e., 1/3, 1, 2, 3, 4, and 5km in the along-track direction) are add to test the GDM algorithm, as the following picture shown.

3. The reviewer’s comment: The author claimed that they use nighttime data of CALIPSO and Lidar (0210LT), but the nighttime BLHs at 0210LT from CALIPSO and Lidar looks a little high. It may be due to the that the Lidar system regarded the top of residual layer as the BLH at night. So, the authors should explain it clearly.

The authors’ Answer: Thank you very much for your suggestion and guidance. As your said, the structure of boundary layer is divided into a stable layer and a residual layer in the nighttime. The Lidar system obtained the boundary layer height based on the aerosol scattering profile. If the aerosol loading in the residual layer is large, the top of residual layer would be identified as the boundary layer height by Lidar. After our experiment, we found that the CALIPSO system was hard to identify the top of stable layer in nighttime. Therefore, the top of residual layer was defined as the boundary layer height in CALIPSO and Lidar system. It leads to that the BLHs from CALIPSO and Lidar are all a little high. About this question, more details would be added in the 3.2 section (Error analysis) to avoid misleading readers. Meanwhile, overcoming the effect of the residual layer on CALIPSO is our future work. According to your
suggestion, we add some descriptions in the P5, line 23-24. “In addition, due to the effect of the nocturnal residual layer, the top of residual layer would be identified as the BLH by Lidar system in some cases.”

4. The reviewer’s comment: About data collection time, the authors claimed that the number of residual CALIPSO data over Wuhan area was 49 after removing the cases with cloud and dust. The author should describe the continuous observation period for Lidar and RS, and indicate that how many cases have collected.

The authors’ Answer: Thank you very much for your suggestion and guidance. I am very sorry that we did not describe clearly the time of data. The experimental time was from January 2013 to December 2017. During this time, the total number of CALIPSO crossing Wuhan were 93. After removing the cloud cases, there were 49 valid samples. Moreover, the ground-based Lidar and RS data were collected at the same time. The number of the ground-based Lidar and RS data matching CALIPSO data were 21 and 49, respectively. According to your suggestion, the descriptions about continuous observation period for Lidar and CALIPSO were added in the P3, line 19-21 and 30-33. “The Lidar data was collected from January 2013 to December 2017. After matching the CALIPSO data, the valid number of the ground-based Lidar data were 21 cases.” “The data collection time was from January 2013 to December 2017. During this time, the total number of CALIPSO crossing Wuhan were 93. After removing the cloud cases, there were 49 valid samples.”

5. The reviewer’s comment: The principle that satellite data matches the ground station did not appear in the paper. The authors should clarify the match distance range and time range between the CALIPSO and the ground lidar (RS). Because the returns trajectory of CALIPSO is not completely coincident. It is necessary to point out the match distance range and time range.
The authors’ Answer: Thank you very much for your suggestion and guidance. About the matching principles of ground-based Lidar and CALIPSO, we have explained it in two aspects. First, the distance between CALIPSO and ground-based Lidar stations is within 50 km. Moreover, the ground-based Lidar data were obtained within 30 min of CALIPSO overpass times. According to your suggestion, we add the descriptions in in the P3, line 7-10. “About matching principles of ground-based and space-borne Lidar, the distance between CALIPSO and ground-based Lidar stations is within 50 km. Meanwhile, the ground-based Lidar data were obtained within 30 min of CALIPSO overpass times.”

6. The reviewer’s comment: P2, Line 2: RS is the abbreviation. It should give the full name when it first appears.

The authors’ Answer: Thank you very much for your suggestion and guidance. In here, the RS refers to radiosonde. According to your suggestion, its full name was given in the P2, line 3.

7. The reviewer’s comment: The English of the paper should be improved.

The authors’ Answer: The authors’ Answer: Thank you very much for your patience and guidance. I am very sorry for my poor English expression. To improve the poor language, I have get a professional language editing service to correct the language.

Many grammatical or typographical errors have been revised.

All the lines and pages indicated above are in the revised manuscript. Thank you for the kind advice.

Sincerely

yours, Boming Liu
Graphics Algorithm for Deriving Atmospheric Boundary

Layer Heights from CALIPSO Data

Boming Liu1, Yingying Ma1,2*, Jiqiao Liu3*, Wei Gong1,2, Wei Wang4 and Ming Zhang1

1 State Key Laboratory of Information Engineering in Surveying, Mapping and Remote Sensing (LIESMARS), Wuhan University, Wuhan 430079, China
2 Collaborative Innovation Centre for Geospatial Technology, Wuhan 430079, China
3 Shanghai Institute of Optics and Fine Mechanics, Chinese Academy of Sciences, Shanghai, 201800
4 School of Geoscience and Info-Physics, Central South University, Changsha, 410083
* Correspondence: yym863@whu.edu.cn and liujiqiao@siom.ac.cn

Abstract: The atmospheric boundary layer is an important atmospheric feature that affects environmental health and weather forecasting. In this study, we proposed a graphics algorithm for the derivation of atmospheric boundary layer height (BLH) from the Cloud-Aerosol Lidar and Infrared Pathfinder Satellite Observations (CALIPSO) data. Owing to the differences in scattering intensity between molecular and aerosol particles, the total attenuated backscatter coefficient 532 and attenuated backscatter coefficient 1064 were used simultaneously for BLH detection. The proposed algorithm transformed the gradient solution into graphics distribution solution to overcome the effects of large noise and improve the horizontal resolution. This method was then tested with real signals under different horizontal smoothing numbers (1, 3, 15 and 30). The algorithm provided a reliable result when the horizontal smoothing number was greater than 5. Finally, the results of BLH obtained by CALIPSO data were compared with the results retrieved by the ground-based Lidar and radiosonde (RS) measurements. Under the horizontal smoothing number of 15, 9, 12 and 39, the correlation coefficients between the BLH derived by the proposed algorithm and ground-based Lidar were both 0.72. Under the horizontal smoothing number of 6, 3 and 1, the correlation coefficients between the BLH derived by GDM algorithm and ground-based Lidar were 0.47, 0.14 and 0.12, respectively, 0.72, 0.72 and 0.14, respectively, and those between the BLH derived by the proposed algorithm and radiosonde measurements were 0.59, 0.59 and 0.07. When the horizontal smoothing number was large (15, 12 and 9), the CALIPSO BLH derived by the proposed method demonstrated a good correlation with ground-based Lidar and RS. The algorithm provided a reliable result when the horizontal smoothing number was greater than 9. This finding indicated that the proposed algorithm can be applied to the CALIPSO satellite data with 3 and 5 km horizontal resolution.

Keywords: Aerosol; Lidar; Radiosondes; Boundary layer height; CALIPSO

1. Introduction

The atmospheric boundary layer is the layer of the Earth’s surface atmosphere which is closely related to human activities (Bonin et al. 2013; Reuder et al. 2009; Flamant et al. 1997). It plays a crucial role in regional environmental pollution health and is important in weather forecasting model (Liu et al. 2018a; Leventidou et al. 2013). Meanwhile, the heating process of solar radiation for the surface are also achieved through boundary layer dynamics (Yang et al, 2013). Furthermore, atmospheric activity in the boundary layer affects the propagation of
cloud nuclei and pollutant dispersion (Lange et al., 2014). Therefore, the boundary layer height (BLH) is essential to environmental health and human activity, and atmospheric aerosol pollution must be accurately and continuously monitored (Li et al., 2017).

Various detection technologies are currently used for BLH observation, including optical (Lidar, ceilometers) and electromagnetic (radiosondes, Doppler radar) remote sensing (Seibert et al., 2000; Sawyer et al., 2013; Guo et al., 2016a). The radiosonde (RS) was the most common measurement instrument used for detecting the vertical profiles of meteorological parameters (Hennemuth et al., 2006). The BLH can be derived from the thermodynamic profiles measured by the RS (Holzworth et al., 1964). However, the observation time of RS is discontinuous. That is, RS is typically launched routinely twice a day or from four to eight times daily during field experiments (Holzworth et al., 1967). Moreover, the spatial coverage of RS sites is usually too sparse to capture BLH spatial variability. The ground-based Lidar system is an active remote sensing equipment, which can provide aerosol extinction profile with a high spatial resolution (Huang et al., 2010). This system has been widely employed for the study of the optical and physical properties of atmospheric aerosols (Melfi et al., 1985). Lidar systems can continuously detect the BLH from the aerosol vertical profile (Li et al., 2017). However, owing to expensive price and maintenance costs, the spatial coverage of ground-based Lidar remains poor.

The CALIPSO is the only space-borne Lidar in operation in the world (Winker et al., 2007, 2009; Liu et al., 2015). CALIPSO provides the vertical distributions of clouds and aerosols with high vertical resolution and offers a significant potential for the estimation of global BLHs from space (Mamouri et al., 2009). The major methods of deriving BLH from CALIPSO data include the wavelet covariance transform (WCT) and maximum standard deviation (MSD) methods (McGrath-Spangler et al., 2012; Brooks et al., 2003). Through these methods, the BLH can be determined by using the vertical profile of aerosol. The MSD method determines the BLH from CALIPSO as the lowest occurrence of a local maximum in the standard deviation of backscatter profile collocated with a maximum in the backscatter itself (Jordan et al., 2010). The WCT method searches the local maximum with a coherent scale and defines the height of maximum value as BLH (Davis et al., 2000). These methods have been widely used for BLH derivation. However, due to the low signal-to-noise ratio (SNR) of CALIPSO data, these methods can be applied to the real signals only when the horizontal smoothing number is large. The CALIPSO provided the total attenuated backscatter coefficient with a horizontal resolution of 1/3 km (Winker et al., 2009). In particular, the signals reaching the CALIPSO Lidar from low altitudes can possess significant noise due to the long travel distance of attenuated backscatter. The large noise conceals the gradient value at the top of boundary layer when the horizontal smoothing number was small. Therefore, obtaining the BLH by using the WCT and MSD methods is difficult. Therefore, a horizontal smoothing method is necessary for improving the SNR of satellite data (Guo et al., 2016). Zhang et al. (2016) obtained a 5 km horizontal smoothing profile by averaging 15 CALIOP vertical profiles to retrieve BLH results. Su et al. (2017) retrieved BLHs from a 7 km horizontal smoothing (horizontal smoothing number = 21) CALIPSO data to minimise the influence of outliers. In this manner, the noise of satellite data can be effectively restrained, and the BLH results can be obtained from CALIPSO. However, this method sacrifices the horizontal resolution of CALIPSO detection.

In this research, we proposed a graphics distribution method (GDM) for deriving the BLH from CALIPSO data and preventing significant reduction of horizontal resolution. The total attenuated backscatter coefficient 532 (TAB532) and attenuated backscatter coefficient 1064 (AB1064) were used for the construction of two-dimensional graphics distribution, which was used for BLH derivation. The GDM algorithm was then tested with real signals under different horizontal smoothing numbers. Finally, the results of BLH obtained by CALIPSO data were
compared with those retrieved by the ground-based Lidar and RS measurements during January 2013 to December 2017.

2. Materials

2.1 Study Area

The CALIPSO, ground-based Lidar, and RS were used for calculation of BLHs over Wuhan, a megacity close to the Han and the Yangtze River. Wuhan is one of the most densely populated and industrialised region over central China (Liu et al. 2018b; Zhang et al. 2017). In the Wuhan area, the ground-based Lidar stations are located at the State Key Laboratory of Information Engineering in Surveying, Mapping and Remote Sensing, Wuhan University (30°32’N, 114°08’E) (Liu et al. 2017). The RS measurements station (30°37’N, 114°08’E) operated by the Wuhan meteorological bureau routinely launches RS at 8:00 and 20:00 local time (LT) daily (Liu et al. 2018a). Fig. 1 shows the geographic distributions of the ground-based Lidar and RS station. The black point and blue triangle represent the ground-based Lidar and RS station, respectively. The black line represents the track of CALIPSO satellite. About matching principles of ground-based and space-borne Lidar, The trajectory of CALIPSO does not completely coincide, but the distance between CALIPSO and ground-based Lidar stations is within 50 km. Meanwhile, the ground-based Lidar data were obtained within 30 min of CALIPSO overpass times.

2.2 Ground-based Lidar Data

A ground-based Lidar system was used for the detection of the atmospheric vertical profiles in Wuhan (Wei et al. 2015). The Lidar system uses a pulsed Nd: YAG laser with 532 nm wavelength. The pulse rate of the laser was 20 Hz, and the laser energy was 150 mJ. The vertical resolution of the system was 3.75 m, and the acquisition frequency of the system was 20 Hz. Additional details of this Lidar system can be found in previous studies. Given that the Lidar signal is susceptible to the noise of background light during daytime, the Lidar system was employed at night from 19:00 to 07:00 local time. The ideal profile fitting method proposed by Steyn et al. (1999) is an effective method for delineating stable boundary layers. As this method can be successfully used for obtaining the BLH in ground-based Lidar research, an ideal profile fitting method was used. The Lidar data was collected from January 2013 to December 2017. After matching the CALIPSO data, the valid number of the ground-based Lidar data were 21 cases.

2.3 CALIPSO Data

The CALIOP satellite is the first space-borne Lidar optimised for aerosol and cloud profiling, which has 532 nm channel (parallel and perpendicular polarisation) and 1064 nm channel (Liu et al. 2009). This satellite can provide the total attenuated backscatter coefficient 532 and attenuated backscatter coefficient 1064 with a horizontal resolution of 1/3 km and vertical resolution of 30 m. Attenuated backscatter data (Level 1B) were used for testing the proposed algorithm. The cycle time of CALIPSO across the central China region is 16 days, and the crossing time of the satellite in Wuhan is 13:10 and 02:10 local time. Due to the nighttime data have a higher SNR relative to daytime data (Winker et al., 2009; Guo et al., 2016b). The nighttime data were employed for this analysis for the matching of the ground-based data, and cases with cloud and dust were removed in this study. The data collection time was from January 2013 to December 2017. During this time, the total number of CALIPSO crossing Wuhan were 93. After removing the cloud cases, there were 49 valid samples.
2.4 Radiosonde Measurements Data

The RS data were provided by the Bureau of Meteorology at Wuhan site, which is 23 m above sea level and 30 km northwest from the Lidar site. The RS was launched twice a day at 8:00 (LT) and 20:00 (LT). The RS data from 20:00 (LT) were selected to calculate the BLH and match the satellite data (Pal et al. 2013). The vertical profiles of the mean horizontal wind speed and potential temperature were used to determine the BLH following the method described in Liu and Liang because the construction of nighttime boundary layer is complicated (Liu et al. 2010). Moreover, due to the mismatched time of RS data, the BLH estimated from RS measurements data cannot be regarded as ‘truth’; thus, the estimated BLH is jointly used with the ground-based Lidar for validating CALIPSO results.

3. Methodology

3.1. Method

Previous studies reported that the different particles are distributed in different vertical heights (Liu et al. 2018c; Sugimoto et al. 2002). Most of the particles above the boundary layer are molecular particles, and the particles below the boundary layer are mainly aerosol particles, as shown in Figs. 2a and 2c, respectively. Therefore, we proposed a dual-wavelength algorithm that determines BLH on the basis of two-dimensional graphical distribution. The total attenuated backscatter coefficient 532 (TAB532) and attenuated backscatter coefficient 1064 (AB1064) were used to construct the two-dimensional graphical distribution. The specific steps are as follows:

Firstly, the TAB532 and AB1064 were employed for the construction of the sample sequence X(z). As shown in Figs. 2b and 2d, the TAB532 and AB1064 represent the aerosol vertical profile at 532 and 1064 wavelength measured by CALIPSO, respectively. The X(z) can be expressed as:

\[
X(z) = [TAB_{532}(z), AB_{1064}(z)]
\]  

where \(z\) stands for the altitude of sample points; \(X(z)\) represents the coordinates of the sample point at the altitude of \(z\); \(TAB_{532}(z)\) and \(AB_{1064}(z)\) represent the total attenuated backscatter (532 nm) and attenuated backscatter (1064 nm) value of the sample point at the altitude of \(z\), respectively.

The sample sequence \(X(z)\) is shown in Fig. 3a. The colour bar is the altitude of sample points. The figure shows that TAB532 and AB1064 of blue points (the particles below the boundary layer) were larger than those of the red points (the particles above the boundary layer). According to this two-dimensional distribution, the sample sequence \(X(z)\) can be divided into two categories.

The k-means method was used for the classification of the sample sequence. Two centroid points \((u_1, u_2)\) were randomly selected from the sample sequence. For each sample point of sample sequence \(X(z)\), the cluster \(C\) belonging to is calculated as follows:

\[
c(z) = \arg \min_j \|X(z) - u_j\|^2
\]

where \(C(z)\) represents the cluster of sample point at the altitude of \(z\), and \(u_j\) is the centroid of cluster \(j\) \((u_1\) or \(u_2)\). For each cluster \(j\), the centroid \(u_j\) is recalculated as follows:
Eqs. (3) and (4) are repeated until the centroids \((u_1 \text{ and } u_2)\) converge. The sample sequence is divided into two categories after the convergence. As shown in Fig. 3b, cluster; (blue points) indicates the aerosol particles below the boundary layer, and cluster, (red points) is the molecular particles above the boundary layer. Black cross represents centroid points. Meanwhile, the categories sequence \(f(z)\), which changes with height, can be obtained and expressed as:

\[
f(z) = \begin{cases} 
1, & z \in \text{cluster}_i \\
2, & z \in \text{cluster}_j
\end{cases}
\]

where \(f(z)\) is the category of sample point at the altitude of \(z\). The noise points would affect the classification results due to the large noise of satellite data. Therefore, the noise points on the categories sequence must be eliminated. The noise point was determined by comparing two points near the point. If the two points above and below this point belong to the same class, then this point should also belong to this category. The noise point can be filtered by:

\[
f(z) = f(z - m), \quad \text{if } f(z - m) = f(z + m)
\]

where \(m\) represents the multiple of the vertical resolution, and the different values can be selected at different noise levels. When the horizontal smoothing number is small and the signal noise is large, the value of \(m\) can be set as 2; and when the horizontal smoothing number is large, the value of \(m\) can be set as 1. According to the noise removal principle, the category of noise point was judged as a cluster which same with the neighbouring particles. Hence, the noise points were removed, and the new categories sequence \(F(z)\) was obtained as follows:

\[
F(z) = \begin{cases} 
1, & z > \text{BLH} \\
2, & z < \text{BLH}
\end{cases}
\]

where \(F(z)\) represents the category of the sample point at the altitude of \(z\). BLH indicates the BLH result. Fig. 3c shows the category sequence \(F(z)\), which contains the height information and shows evident variation at the top of boundary layer. Therefore, the maximum gradient of the categories sequence \(F(z)\) is the top point of boundary layer. The BLH can be calculated by searching the maximum gradient, which can be expressed as:

\[
\text{BLH} = \left[ df \left[ F(z) \right] \right]_{\text{max}}
\]

Following this process, the BLH was obtained based on the two-dimensional distribution of particles.

### 3.2. Error analysis

Fig. 4 shows the flowchart of the GDM algorithm. Four calculation steps are available: establishing the sample sequence, particle clustering, filtering noise points, and maximum gradient searching. The error of input parameters is the main factor affecting the accuracy of the algorithm because these steps are quantitative calculations. According to the official description, the uncertainty of backscatter coefficient was 20%–30% (Winker et al. 2009). The total attenuated backscatter at 532 nm wavelength and the attenuated backscatter at 1064 nm wavelength were measured from CALIPSO. Therefore, the error of input parameters was 20%–30%. The error
of the BLHs derived by the GDM algorithm is approximately 20%-30%. In addition, it need to note that this method cannot be applied to low cloud and dust cases, because the boundary of cloud or dust would be misclassified to BLH. In addition, due to the effect of the nocturnal residual layer, the top of residual layer would be identified as the BLH by Lidar system in some cases.

4. Results

The GDM algorithm was applied to the CALIPSO data acquired from January 2013 to December in 2017. After removing the cases with cloud and dust, the number of residual CALIPSO data over Wuhan area was 49. In addition, the results of BLH were compared with those retrieved by the ground-based Lidar and RS measurements.

4.1. Testing with real signals

Fig. 5 shows the case study of CALIPSO data with different horizontal smoothing numbers on 4 October 2013 over Wuhan area. Figs. 5a, 5b, 5c and 5d represent the vertical profile of TAB_{532} derived from CALIPSO profile with a horizontal smoothing number of 1, 3, 15 and 30, respectively, and their BLH result was 1020, 980, 980 and 980 m, respectively. Fig. 5a shows the vertical profile of TAB_{532} with a horizontal smoothing number of 1, in which the noise of satellite data was large. Such noise produced discrete sample sequence distribution. However, the category sequence and the BLH result (1010 m) can still be obtained. As shown in Figs. 5b, 5c and 5d, the noise of satellite data was reduced with the increase in horizontal smoothing number. Moreover, the vertical profile of TAB_{532} derived from CALIPSO profile was gradually becoming smooth. Such transformation resulted in significantly compact distribution of sample sequences (Fig. 5d), which were conducive to the classification of sample points. The categories sequence was easily obtained from the classification calculation, and the result of the BLH converged to 980 m. In this case, the GDM algorithm can obtain the BLH result under different horizontal smoothing numbers.

Fig. 6 shows the case study of CALIPSO data with different horizontal smoothing numbers on 12 February 2015 over Wuhan area. The BLH result of Figs. 6a, 6b, 6c and 6d were 532, 1280, 1370 and 1370 m, respectively. As shown in Fig. 6a, when the horizontal smoothing number was 1, the high noise of CALIPSO mixed together the sample points at different heights. In this condition, the categories sequence cannot accurately distinguish between molecular and aerosol particles. Therefore, an inaccurate BLH result was obtained under this condition. When the horizontal smoothing number was added to 3 (Fig. 6b), the distribution of sample sequences significantly improved, and the obtained BLH result was 1280 m. Figs. 5c and 5d show the vertical profile of TAB_{532} with the horizontal smoothing number of 15 and 30, respectively, in which the distribution of sample sequences gradually became compact. The result of the BLH converged to 1370 m. This result indicates that the GDM algorithm cannot be applied to the data with horizontal smoothing number of 1 in this case, but it can provide a relatively reliable result when the horizontal smoothing number was greater than 3.

The relationship between the horizontal smoothing number and BLH was investigated to determine the convergence of the BLH results. Fig. 7 shows the relationship between the horizontal smoothing number and BLH under different cases. Fig. 7a shows the case study on 4 October 2013. The result of the BLH converges to 980 m when the horizontal smoothing number was greater than 2. Fig. 7b shows the case study on 12 February 2015. The result of the BLH converged to 980 m when the horizontal smoothing number was greater than 4. These results indicate that the PDM algorithm was not applied to the satellite data when the horizontal smoothing number was
extremely small. However, this algorithm can provide a reliable result when the horizontal smoothing number is greater than 5.

4.2. Comparison with other algorithms

In this section, we compare the results of BLH obtained by CALIPSO data with those retrieved by the ground-based Lidar and RS measurements to verify the stability of the algorithm. The number of the ground-based Lidar and RS-data matching CALIPSO data were 21 and 49, respectively. The results of BLH calculated by the MSD method were used as a reference.

Figs. 8a and 8c show the total attenuated backscatter at 532 nm plot from CALIPSO on 7 October 2014 under the horizontal smoothing number 15 and 9, respectively. The black and blue line represent the BLH results calculated by GDM algorithm and MSD method, respectively. The red circle stands for the BLH result from ground-based Lidar. Fig. 8b shows the corresponding vertical profile of TAB532 derived from CALIPSO profile over Wuhan area under the horizontal smoothing number 15. The BLH results calculated by GDM algorithm, MSD method and ground-based Lidar were 1220, 980 and 1250 m, respectively. Fig. 8b shows the corresponding vertical profile of TAB532 under the horizontal smoothing number 9. The BLH results calculated by GDM algorithm, MSD method and ground-based Lidar were 1220, 770 and 1250 m, respectively.

Figs. 9a, 9b and 9c show the correlation coefficients between the BLH derived from CALIPSO and ground-based Lidar under the horizontal smoothing numbers of 15, 3, 6, 9, 12 and 15. The red and blue points represent the BLH calculated by GDM algorithm and MSD method, respectively. Figs. 9a, 9b and 9c show the comparison of BLH between CALIPSO and Lidar under the horizontal smoothing number of 1, 3 and 6. The correlation coefficients between the BLH derived by GDM algorithm and ground-based Lidar were 0.720.12, 0.720.14 and 0.140.47 under the horizontal smoothing number of 15, 9 and 3, respectively. Meanwhile, the correlation coefficients between the BLH derived by MSD method and ground-based Lidar were 0.20.1, 0.540.27 and 0.270.33. The correlation between BLH derived from RS measurements and CALIPSO is shown in Figs. 9d, 9e and 9f. show the comparison of BLH between CALIPSO and Lidar under the horizontal smoothing number of 15, 9 and 12, and the correlation coefficients between the BLH derived by GDM algorithm and RS measurementsLidar measurements were both 0.72, 0.59, 0.59 and 0.07, respectively, and the correlation coefficients between the BLH derived by MSD method and RS-Lidar measurements were 0.54, 0.420.62 and 0.430.7, respectively. These results indicate that the performance of GDM algorithm was similar to the MSD method when the horizontal smoothing number was large (15). When the horizontal smoothing number was 9, the performance of GDM algorithm was superior to the MSD method. Moreover, the GDM algorithm and MSD method show a poor performance when the horizontal smoothing number was small (3).

5. Discussion

The CALIPSO satellite is a powerful tool for monitoring the vertical distribution of clouds and aerosols, which offers a significant potential for the estimation of global BLHs from space (Winker et al. 2007, 2009). Moreover, a horizontal smoothing method was used to improve the SNR of satellite data due to its large noise (Guo et al. 2016; Zhang et al. 2016; Su et al. 2017). However, this method considerably sacrificed the horizontal resolution of CALIPSO detection. A graphics algorithm was proposed to determine the BLHs from CALIPSO data and overcome this problem.
The total attenuated backscatter coefficient 532 and attenuated backscatter coefficient 1064 were used to construct the two-dimensional graphics distribution, as shown in Fig. 3a. The extremum and negative points can be filtered through this graphics distribution. The sample sequence was then classified by the k-means method, and the categories sequence was obtained (Fig. 3b). When the horizontal smoothing number was different, the degree of noise was also different. When the noise was large, the noise point which was above the boundary layer and may be classified below the boundary layer, thereby significantly affecting the accuracy of categories sequence. Therefore, the noise points were removed again, and the new categories sequence was obtained (Fig. 3c). The BLH result can be determined from the new categories sequence by maximum gradient search (Fig. 3d). The advantage of the GDM algorithm is that this algorithm transforms the gradient solution into graphics distribution solution. The multiple gradient values in the backscatter coefficient profile can be understood as the extremely dispersed distribution of the particles. According to the graphic classification, the influence of noise gradient can be avoided, and a reliable BLH result can be obtained.

The test results of GDM algorithm are shown in Figs. 5, 6 and 7. These results indicate that the GDM algorithm can be applied to the satellite data when the horizontal smoothing number is small. However, when the horizontal smoothing number is below 5, the large noise affects the distribution of the sample sequence, and obtaining the BLH by graphic classification is difficult. Regarding the performance of algorithm, as shown in Figs. 8 and 9, the performance of the GDM algorithm was similar to that of the MSD algorithm when the horizontal smoothing number was large. This finding can be attributed to the noise of satellite data, which produced the evident gradient of aerosol concentration when effectively restrained by the horizontal smoothing method. Thus, both the algorithms can accurately detect the BLH. However, with the decrease in the number of horizontal smoothing, a difference was observed between the GDM and MSD algorithms with respect to performance. When horizontal smoothing number was small (9), the noise of satellite data was ineffectively controlled, thereby resulting in multiple gradients in the vertical direction. The MSD algorithm failed to obtain the effective BLH from the multiple gradient values. However, the GDM algorithm can still detect the BLH based on the graphics distribution, overcome the effect of multiple gradient values and accurately identify the BLH. Therefore, the GDM algorithm can deal well with the CALIPSO data with a small horizontal smoothing number.

6. Conclusions

We proposed a graphics algorithm to obtain the BLHs from CALIPSO data. The following four calculation steps were used: establishing the sample sequence, particle clustering, filtering noise points and maximum gradient searching. The TAB532 and AB1064 were used for the construction of the two-dimensional graphics distribution. Based on the graphics distribution of atmospheric particulate, the k-means method was used for the classification of the sample sequence and acquisition of the BLH. The algorithm was then applied to the real signals with different horizontal smoothing numbers for the evaluation of the algorithm’s performance. The results indicate that the performance of GDM algorithm was poor when the horizontal smoothing number was extremely small (such as 1 to 3), although it can provide a reliable result when the horizontal smoothing number was greater than 5. Finally, the results of BLH obtained by CALIPSO data were compared with those retrieved by the ground-based Lidar and RS measurements from January 2013 to December 2017. Notably, when the horizontal smoothing number was extremely large (above 15), the performance of the GDM algorithm was similar to that of the MSD method. It indicated that the 5 km horizontal resolution CALIPSO data (the horizontal smoothing number of 15) was suitable for both GDM and MSD method to derive the BLH. Moreover, the correlation coefficients between
the BLH derived by the GDM method and ground-based Lidar were superior to those between the BLH derived by the MSD method and ground-based Lidar when the horizontal smoothing number was 9. This finding indicates that the performance of the GDM algorithm is superior to that of the MSD method when the 3 km horizontal resolution CALIPSO data was used. Overall, the CALIPSO BLH derived by GDM method is reasonably consistent with ground-based Lidar and RS. The MSD algorithm can derive the BLH effectively from the 3 km and 5 km horizontal resolution CALIPSO data.

**Acknowledgments:** This work was supported by the National Key R&D Program of China (2017YFC0212600), and the Haze Program of the Wuhan Technological Bureau (2017CFB404), and the National Natural Science Foundation of China (Program No. 41127901 and No. 41627804).

**References**


Flamant, C., J. Pelon, and P. Flamant (1997), Lidar determination of the entrainment zone thickness at the top of the unstable marine atmospheric boundary layer, Boundary Layer Meteorol., 83(2), 247–284.


Liu, B., Ma, Y., Gong, W., Zhang, M., & Yang, J. (2018b). Study of continuous air pollution in winter over Wuhan based on ground-based and satellite observations. Atmospheric Pollution Research, 9(1), 156-165.


Sawyer, V., and Z. Li (2013), Detection, variations and intercomparison of the planetary boundary layer depth from radiosonde, lidar and infrared spectrometer, Atmos. Environ., 79, 518–528.


Figure 1. Geographic distributions of the ground-based Lidar and RS measurements station. The black point and blue triangle represent the ground-based Lidar and radiosonde measurements station, respectively. The black line represents the track of CALIPSO satellite.
Figure 2. (a) Total attenuated backscatter at 532 nm wavelength (TAB\textsubscript{532}) and (c) the attenuated backscatter at 1064 nm wavelength (AB\textsubscript{1064}) plot from CALIPSO on 7 October 2014. (b) and (c) indicate the corresponding vertical profile of TAB\textsubscript{532} and AB\textsubscript{1064} derived from CALIPSO profile over Wuhan area, respectively. The number of horizontal smoothing is 20.
Figure 3. Case study over Wuhan area on 7 October 2014. (a) Scatter plots of TAB532 and AB1064. The color bar shows the altitude of sample point. (b) Classification results. The red and blue point represent the cluster 1 and 2, respectively. The black fork represents the centroid of the cluster. (c) The sequence of category F(z). (d) The result of the case analysis. The orange circle represents the result of BLH.
Figure 4. Flowchart of the GDM algorithm. The red box indicated the four calculation steps.
Figure 5. Case study of CALIPSO data with different horizontal smoothing numbers on 4 October 2013 over Wuhan area. (a) average number = 1, (b) average number = 3, (c) average number = 15 and (d) average number = 30. The blue line represents the vertical profile of TAB$_{532}$ derived from CALIPSO data, the Black cross represents the centroid of the cluster and the orange horizontal line represents the BLH result.
Figure 6 Case study of CALIPSO data with different horizontal smoothing numbers on 12 February 2015 over Wuhan area. (a) average number = 1, (b) average number = 3, (c) average number = 15 and (d) average number = 30. The blue line represents the vertical profile of $\text{TAB}_{532}$ derived from CALIPSO data, the black cross represents the centroid of the cluster and the orange horizontal line represents the BLH result.
Figure 7. Relationship between the horizontal smoothing number and BLH under different cases: (a) 4 October 2013 and (b) 12 February 2015.
Figure 8. Total attenuated backscatter at 532 nm wavelength (TAB\textsubscript{532}) plot from CALIPSO on 7 October 2014 under the horizontal smoothing number (a) 15 and (c) 9. The corresponding vertical profile of TAB\textsubscript{532} derived from CALIPSO profile over Wuhan area under the horizontal smoothing number (b) 15 and (d) 9.
Figure 9 Correlation of BLH derived from CALIPSO and ground-based Lidar under the horizontal smoothing number of (a) 1, (b) 3, (c) 6, (d) 9, (e) 12 and (f) 15. The correlation of BLH derived from CALIPSO and RS measurements under the horizontal smoothing number of (d) 15, (e) 9 and (f) 3. The red and blue points represent the BLH calculated by GDM algorithm and MSD method, respectively.