The link between Outgoing Longwave Radiation and the altitude where a spaceborne lidar beam is fully attenuated

Thibault Vaillant de Guélis¹, Hélène Chepfer¹, Vincent Noel², Rodrigo Guzman³, Philippe Dubuisson⁴, David M. Winker⁵, Seiji Kato⁵

¹LMD/IPSL, Université Pierre et Marie Curie, Paris, France
²Laboratoire d’Aéologie, CNRS, Toulouse, France
³LMD/IPSL, CNRS, École polytechnique, Palaiseau, France
⁴Laboratoire d'Optique Atmosphérique, Université Lille, Lille, France
⁵NASA Langley Research Center, Hampton, Virginia, USA

Correspondence to: Thibault Vaillant de Guélis (thibault.vaillant-de-guelis@lmd.polytechnique.fr)

Abstract. According to climate model simulations, the changing altitude of mid and high clouds is the dominant contributor to the positive global mean longwave cloud feedback. Nevertheless, the mechanism of this longwave cloud altitude feedback and its magnitude have not yet been verified by observations. Accurate, stable, and long-term observations of a metric characterizing cloud vertical distribution and related to the longwave cloud radiative effect is needed to achieve a better understanding of the mechanism of longwave cloud altitude feedback. This study shows that direct measurement of the altitude of atmospheric lidar opacity is a good candidate for the necessary observational metric. The opacity altitude is the level at which a spaceborne lidar beam is fully attenuated when probing an opaque cloud. By combining this altitude with direct lidar measurement of the cloud top altitude, we derive the effective radiative temperature of opaque clouds which linearly drives (as we will show) the outgoing longwave radiation. We find that, for an opaque cloud, a cloud temperature change of 1 K modifies its cloud radiative effect by 2 W m⁻². Similarly, the longwave cloud radiative effect of optically thin clouds can be derived from their top and base altitudes and an estimate of their emissivity. We show with radiative transfer simulations that these relationships hold true at single atmospheric column scale, at the scale of the Clouds and the Earth's Radiant Energy System (CERES) instantaneous footprint, and at monthly mean 2°×2° scale. Opaque clouds cover 35 % of the ice-free ocean and contribute to 73 % of the global mean cloud radiative effect. Thin cloud coverage is 36 % and contributes 27 % of the global mean cloud radiative effect. The link between outgoing longwave radiation and the altitude where a spaceborne lidar beam is fully attenuated provides a simple formulation of the cloud radiative effect in the longwave domain and so helps to understand the longwave cloud altitude feedback mechanism.
1 Introduction

Cloud feedbacks remain the main source of uncertainty in predictions of climate sensitivity (e.g. Dufresne and Bony, 2008; Vial et al., 2013; Webb et al., 2013; Caldwell et al., 2016). One reason for this uncertainty is that clouds simulated by climate models in the current climate, exhibit large biases compared to observations (e.g. Zhang et al., 2005; Haynes et al., 2007; Chepfer et al., 2008; Williams and Webb, 2009; Marchand and Ackerman, 2010; Cesana and Chepfer, 2012; Kay et al., 2012; Nam et al., 2012; Cesana and Chepfer, 2013; Klein et al., 2013), leading to low confidence in the cloud feedbacks predicted by the models.

To understand feedback mechanisms, it is useful to identify the fundamental variables driving the climate radiative response, and then to decompose the overall radiative response as the sum of the individual responses due to changes in each of these variables. This classical feedback analysis has been frequently applied to outputs from numerical climate system simulations in order to estimate the effects of changes in water vapor, temperature lapse rate, clouds and surface albedo on the overall climate radiative response (e.g. Cess et al., 1990; Le Treut et al., 1994; Watterson et al., 1999; Colman, 2003; Bony et al., 2006; Bates, 2007; Soden et al., 2008; Boucher et al., 2013; Sherwood et al., 2015; Rieger et al., 2016). Focusing only on the cloud feedback mechanisms, Zelinka et al. (2012a) and others used this approach to isolate the role of each of the fundamental cloud variables that contribute to the cloud radiative response: cloud cover, cloud optical depth or water phase (liquid or ice), and cloud altitude (or cloud temperature). The shortwave (SW) cloud feedback is primarily driven by changes in cloud cover and cloud optical depth, whereas the longwave (LW) cloud feedback is driven by changes in cloud cover, cloud optical depth and cloud vertical distribution (e.g. Klein and Jakob, 1999; Zelinka et al., 2012b, 2013, 2016).

Using observations to verify the cloud feedback mechanisms simulated in climate models requires two steps: First, establish a robust link between the observed fundamental cloud variables and the cloud radiative effect (CRE) at the top of the atmosphere (TOA), so that a change in a fundamental cloud variable can be unambiguously related to a change in the CRE at the TOA. Second, establish an observational record of these fundamental cloud variables that is long enough, stable enough, and accurate enough to detect the cloud changes due to greenhouse gases forcing (Wielicki et al., 2013). Such records do not exist yet, but existing records might help our understanding (Klein and Hall, 2015).

This paper focuses on the LW cloud feedback. Current climate models consistently predict that cloud altitude change is the dominant contributor to the LW cloud feedback (Zelinka et al., 2016) consistent with many previous studies (e.g. Schneider, 1972; Cess, 1975; Hansen et al., 1984; Wetherald and Manabe, 1988; Cess et al., 1996; Hartmann and Larson, 2002). While models agree on the sign and the physical mechanism of the LW cloud altitude feedback, they predict different magnitude. Simulations from the Coupled Model Intercomparison Project Phase 5 (CMIP5) suggest that upper tropospheric clouds will rise by 0.7 to 1.7 km, at all latitudes, in a warmer climate (+4 K). This is a significant change compared to the currently observed variability and means cloud altitude could be a more robustly observable signature of climate change than the CRE (Chepfer et al., 2014). Nevertheless, the LW cloud altitude feedback mechanism and its magnitude still remain to be confidently verified with observations, because 1) there is no simple, robust, and comprehensive mathematical formulation linking the observed fundamental cloud variables and the LW CRE at the TOA and 2) there are no sufficiently accurate and stable observations of the vertical distribution of clouds over several decades.

A preliminary step toward observational constraints on LW cloud feedback would be to establish a robust link between the LW CRE at the TOA and a small number of fundamental cloud properties that can be both accurately observed and simulated in climate models. In the SW, Taylor et al. (2007) defined such a simplified radiative transfer model by robustly expressing the SW CRE as a function of the cloud cover and the cloud optical depth. This linear relationship has been widely used for decomposing SW cloud feedbacks into contributions from changes in cloud cover and optical depth. Unlike the SW CRE, the LW CRE depends on a third variable, cloud vertical distribution, in addition to cloud cover and optical depth. This makes establishing a simple radiative transfer model that robustly expresses the CRE as a function of a
limited number of properties more challenging in the LW than in the SW, as Taylor et al. (2007) and Yokohata et al. (2005) recognized.

Detailed information from active sensors has already been fed into comprehensive radiative transfer simulations to accurately compute the TOA and surface LW CRE in well-defined atmospheric conditions (e.g. Zhang et al., 2004; L’Ecuyer et al., 2008; Kato et al., 2011; Rose et al., 2013). Defining a simple linear formulation linking the LW CRE at the TOA to a limited number of cloud variables would be more directly useful for decomposing cloud climate feedbacks. This formulation, however, cannot utilize the detailed cloud vertical distribution but must be based on specific cloud levels that drive the LW CRE at the TOA. Further, these specific cloud levels must be accurately observable at global scale from satellites.

Most of the cloud climatologies derived from space observations rely on passive satellites, which do not retrieve the detailed cloud vertical distribution, and instead retrieve single-layer effective cloud heights, often summarized as cloud fraction in seven cloud top pressure bins. Hartmann et al. (1992) used these pressure bins coupled with ranges of cloud optical depth to define different cloud types associated to different values of CRE. These cloud types have been used to analyze the interannual cloud record collected by the Moderate Resolution Imaging Spectroradiometer (MODIS) (e.g. Zelinka and Hartmann, 2011; Zhou et al., 2013; Yue et al., 2017). Recently, Marvel et al. (2015) and Norris et al. (2016) analyzed data from the International Satellite Cloud Climatology Project (ISCCP) and the Pathfinder Atmospheres Extended (PATMOS-x) datasets in terms of these cloud types to search for trends in LW CRE which would be associated with changes in cloud properties.

Today, ten years of satellite-borne active sensor data collected by the Cloud-Aerosol Lidar with Orthogonal Polarization (CALIOP) from the Cloud-Aerosol Lidar and Infrared Pathfinder Satellite Observations (CALIPSO; Winker et al., 2010) and the Cloud Profiling Radar (CPR) from CloudSat (Stephens et al., 2002) are available to provide a detailed and accurate view of cloud vertical distribution. Recently, Stephens et al. (submitted) used combined passive and active sensor observations (2B-FLXHR-LIDAR product; Henderson et al., 2013) to re-build cloud types similar to Hartmann et al. (1992). Stephens et al (submitted) found differences in attribution of CRE to cloud type compared to Hartmann et al. (1992), largely due to ambiguities of passive cloud top height retrievals in the presence of optically thin and multi-layer clouds (e.g. Sherwood et al., 2004; Holz et al., 2008; Mace et al., 2011; Michele et al., 2013; Stubenrauch et al., 2013). Data from CALIOP and CloudSat can be used to build, for the first time, a simplified radiative transfer model that robustly expresses the LW CRE as a function of cloud cover, optical depth (or emissivity) and cloud altitude, and that can be tested against observations. In this paper, we summarize the vertical profiles of clouds observed by active sensors using three specific cloud levels that drive the LW CRE at the TOA and that can be accurately observed by spaceborne lidar: cloud top altitude, cloud base altitude, and the altitude of opacity, at which lidar signal becomes fully attenuated within an Opaque cloud. This altitude of opacity and the Opaque cloud cover are both observed by spaceborne lidar, and are strongly correlated to the LW CRE (Guzman et al., 2017) because emissions from layers located below the altitude of opacity have little influence on the outgoing LW radiation (OLR). Previous studies (Ramanathan, 1977; Wang et al., 2002), suggested that the link between the Opaque cloud temperature and the OLR is linear, which would be mathematically very convenient for the study of cloud feedbacks (derivatives), but these studies are limited to radiative transfer simulations only. We propose to build on these studies by adding spaceborne lidar information to obtain a simplified radiative transfer model in the LW domain that can give a highly accurate proxy for OLR with a small set of parameters available from both observations (space-lidar) and models (space-lidar simulator). This approach is in contrast to reliance on 7×7 histograms (altitude×optical depth) of cloud types from ISCCP and use of a matching radiative kernel. Moreover, a highly stable long-time observational record is essential to study clouds and climate feedback (Wielicki et al., 2013), and current passive instruments have shown limited calibration stability over decadal time scales (e.g. Evan et al., 2007; Norris and Evan, 2015; Shea et al., 2017).
In Section 2 we present the data and methods used in this study. In Section 3 we define the radiative temperatures of Opaque and Thin clouds derived from combined lidar observations and reanalysis, and document them over the mid-latitudes and the tropics. In Section 4 we use radiative transfer simulations to establish a simple expression of the OLR as a function of lidar cloud observations for Opaque cloud single columns and for Thin cloud (non-opaque) single columns, using clear sky data from the Clouds and the Earth's Radiant Energy System (CERES) satellite instrument. We verify this relationship using CERES and CALIPSO observations, first collocated at the instantaneous 20 km scale, then monthly-averaged on 2° latitude × 2° longitude grids. In Section 5 we estimate the independent contributions to the LW CRE of optically Opaque clouds and optically Thin clouds. We then focus on the Tropics and examine Opaque and Thin cloud CRE partitioned into regions of subsidence and deep convection. Section 6 discusses the limits of the linear expression we propose, and concluding remarks are summarized in Section 7.
2 Data and Method

2.1 Opaque and Thin cloud observations by spaceborne lidar

Eight years (2008–2015) of CALIPSO observations are used in this study. The GCM-Oriented CALIPSO Cloud Product (GOCCP-OPAQ (GOCCP v3.0; Guzman et al., 2017) has 40 vertical levels with 480 m vertical resolution. Every CALIOP single shot profile — including multi-layer profiles — is classified into one of three types (Fig. 1):

- **Clear sky single column** (brown, center) is entirely free of clouds: none of the 40 levels composing the atmospheric single column are flagged as "Cloud" (cloud detection information in Chepfer et al., 2010).

- **Opaque cloud single column** (orange, right) contains a cloud in which the lidar is fully attenuated, at an altitude termed $Z_{\text{opaque}}$. Full attenuation of the signal is reached at a visible optical depth of about 3 to 5 integrated from the TOA (Vaughan et al., 2009). This corresponds to a cloud LW emissivity of 0.8 to 0.9, if we consider that cloud particles do not absorb visible wavelengths and that scattering can be neglected in the LW domain. In GOCCP, such an opaque single column is identified by one level flagged as "z_opaque". Like other variables identified by the superscript "|" in the rest of this paper, $Z_{\text{opaque}}$ refers to a *single column*, i.e. a 1D atmospheric column from the surface to the TOA where each altitude layer is uniformly filled with molecules and/or clouds. $Z_{\text{opaque}}$ depends on the horizontal and vertical averaging used in the retrieval algorithm. It is also affected during daytime by noise from the solar background. At 480 m vertical resolution, it depends weakly on the characteristics of the lidar.

- **Thin cloud single column** (brown and blue, left), contains one or more semi-transparent clouds. In GOCCP, such a single column is identified by at least one level flagged as "Cloud" but no level flagged as "z_opaque".

![Fig. 1. Partitioning of the atmosphere into 3 single column types thanks to the CALIOP lidar: (left) Thin cloud single column, when a cloud is detected in the lidar signal and the laser beam reaches the surface, (middle) Clear sky single column, when no cloud is detected, and (right) Opaque cloud single column, when a cloud is detected and the laser beam becomes fully attenuated at a level called $Z_{\text{opaque}}$. $C$, $T$ and $\varepsilon$ account for cover, temperature and emissivity. Variables highlighted in yellow are the key cloud properties, extracted from GOCCP-OPAQ, that drive OLR over Thin cloud and Opaque cloud single columns. The total gridded OLR will be computed from the 3 single column OLRs weighted by their respective cover: $C_{\text{Thin}}, C_{\text{clear}}, C_{\text{opaque}}$.](image-url)
Figure 2 shows the global coverage of these 3 single column types on $2^\circ \times 2^\circ$ grids. Global mean Opaque cloud cover $C_{\text{opaque}}^{\oplus}$ is 35%, Thin clouds cover $C_{\text{thin}}^{\oplus}$ is 36% and the Clear sky cover $C_{\text{clear}}^{\oplus}$ is 29%. $C_{\text{opaque}}^{\oplus}$, $C_{\text{thin}}^{\oplus}$ and $C_{\text{clear}}^{\oplus}$ refer to $2^\circ \times 2^\circ$ grid box, like any variable identified by the superscript "$\oplus$" in the rest of the paper. Opaque cloud cover is very high at mid-latitudes and, in the tropics, high occurrences clearly reveal regions of deep convection (warm pool, ITCZ) and stratocumulus regions at the east part of oceans. Thin cloud cover is very homogeneous over all oceans, with slight maxima in some regions, near the warm pool. These results are discussed in Guzman et al. (2017).

Our study builds on the work of Guzman et al. (2017) by considering $Z_{\text{opaque}}^{\parallel}$ in terms of temperature rather than altitude, and by estimating an additional variable, the Thin cloud emissivity:

- Temperatures $T_{\text{opaque}}^{\parallel}$, $T_{\text{top}}^{\parallel}$ and $T_{\text{base}}^{\parallel}$ are respectively those at the altitudes of the level flagged as "z_opaque" ($Z_{\text{opaque}}^{\parallel}$) and of the highest ($Z_{\text{top}}^{\parallel}$) and lowest ($Z_{\text{base}}^{\parallel}$) levels flagged as "Cloud", using temperature profiles from the NASA Global Modeling and Assimilation Office (GMAO) reanalysis (Suarez et al., 2005) provided in CALIOP Level 1 data and also reported in GOCCP v3.0 data.
• Thin cloud emissivity $\varepsilon_{\text{thin}}^\perp$ of a Thin cloud single column is inferred from the attenuated scattering ratio of clear sky layers measured by the lidar below the cloud. This is approximately equal to the apparent two-way transmittance through the cloud which, considering a fixed multiple scattering factor $\eta = 0.6$, allows retrieval of the Thin cloud visible optical depth $r_{\text{thin}}^{\text{VIS}}$ (Garnier et al., 2015). As cloud particles are much larger than the wavelengths of visible and infrared light, and assuming there is no absorption by cloud particles in the visible domain, the Thin cloud LW optical depth $r_{\text{thin}}^{\text{LW}}$ is approximately half of $r_{\text{thin}}^{\text{VIS}}$ (Garnier et al., 2015). Finally, we retrieve the Thin cloud emissivity as $\varepsilon_{\text{thin}}^\perp = 1 - e^{-r_{\text{thin}}^{\text{LW}}}$. Emissivity of Opaque clouds cannot be inferred and we assume they are approximately black bodies, i.e. $\varepsilon_{\text{opaque}}^\perp \approx 1$.

Our approach takes into account the possibility of multi-layer clouds within single columns: $T_{\text{top}}^\perp$ and $Z_{\text{top}}^\perp$ refer to the highest level of the highest cloud in the column and $T_{\text{base}}^\perp$ and $Z_{\text{base}}^\perp$ to the lowest level of the lowest cloud in the column. In this case, $\varepsilon_{\text{thin}}^\perp$ is computed from the summed optical depth of all cloud layers in the column.

To avoid effects of solar background noise, results presented in this paper are only for nighttime conditions.

Furthermore, we only consider observations over oceans to avoid uncertainties due to the ground temperature diurnal cycle over land. In order not to be influenced by major surface changes across seasons, we also removed from this study all observations over sea ice, based on sea ice fraction from the European Centre for Medium-Range Weather Forecasts (ECMWF) ERA-Interim reanalysis (Berrisford et al., 2011).

2.2 Flux observations collocated with lidar cloud observations

The CERES radiometer, on-board the Aqua satellite, measures the OLR at the location where the CALIOP lidar, on board the CALIPSO satellite, will fire 2 minutes and 45 seconds later. The instantaneous Single Scanner Footprint (SSF) of the CERES swath crossing the CALIPSO ground-track gives the OLR over atmospheric single columns sounded by the lidar. The CERES footprint has a ~20 km diameter, while the CALIOP lidar samples every 333 m along-track with a 70 m diameter footprint, meaning the lidar can sample up to 60 atmospheric single columns within a single CERES footprint. To collocate the GOCCP-OPAQ instant data and the CERES SSF measurements, we use the CALIPSO, CloudSat, CERES, and MODIS Merged Product (C3M; Kato et al., 2011) which flags the instantaneous CERES SSF footprints where the CERES swath crosses the CALIPSO ground-track. For each of these flagged CERES SSF footprints, we matched, from geolocation information, all the GOCCP-OPAQ single columns falling into the CERES footprint. We consider that an atmospheric column with CERES footprint base is an Opaque (Thin) cloud column if all matched single columns are declared as Opaque (Thin) cloud single column. We then use these Opaque and Thin cloud columns to validate the lidar-derived OLR.

From the C3M product, we also use the estimated Clear sky OLR of the instantaneous CERES SSF where the CERES swath crosses the CALIPSO ground-track. This estimated Clear sky OLR is computed from radiative transfer simulations using the synergistic information of the different instruments flying in the Afternoon Train (A-Train) satellite constellation. As C3M only covers the period when both CALIPSO and CloudSat are both fully operational (until April 2011) we also use the Clear sky OLR from $1^\circ \times 1^\circ$ gridded data monthly mean CERES Energy Balanced and Filled (EBAF) Edition 2.8 $1^\circ \times 1^\circ$ product (Loeb et al., 2009), that we average over $2^\circ \times 2^\circ$ grid boxes.

2.3 Radiative transfer computations

For all the radiative transfer computations needed in this study, we use the GAME radiative transfer code (Dubuisson et al., 2004) combined with mean sea surface temperature (SST) and atmospheric profiles of temperature, humidity and ozone extracted from the ERA-Interim reanalysis. GAME calculates the radiative flux and radiances over the total solar and infrared spectrum. The radiative transfer equation is solved using DISORT (Stamnes et al., 1988) and gaseous...
absorption is calculated from the k-distribution method. The code accounts for scattering and absorption by aerosol and clouds as well as interactions with gaseous absorption. GAME does not take into account cloud 3D effects, and is based on the plane-parallel approximation. In this study, we use GAME to compute integrated OLR between 5 and 100 µm.
3 Radiative temperatures of Opaque and Thin clouds derived from lidar cloud observations and reanalysis

We define in this section the radiative temperatures of Opaque and Thin clouds that can be derived from lidar measurements. The cloud radiative temperature corresponds to the equivalent radiative temperature of the cloud \( T_{\text{rad}} \) such that the upward top of the cloud LW radiative flux emitted by the cloud with emissivity \( \varepsilon \) is \( F_{\text{cloud}}^{\text{LW}}(\text{Cloud Top}) = \varepsilon \sigma (T_{\text{rad}}^4) \), where \( \sigma \) denotes the Stefan–Boltzmann constant. We present distributions of these cloud radiative temperatures derived from lidar measurements over the mid-latitudes and the tropics.

3.1 Definition and approximations of the cloud radiative temperature

Considering an optically uniform cloud with a cloud total LW optical depth \( \tau_{\text{LW}}^{\text{cloud}} \), and assuming a linearly increasing temperature from the cloud top to the cloud base, we can compute the upward LW radiative flux at the cloud top emitted by the cloud \( F_{\text{cloud}}^{\text{LW}}(\text{Cloud Top}) \) using the radiative transfer equation (RTE) (see appendix A). Solving the equation \( F_{\text{cloud}}^{\text{LW}}(\text{Cloud Top}) = \varepsilon \sigma (T_{\text{rad}}^4) = (1 - e^{-\tau_{\text{LW}}^{\text{cloud}}}) \sigma (T_{\text{rad}}^4) \), we can infer the value of the equivalent radiative cloud temperature \( T_{\text{rad}} \). Figure 3 shows \( T_{\text{rad}} \) computed from RTE (green) as a function of \( \tau_{\text{LW}}^{\text{cloud}} \). As \( \tau_{\text{LW}}^{\text{cloud}} \) increases, \( T_{\text{rad}} \) decreases and approaches the cloud top temperature.

![Figure 3](image)

**Fig. 3.** Comparison of (green) the cloud radiative temperature \( T_{\text{rad}} \) inferred from the RTE (see appendix A) with the lidar-definitions of (blue) the Thin cloud radiative temperature \( T_{\text{Thin}}^1 \) and (red) the Opaque cloud radiative temperature \( T_{\text{Opaque}}^1 \), as a function of the cloud total LW optical depth \( \tau_{\text{LW}}^{\text{cloud}} \). Here, on an example with a fixed cloud top temperature \( T_{\text{Top}}^1 \) at 250 K and a fixed cloud base temperature \( T_{\text{Base}}^1 \) at 260 K.

\( T_{\text{rad}}^1 \) is obtained by computing the LW flux emitted by the cloud at the top \( F_{\text{cloud}}^{\text{LW}}(\text{Cloud Top}) \) from the RTE and solving \( F_{\text{cloud}}^{\text{LW}}(\text{Cloud Top}) = \varepsilon \sigma (T_{\text{rad}}^4) \).

Orange area defines Opaque clouds, which in lidar observations have \( \tau_{\text{LW}}^{\text{cloud}} \) greater than a limit situated between 1.5 to 2.5. Below this limit clouds are declared as Thin clouds (blue area). Clouds with \( \tau_{\text{cloud}} \) between 1.5 and 2.5 could be either Opaque or Thin clouds (gray area).

We approximate \( T_{\text{rad}}^1 \) for Opaque clouds and Thin clouds using straightforward formulations that can be derived from lidar cloud observations and reanalysis. For the Opaque cloud case (Fig. 1, right), the optically thick cloud completely absorbs upward LW radiative flux propagating from below. In this case, atmospheric layers below \( Z_{\text{Opaue}}^1 \) have little influence on \( OLR_{\text{Opaque}}^1 \). Therefore, \( OLR_{\text{Opaque}}^1 \) is mainly driven by an Opaque cloud radiative temperature defined as:
For the Thin cloud case (Fig. 1, left), the cloud is translucent so that a part of the upward LW radiative flux emitted by the surface and cloud-free atmospheric layers underneath the cloud is transmitted through the cloud. In this case, \( OLR_{\text{Thin}} \) depends on the surface temperature and surface emissivity, the temperature and humidity profiles below the cloud, the cloud emissivity \( e_{\text{Thin}} \), and the Thin cloud radiative temperature defined as:

\[
T_{\text{Thin}}^L = \frac{T_{\text{Top}}^L + T_{\text{Base}}^L}{2}
\]  

(2)

\( T_{\text{Thin}}^L (\tau_{\text{Cloud}} < 1.5, \text{ blue area in Fig. 3) and } T_{\text{opaque}}^L (\tau_{\text{Cloud}} > 2.5, \text{ orange area) agree well with } T_{\text{rad}}^L \) (deduced from RTE, green). Clouds with \( 1.5 < \tau_{\text{Cloud}} < 2.5 \) (gray area) can be either Thin or Opaque clouds depending on the integrated LW optical depth at which \( \tau_{\text{opaque}} \) will occur. In computing LW radiative flux, we assume the fixed cloud top temperature \( T_{\text{Top}}^L \) of 250 K and fixed cloud base temperature \( T_{\text{Base}}^L \) of 260 K. \( T_{\text{opaque}}^L \) depends on the integrated LW optical depth \( \tau_{\text{Cloud}}^L \) from cloud top to \( Z_{\text{opaque}}^L \). Since the equivalent visible optical depth \( \tau_{\text{VIS}}^L \) to \( Z_{\text{opaque}}^L \) is between 3 and 5 (Vaughan et al., 2009), and \( \tau_{\text{Cloud}}^L = 2 \tau_{\text{VIS}}^L \) (Chepfer et al., 2014), \( \tau_{\text{Cloud}}^L \) is known to be between 1.5 and 2.5, provided a range of possible values of \( T_{\text{opaque}}^L \) (black shadow area), and then, a range of possible values of \( T_{\text{opaque}}^L \) (red shadow area).

Computations with other pairs of \( T_{\text{Top}}^L \) and \( T_{\text{Base}}^L \) temperatures (not shown) reveal that the relative vertical position of \( T_{\text{rad}}^L \) does not depend much of the cloud top and base temperatures. In other words, other pairs of \( T_{\text{Top}}^L \) and \( T_{\text{Base}}^L \) would produce almost the same figure as Fig. 3, only with the y-axis temperature values changed. This means that the difference between \( T_{\text{rad}}^L \) and \( T_{\text{Thin}}^L \) or between \( T_{\text{rad}}^L \) and \( T_{\text{opaque}}^L \) becomes larger as the difference between \( T_{\text{Top}}^L \) and \( T_{\text{Base}}^L \) increases. Generally, the error made by using specific values of \( T_{\text{Thin}}^L \) and \( T_{\text{opaque}}^L \) in computing \( T_{\text{rad}}^L \) also depends on other cloud properties used in the computation, such as cloud inhomogeneity and cloud microphysics. However, this simple theoretical calculation shows that \( T_{\text{Thin}}^L \) and \( T_{\text{opaque}}^L \) as defined above are good approximations of the cloud radiative temperature of the Thin and Opaque clouds. Considering a cloud with \( \tau_{\text{Cloud}}^L > 5 \) and 10 K between its base and top temperatures, this approximation leads to an error of the radiative temperature less than 2 K for a Thin cloud, and less than 1 K error for an Opaque cloud.

These cloud radiative temperatures are fundamental to study the LW CRE and are different from the effective radiating temperatures measured by passive instruments which are influenced by radiation coming from below the cloud. In the case of Opaque cloud which completely absorbs upward LW radiative flux propagating from below, the effective radiating temperature measured by passive instruments should agree with the cloud radiative temperature. However, this assumes to know that the cloud is Opaque, but cloud emissivity from passive measurements is also sensitive to hypothesis made on the clear sky and surface property. Unlike passive measurements, lidar measurements robustly separate Opaque clouds and Thin clouds from the presence or not of a surface echo (Guzman et al., 2017).

3.2 \( T_{\text{opaque}}^L \) and \( T_{\text{Thin}}^L \) retrieved from CALIOP observations during 2008–2015

For each cloudy single column observed by CALIOP, we derive \( T_{\text{opaque}}^L \) from \( T_{\text{Top}}^L \) and \( T_{\text{Base}}^L \) using Eq. (1). We also derive \( T_{\text{Thin}}^L \) from \( T_{\text{Top}}^L \) and \( T_{\text{Base}}^L \) using Eq. (2). We then compute the probability density function (PDF) of \( T_{\text{opaque}}^L \) and \( T_{\text{Thin}}^L \) for 3 different regions: tropical ascending regions between \( \pm 30^\circ \) latitude with monthly mean 500-hPa pressure vertical velocity \( \omega_{500} < 0 \) hPa day\(^{-1}\), tropical subsidence regions between \( \pm 30^\circ \) latitude with monthly mean \( \omega_{500} > 0 \) hPa day\(^{-1}\) and
the mid-latitudes (North and South) between 65° S and 30° S and between 30° N and 65° N. To compute these PDFs, e.g. 
the PDF of $T_{\text{opaque}}$ among Opaque clouds, we firstly compute the PDF of $T_{\text{opaque}}$ using all single columns on each 2°×2° grid box for the 2008–2015 period. Then, we compute the PDF with area-weighted average by region, weighting each 2°×2° grid box PDF by the ratio of the number of Opaque single columns over the number of all single columns. We do this latter 
weighting in order to take into account sampling differences among 2°×2° grid boxes.

Figure 4a shows the distributions of $T_{\text{opaque}}$. In tropical subsidence regions (green), 71 % of $T_{\text{opaque}}$ are between 
0 °C and 25 °C with a maximum at 15 °C. Because these clouds are almost as warm as the surface, they do not strongly 
affect the OLR compared to clear sky conditions. These clouds are the marine boundary layer clouds present over the 
descending branches of the Hadley cells. In tropical ascending regions (red), $T_{\text{opaque}}$ follows a bimodal distribution with few 
clouds warmer than 0 °C (21 %) and most clouds between 0 °C and -80 °C (79 %). These cold Opaque clouds have locally a 
very strong impact on the OLR since they can be 100 K colder than the surface skin temperature. However, tropical 
ascending regions represent about only 1/5 of the ocean between 65° S and 65° N, making their global contribution less 
striking. In the mid-latitudes (purple), $T_{\text{opaque}}$ are concentrated in a narrower range (20 °C to -60 °C), with temperatures 
mostly between 10 °C and -30 °C. The local radiative effect of these Opaque clouds is weaker than the effect if they were in 
tropical ascending regions. Mid-latitudes are, however, a large area (43 % of the ocean surface between 65° S and 65° N) 
and the cover of Opaque clouds is large (Fig. 2a). So, their contribution to the global CRE is expected to be large.

The radiative temperature of Opaque clouds $T_{\text{opaque}}$ is based on the key new lidar information $Z_{\text{opaque}}$ (Eq. (1)).

Figure 4b shows that $Z_{\text{opaque}}$ is low for all regions, near 1 km altitude, especially in subsidence regions. $Z_{\text{opaque}}$ are 
sometimes between 2 km and 8 km in the mid-latitudes storm track regions. In tropical ascending regions, the PDF is tri-
modal with a lowest peak around 1 km associated with boundary layer clouds, and a highest peak around 12 km associated 
with deep convection systems. The middle mode, near 5 km, might be due to developing convective clouds or middle 
alitude clouds. Since $T_{\text{opaque}}$ also depends on $Z_{\text{top}}$, distributions of the distance between cloud top and $Z_{\text{opaque}}$ are given in 
Fig. A1a (appendix B).

The radiative temperature of Thin clouds $T_{\text{thin}}$ is mostly warmer than 0°C in tropical subsidence regions (Fig. 4c). 
$T_{\text{thin}}$ colder than -40 °C occurs more frequently than $T_{\text{opaque}}$ colder than -40 °C, suggesting high-altitude optically thin 
cirrus from detrainments of anvil clouds being generated in adjacent convective regions. In tropical ascending regions, the 
"warm" mode of the bimodal distributions of $T_{\text{thin}}$ is more populated and warmer than that of $T_{\text{opaque}}$. The main mode of 
$T_{\text{thin}}$ in the mid-latitudes, is also warmer than that of $T_{\text{opaque}}$. Warmer cloud temperatures, implying smaller CREs, 
reinforces the importance of the role of the Opaque clouds versus Thin clouds in the total CRE. Distributions of the distance 
between top and base for Thin clouds are given in Fig. A1b (appendix B).

Because the radiative impact of Thin clouds will also depend on cloud emissivity, we also compute the distributions 
of $e_{\text{thin}}$ (Fig. 4d). For all regions, the maximum occurs around 0.25: emissivities of Thin clouds are usually small, so they 
have little impact on the OLR and hence their contribution to CRE should be significantly smaller than that of Opaque 
clouds.
Observed distributions of (a) $T_{\text{opaque}}^\parallel$ among Opaque clouds, (b) $Z_{\text{opaque}}^\parallel$ among Opaque clouds, (c) $T_{\text{thin}}^\parallel$ among Thin clouds and (d) $\varepsilon_{\text{thin}}^\parallel$ among Thin clouds in three regions: (red) the tropical ascendance [$30^\circ S$–$30^\circ N$] (monthly mean $\omega_{500} < 0$ hPa day$^{-1}$), (green) the tropical subsidence [$30^\circ S$–$30^\circ N$] (monthly mean $\omega_{500} > 0$ hPa day$^{-1}$) and (purple) the mid-latitudes [$30^\circ$–$65^\circ$]. These regions represent respectively 22%, 35% and 43% of the $\pm 65^\circ$ ocean surface. Only nighttime over ice-free oceans for the 2008–2015 period is considered.
4. Outgoing longwave radiation derived from lidar cloud observations

In this section, we express the OLR as a function of cloud properties derived from lidar observations ($T_{opaque}^{l}$, $T_{thin}^{l}$, and $\varepsilon_{thin}^{l}$). We evaluate this relationship with observations at an instantaneous 20 km footprint scale, using high spatial resolution collocated satellite-borne broadband radiometer and lidar data. We also evaluate the relationship at a monthly mean 2° latitude × 2° longitude gridded scale.

4.1 Linear relationship deduced from radiative transfer simulations over a single cloudy column

The goal of this sub-section is to establish a simple and robust relationship between 1) the OLR over an Opaque cloud single column $OLR_{opaque}^{l}$ and the radiative temperature $T_{opaque}^{l}$ and, 2) the OLR over a Thin cloud single column $OLR_{thin}^{l}$ and the radiative temperature $T_{thin}^{l}$ and the Thin cloud emissivity $\varepsilon_{thin}^{l}$.

1) For an Opaque cloud single column, we computed $OLR_{opaque}^{l}$, using direct radiative transfer computations, for various atmospheres containing an Opaque cloud with variable altitude and vertical extent. The cloud is represented by a cloud layer with emissivity equal to 1 at $Z_{opaque}^{l}$ topped with optically uniform cloud layers with vertically integrated visible optical depth equal to 3.2, which corresponds to $\varepsilon \approx 0.8$. Dots in Fig. 5a show the obtained $OLR_{opaque}^{l}$ as function of $T_{opaque}^{l}$ for tropical atmosphere conditions. Linear regression (solid line) leads to:

$$OLR_{opaque}^{l(UID)} = 2.0T_{opaque}^{l} - 310.$$  \hspace{1cm} (3)

where $OLR_{opaque}^{l(UID)}$ is expressed in W m$^{-2}$ and $T_{opaque}^{l}$ in K. So, when $T_{opaque}^{l}$ decreases by 1 K (e.g. if the Opaque cloud rises up) then the OLR decreases by 2 W m$^{-2}$. This linear relationship, initially pointed out by Ramanathan (1977), has a slope which is consistent with previous work that found 2.24 W m$^{-2}$/K (Wang et al. (2002) using the radiative transfer model of Fu and Liou (1992, 1993) and the analysis of Kiehl (1994)). Conducting the same linear regression on very different atmospheric conditions (from tropical to polar) gives similar coefficients. This means that $OLR_{opaque}^{l}$ depends mainly on $T_{opaque}^{l}$. This remarkable result demonstrates that a cloud property driving the OLR can be derived from spaceborne lidar measurement. Differences between the computed OLR and the black body emission (dashed line in Fig. 5a) represent the extinction effect of the atmospheric layers above the cloud.

2) For a Thin cloud single column, we can consider that $OLR_{thin}^{l}$ is composed of two parts (Fig. 1). The first part, coming from the LW flux emitted by the cloud, can be expressed in the same way as Eq. (3) using $T_{thin}^{l}$ instead of $T_{opaque}^{l}$, and weighted by the Thin cloud emissivity $\varepsilon_{thin}^{l}$. The second part is equal to the OLR over a Clear sky single column $OLR_{clear}^{l}$ (the same single column without the cloud) multiplied by the cloud transmissivity $(1 - \varepsilon_{thin}^{l})$:

$$OLR_{thin}^{l(UID)} = \varepsilon_{thin}^{l}(2.0T_{thin}^{l} - 310) + (1 - \varepsilon_{thin}^{l})OLR_{clear}^{l}.$$  \hspace{1cm} (4)

where $OLR_{thin}^{l(UID)}$ and $OLR_{clear}^{l}$ are expressed in W m$^{-2}$ and $T_{thin}^{l}$ in K. In order to evaluate this expression and to examine the dependence of $OLR_{thin}^{l}$ to $T_{thin}^{l}$ and $\varepsilon_{thin}^{l}$, we computed $OLR_{thin}^{l}$, using direct radiative transfer computations, for various atmospheres containing a Thin cloud (represented by optically uniform cloud layers with integrated emissivities equal to $\varepsilon_{thin}^{l}$) with different altitudes, vertical extents and emissivities. Dots in Fig. 5b show the resulting $OLR_{thin}^{l}$ as a function of $T_{thin}^{l}$ for 4 different values of $\varepsilon_{thin}^{l}$ in tropical atmosphere conditions. We compare these results with the linear expression of Eq. (4) (solid lines), in which $OLR_{clear}^{l}$ is computed for a single column without cloud. The theoretical formulation agrees quite well with the different simulations. This formulation seems to overestimate $OLR_{thin}^{l}$ (up to +10 W m$^{-2}$) in many cases. Reasons for it are discussed in Section 6.
Fig. 5. Relationship between the OLR and the cloud radiative temperature from radiative transfer computations: (a) over an Opaque cloud single column and (b) over a Thin cloud single column. Direct radiative transfer computations are shown in dots. Solid lines represent the linear relationships inferred from a regression on dots in the Opaque case and applied to the Thin cloud case according to Eq. (4). For a fixed value of cloud emissivity (dots colors; 1 [purples] for Opaque clouds and 0.1 [reds], 0.3 [ blues], 0.5 [ greens], 0.7 [greys] for Thin clouds), the linear relationship does not depend on the cloud altitudes (dots light intensity; 0 km [ dark] – 16 km [ bright]) or geometrical thickness (dots size; 1 km [ small] – 5 km [ large]). Results shown here use the 2008-year mean thermodynamic atmospheric variables over the tropics [30° S–30° N] from ERA-I reanalysis.

4.2 Evaluation of the linear relationship using observations at instantaneous CERES footprint scale

We evaluate the robustness of the OLR expressions (Eqs. (3) and (4)) at the resolution of a CERES footprint (∼20 km) using CERES measurements, and cloud properties derived from collocated CALIOP observations $T_{\text{Opaque}}$, $T_{\text{Thin}}$ and $\varepsilon_{\text{Thin}}$. For this purpose, we apply Eqs. (3) and (4) using $T_{\text{Opaque}}$, $T_{\text{Thin}}$, $\varepsilon_{\text{Thin}}$ and the estimated OLR over the scene without the clouds $\text{OLR}_{\text{Clear}}$ given by CSM. $T_{\text{Opaque}}$, $T_{\text{Thin}}$, $\varepsilon_{\text{Thin}}$ refer to an atmospheric column with a CERES footprint base (identified by the superscript “$\square$”) and are obtained by averaging all $T_{\text{Opaque}}$, $T_{\text{Thin}}$ and $\varepsilon_{\text{Thin}}$ within the CERES footprint. $\text{OLR}_{\text{Clear}}$, $\text{OLR}_{\text{Opaque}}$ and $\text{OLR}_{\text{Thin}}$ refer to atmospheric columns with a CERES footprint base.

Figure 6 compares lidar-derived and observed OLR during January 2008. Figure 6a compares the $\text{OLR}_{\text{Opaque}}$ measured by CERES over footprints entirely covered by an Opaque cloud, with the $\text{OLR}_{\text{Opaque}}^{(\text{lid})}$ computed from $T_{\text{Opaque}}$ using Eq. (3). We see a very strong correlation between observed and computed OLR ($R = 0.95$). This confirms that the OLR over an Opaque cloud is linearly dependent on $T_{\text{Opaque}}$, and that it is possible to derive a cloud property which is proportional to the OLR from lidar measurement. Monitoring $T_{\text{Opaque}}$ on long-term should provide important information useful to better understand the LW cloud feedback mechanism.

Figure 6b is the same as Fig. 6a but only CERES footprints entirely covered by a Thin cloud are used. $\text{OLR}_{\text{Thin}}^{(\text{lid})}$, computed from $T_{\text{Thin}}$, $\varepsilon_{\text{Thin}}$ and $\text{OLR}_{\text{Clear}}$ using Eq. (4), correlates well with $\text{OLR}_{\text{Thin}}^{(\text{CERES})}$ ($R = 0.89$) but the regression line slightly differs from the identity line. Possible reasons for disagreements between both values are discussed in Section 6.
These same results are also shown as a function of $T_{\text{Thin}}^{\ominus}$ and $\varepsilon_{\text{Thin}}^{\ominus}$ in Fig. A2 for a fixed value of $\text{OLR}_{\text{Clear}}^{\ominus}$ (we selected measurements where $\text{OLR}_{\text{Clear}}^{\ominus} \in [275, 285] \text{ W} \cdot \text{m}^{-2}$) in order to show the effect of those two cloud properties on $\text{OLR}_{\text{Thin}}^{\ominus}$.

The same evaluation performed with July 2008 data (not shown) gives similar results, with $R = 0.96$ for Opaque clouds and $R = 0.90$ for Thin clouds.

![Fig. 6. Comparison between observed and lidar-derived OLR at CERES footprint scale: (a) over Opaque cloud single columns and (b) over Thin cloud single columns. Results obtained from CERES (y-axis) and CALIOP (x-axis) collocated measurements. $\text{OLR}_{\text{Opaque}}^{\ominus}$ and $\text{OLR}_{\text{Thin}}^{\ominus}$ are computed using Eqs. (4) and (5). Only nighttime conditions over ice-free oceans for January 2008 are considered. $R$ is the correlation coefficient.](image)

**4.3 Evaluation of the linear relationship using observations at monthly mean 2°×2° gridded scale**

We first compute the monthly mean gridded total OLR from gridded lidar cloud properties:

$$\text{OLR}_{\text{Total}}^{\ominus} = C_{\text{Clear}}^{\ominus} \text{OLR}_{\text{Clear}}^{\ominus} + C_{\text{Opaque}}^{\ominus} \text{OLR}_{\text{Opaque}}^{\ominus} + C_{\text{Thin}}^{\ominus} \text{OLR}_{\text{Thin}}^{\ominus},$$

where $C_{\text{Clear}}^{\ominus}$, $C_{\text{Opaque}}^{\ominus}$ and $C_{\text{Thin}}^{\ominus}$ are the monthly mean covers (Figs. 1,2): the ratio between the number of a specific kind of single column to the total number of single columns that fall into the grid box during a month. $\text{OLR}_{\text{Opaque}}^{\ominus}$ is computed from $T_{\text{Opaque}}^{\ominus}$ using Eq. (3), and $\text{OLR}_{\text{Thin}}^{\ominus}$ is computed from $T_{\text{Thin}}^{\ominus}$, $\varepsilon_{\text{Thin}}^{\ominus}$ and $\text{OLR}_{\text{Clear}}^{\ominus}$ using Eq. (4). $T_{\text{Opaque}}^{\ominus}$, $T_{\text{Thin}}^{\ominus}$ and $\varepsilon_{\text{Thin}}^{\ominus}$ are obtained by averaging respectively all $T_{\text{Opaque}}^{\ominus}$, $T_{\text{Thin}}^{\ominus}$ and $\varepsilon_{\text{Thin}}^{\ominus}$ within the 2°×2° box.

We then evaluate the lidar-derived $\text{OLR}_{\text{Total}}^{\ominus}$ against the CERES measurements $\text{OLR}_{\text{Total}}^{\ominus}$ (CERES). To do so, we computed the 2008–2010 mean $\text{OLR}_{\text{Total}}^{\ominus}$ from Eq. (5) using $\text{OLR}_{\text{Clear}}^{\ominus}$ from C3M and compared it with the one measured by CERES-Aqua. Figure 7 shows the comparison between the computed $\text{OLR}_{\text{Total}}^{\ominus}$ (Fig. 7a) and the measured $\text{OLR}_{\text{Total}}^{\ominus}$ (Fig. 7b). We first note the agreement of OLR patterns. Figure 7c shows the difference between those two maps. The global mean difference is -0.1 W·m$^{-2}$: $\text{OLR}_{\text{Total}}^{\ominus}$ very slightly underestimate the observed $\text{OLR}_{\text{Total}}^{\ominus}$. The zonal mean differences (not shown) are mostly lower than 2 W·m$^{-2}$, never exceeding 5 W·m$^{-2}$. Locally, we note a lack of
OLR over the warm pool, the Intertropical Convergence Zone (ITCZ) and the stratocumulus regions off the West coast of continents (up to 6–8 W·m⁻²) and an excess of OLR over latitudes beyond 50° N or 40° S (up to 4–6 W·m⁻²). As C3M only covers through April 2011, but we aim to use this framework on long time-series observations, we replace $OLR_{\text{clear}}$ from C3M by $OLR_{\text{clear}}$ from CERES-EBAF in the rest of this paper. Using $OLR_{\text{clear}}$ from C3M instead of CERES-EBAF increases the global mean $OLR_{\text{Total}}^{(LID)}$ by 0.6 W·m⁻² (Fig. A3), for reasons discussed in Section 6.

**Fig. 7.** Comparison between observed and lidar-derived OLR at 2°×2° gridded scale: (a) derived from CALIOP observations and (b) measured by CERES-Aqua. (c) = (a) - (b). Only nighttime conditions over ice-free oceans for the 2008–2010 period are considered. Global mean values are given in parentheses.
5 Contributions of Opaque clouds and Thin clouds to the cloud radiative effect

In the previous section, we found a linear relationship between $OLR_{opaque}$ and $T_{opaque}$ at different scales. The relationship for Thin clouds, though quite simple, is not linear and agrees less with observations than for Opaque clouds. In this section, we evaluate the contributions of Opaque clouds and Thin clouds to the total CRE.

5.1 Partitioning cloud radiative effect into Opaque CRE and Thin CRE

Using Eq. (5), we can decompose the total CRE at the TOA, computed from lidar observations, in Opaque and Thin clouds contributions:

$$CRE^{(LID)}_{Total} = OLR^{(LID)}_{clear} - OLR^{(LID)}_{Total}$$

$$= C^{opaque}_{opaque} (OLR^{opaque}_{clear} - OLR^{opaque}_{opaque}) + C^{Thin}_{Thin} (OLR^{Thin}_{clear} - OLR^{Thin}_{Thin}).$$

(6)

$CRE^{(LID)}_{opaque}$ and $CRE^{(LID)}_{Thin}$

Thereby, using Eq. (3), we can express $CRE^{(LID)}_{opaque}$ as a function of $C^{opaque}_{opaque}$, $T^{opaque}_{opaque}$ and $OLR^{opaque}_{clear}$:

$$CRE^{(LID)}_{opaque} = C^{opaque}_{opaque} (OLR^{opaque}_{clear} - 2.0T^{opaque}_{opaque} + 310)$$

(7)

where $CRE^{(LID)}_{opaque}$ and $OLR^{opaque}_{clear}$ are expressed in W m$^{-2}$ and $T^{opaque}_{opaque}$ in K.

Using Eq. (4), we can express $CRE^{(LID)}_{Thin}$ as a function of $C^{Thin}_{Thin}$, $T^{Thin}_{Thin}$, $\epsilon^{Thin}$ and $OLR^{Thin}_{clear}$:

$$CRE^{(LID)}_{Thin} = C^{Thin}_{Thin} (OLR^{Thin}_{clear} - 2.0T^{Thin}_{Thin} + 310)$$

(8)

where $CRE^{(LID)}_{Thin}$ and $OLR^{Thin}_{clear}$ are expressed in W m$^{-2}$ and $T^{Thin}_{Thin}$ in K.

5.2 Global means of the Opaque cloud CRE and the Thin cloud CRE

Figure 8 shows the zonal mean observations of the 5 cloud properties ($C^{opaque}_{opaque}$, $T^{opaque}_{opaque}$, $C^{Thin}_{Thin}$, $T^{Thin}_{Thin}$ and $\epsilon^{Thin}$). Over the subsidence branches of the Hadley cell, around 20° S and 20° N, $C^{opaque}_{opaque}$ is minimum (Fig. 8a), $T^{opaque}_{opaque}$ and $T^{Thin}_{Thin}$ are warm (Fig 8b, temperatures in y-axis oriented downward) and $\epsilon^{Thin}$ is minimum (Fig. 8c). So, we do not expect a large contribution to the CRE from these regions. In contrast, the Intertropical Convergence Zone (ITCZ) corresponds to local maxima of Opaque and Thin cloud covers, extremely cold $T^{opaque}_{opaque}$ and $T^{Thin}_{Thin}$ and a maximum of $\epsilon^{Thin}$. A large CRE is, therefore, expected from this region. There are always more Opaque clouds than Thin clouds in the extratropics (beyond 30° latitude) and they are colder than the Thin clouds. It is the opposite in the tropical belt: there are always more Thin clouds than Opaque clouds, and those are slightly warmer. This suggests that the relative contribution of the Thin clouds to the CRE is larger in the tropics than in the rest of the globe. This should not be very dependent on a specific year since the interannual variations of these 5 cloud properties (represented by the shaded areas) are very small compared to the zonal differences.
Figure 8. Zonal mean observations: (a) $C_{\text{Opaque}}$ and $C_{\text{Thin}}$, (b) $T_{\text{Opaque}}$ among Opaque clouds and $T_{\text{Thin}}$ among Thin clouds and (c) $\varepsilon_{\text{Thin}}$ among Thin clouds. Only nighttime conditions over ice-free oceans for the 2008–2015 period are considered. Shaded areas represent the envelope (max to min) including interannual variations.

Figure 9 shows that Opaque clouds contribute the most (73 %) to the total CRE. We can also note that the zonal variations of $CRE_{\text{Opaque}}^{(LID)}$, and so approximately the variations of $CRE_{\text{Total}}^{(LID)}$ (black line), can be explained by the zonal variations of $T_{\text{Opaque}}$ and $C_{\text{Opaque}}$ (Fig. 8a,b). For example, the absolute maximum CRE at $5^\circ$ N (~44 W m$^{-2}$) is associated with a large cover and cold temperature of Opaque clouds. As suggested earlier, the relative contribution of Thin clouds ($CRE_{\text{Thin}}^{(LID)}/CRE_{\text{Total}}^{(LID)}$, Fig. 9b) is larger in the tropics, approximately twice larger below $30^\circ$ (up to 40 %) than beyond those latitudes.
Fig. 9. (a) Partitioning of total CRE into Opaque CRE and Thin CRE. (b) Ratios of the Opaque and Thin CRE to the total CRE. Only nighttime conditions over ice-free oceans for the 2008–2015 period are considered.

Figure 10 shows the same CRE partitioning on maps. The similarity of patterns between total CRE (Fig. 10a) and the Opaque clouds CRE contribution (Fig. 10b) is obvious, showing again that Opaque clouds mostly drive the CRE. The contribution of Thin clouds to the CRE (Fig. 10c) is quite large between 20° S and 20° N in the Indian Ocean and the West Pacific Ocean, especially all around Indonesia, where $C_{\text{thin}}$ (Fig. 2b) is maximum and $T_{\text{thin}}$ minimum (not shown).
Globally, the predominance of CRE is obvious since it represents nearly three quarters of the total CRE. Thereby, the cloud property T_{opaque} inferred from lidar observations and linearly linked to OLR_{opaque} should be a very good candidate to constrain LW cloud feedbacks since Thin clouds only account for 27% of CRE_{total}. However, since the OLR expression above Thin clouds is almost as good as for Opaque clouds, it could also be used in a future work to quantify the impact of changes in CRE_{Thin}, T_{Thin}, and ε_{Thin} on the variations of CRE_{Thin}.

5.3 Tropical Opaque cloud CRE and Thin cloud CRE in dynamical regimes

Figure 11 shows the cloud properties as a function of dynamical regime in the tropics (whose PDF according to the 500-hPa pressure velocity is given Fig. 11h). In tropical convection (\(\omega_{500} < 0\) hPa·day\(^{-1}\)), \(C_{opaque}\) is strongly driven by the velocity of ascending air (25% to 45% increase from 0 hPa·day\(^{-1}\) to -100 hPa·day\(^{-1}\)), whereas \(C_{Thin}\) seems to be poorly dependent on it, with an almost constant cover around 40%. In subsidence, the mean \(C_{opaque}\) is also increasing when the air descending velocity is larger but with a wide range of variation from month to month (Fig. 11a). More strikingly, \(T_{opaque}\) and \(T_{Thin}\) (Fig. 11b) vary linearly with \(\omega_{500}\), with a small variability from month to month. \(T_{opaque}\) and \(T_{Thin}\) linearly
contribution from 20 hPa·day$^{-1}$ to -100 hPa·day$^{-1}$ from approximately 5 °C to -35 °C and are constant between 20 hPa·day$^{-1}$ and 70 hPa·day$^{-1}$ at 5 °C. This suggests that, locally, $T_{\text{T opaque}}$ and $T_{\text{T thin}}$ are invariant in each dynamical regime. Radiative cloud temperatures $T_{\text{T opaque}}$ and $T_{\text{T thin}}$ presented in Fig. 11b were built respectively from temperatures at altitudes $Z_{\text{T opaque}}$ and $Z_{\text{T top}}$, and from temperatures at altitudes $Z_{\text{base}}$ and $Z_{\text{T top}}$ (see Section 3.1). The linear decrease from 20 hPa·day$^{-1}$ to -100 hPa·day$^{-1}$ of $T_{\text{T opaque}}$ and $T_{\text{T thin}}$ is due to the cumulative effects of a rising of the altitude of "apparent cloud base" ($Z_{\text{T opaque}}$ for Opaque clouds and $Z_{\text{base}}$ for Thin clouds; see monthly mean 2°×2° gridded $Z_{\text{T opaque}}$ and $Z_{\text{T thin}}$ on Fig. 11c) and an elongation of the cloud vertical distribution which gives even higher $Z_{\text{T top}}$ (see monthly mean 2°×2° gridded distance of "apparent cloud base" $Z_{\text{T top}} - Z_{\text{T opaque}}$ and $Z_{\text{T top}} - Z_{\text{base}}$ on Fig. 11d). Figure 11e shows the distribution in dynamical regimes of $\varepsilon_{\text{T thin}}$. It increases from 0.31 to 0.42 between 20 hPa·day$^{-1}$ and -100 hPa·day$^{-1}$, being almost invariant from month to month, and it is around 0.32 in average in subsidence.

An interesting point that appears in these figures is, in the tropics, the very small variability in the relationship between cloud properties and $\omega_{500}$ in dynamical regimes between 20 hPa·day$^{-1}$ and -100 hPa·day$^{-1}$: standard deviation is around 2.5 % for $C_{\text{T opaque}}$, less than 2 % for $C_{\text{T thin}}$, around 2.5 K for $T_{\text{T opaque}}$, less than 3 K for $T_{\text{T thin}}$, approximately 0.01 for $\varepsilon_{\text{T thin}}$, around 350 m for $Z_{\text{T opaque}}$ and $Z_{\text{base}}$, 300 m for $Z_{\text{T top}} - Z_{\text{T opaque}}$ and 200 m for $Z_{\text{T top}} - Z_{\text{base}}$. So, a change in the large-scale dynamic regimes produces a change in the cloud properties and CRE that seem predictable. For example, if $\omega_{500}$ on a region changes from -40 hPa·day$^{-1}$ to -80 hPa·day$^{-1}$, $C_{\text{T opaque}}$ will increase by 8 % ($C_{\text{T thin}}$ will remain more or less constant), $T_{\text{T opaque}}$ will decrease by 10 K and $T_{\text{T thin}}$ by 7 K, and $\varepsilon_{\text{T thin}}$ will increase by 0.03. These cloud changes would increase the CRE by 17 W·m$^{-2}$, including 14 W·m$^{-2}$ from Opaque clouds (Fig. 11f). Because $C_{\text{T thin}}$ will remain more or less constant whereas $C_{\text{T opaque}}$ will increase with a decrease of $\omega_{500}$ in ascendance, the relative contribution of Opaque clouds to the total CRE will be increase with convection. This is why we see in Fig. 11g a decrease of the Thin clouds relative contribution from 20 hPa·day$^{-1}$ to -100 hPa·day$^{-1}$.
Because cloud properties seem to be invariants for dynamical regimes between 20 hPa·day⁻¹ and -100 hPa·day⁻¹, a change in the tropics of the large-scale circulation should lead to a predictable change in the CRE in regions that stay in this range of dynamical regimes, linked to the spatial distribution (both covers and altitudes) of Opaque clouds and Thin clouds.
sounded by CALIOP. For example, general circulation models suggest that a warmer climate will see a narrowing of the ascending branch of the Hadley cell (e.g. Su et al., 2014), which means less convective regions and more subsiding regions. This should result in a predictable decrease of the CRE, knowing the changes of $\omega_{500}$ for some part of the tropics.
6 Limitations of the OLR linear expression

In this study, from the direct measurement of the altitude of opacity for a spaceborne lidar, termed $Z_{\text{opaque}}$, we were able to infer the radiative temperature of Opaque clouds $T_{\text{opaque}}$, which we found linearly related to the OLR. We propose $Z_{\text{opaque}}$ as a good candidate to provide an observational constraint on the LW CRE and we tested the linear relationship at different scales from instantaneous to monthly means. In this section, we list possible sources of uncertainty.

6.1 Cloud radiative temperatures $T_{\text{opaque}}$ and $T_{\text{Thin}}$

The definitions of the cloud radiative temperatures $T_{\text{opaque}}$ and $T_{\text{Thin}}$ (Section 3.1) only take into account the apparent cloud edges seen by the lidar ($Z_{\text{Top}}$ and $Z_{\text{opaque}}$ or $Z_{\text{Base}}$). A temperature defined by a centroid altitude (Garnier et al., 2012) would better account for the vertical profile, and could give a better estimate of the equivalent radiative temperature. However, our results show that the CRE is mainly driven by $Z_{\text{opaque}}$ and $Z_{\text{Top}}$ above Opaque clouds and $Z_{\text{Base}}$ and $Z_{\text{Top}}$ above Thin clouds. Furthermore, observation-based studies from the Atmospheric InfraRed Sounder (AIRS) and CALIOP showed that the radiative cloud height is located near the “apparent middle” of the cloud (Stubenrauch et al., 2010).

The authors define the “apparent middle” of the cloud as the middle between the cloud top ($Z_{\text{Top}}$) and the “apparent” cloud base seen by the CALIOP lidar ($Z_{\text{base}}$ for Thin clouds and $Z_{\text{opaque}}$ for Opaque clouds), consistently with our own definitions (Eqs. (1) and (2)).

6.2 Multi-layer cloud and broken cloud situations

Plotting the results of Fig. 6 in single-cloud-layer situations (Fig. A4c,d) gives better correlation coefficients, with $R = 0.99$ for Opaque clouds and $R = 0.92$ for Thin clouds. This shows our linear expression does not capture non-linearities which can occur in multi-layer situations (Fig. A4e,f). As an example, all the occurrences far away above the identity line in Fig. 6a are due to multi-layer situations. For single columns with Opaque cloud, taking into account the optical depth of the thinner cloud which overlaps an Opaque cloud in the expression of $T_{\text{opaque}}$ improves the results for the multi-layer scenario from $R = 0.79$ (Fig. A4e) to $R = 0.86$ (Fig. A5). However, this subtlety adds complexity to the computation of $T_{\text{opaque}}$, and provides small improvements to a simple expression which already provides very satisfying results when considering all scenarios ($R = 0.95$ on Fig. 6a).

When clouds are broken, single lidar shots, having a 90 m diameter footprint, can fall on the edge of an Opaque cloud leading to signals from both cloud and the atmosphere and surface below the cloud in the same lidar profile. In this case an Opaque cloud can appear to be semi-transparent. Thus, the frequency of liquid clouds ($T > 0^\circ\text{C}$) classified as Thin clouds (Fig. 4c) may be exaggerated as most liquid clouds are optically dense and not penetrated by lidar. This misclassification does not affect the computation of OLR, as $\text{OLR}^{\text{\#}}_{\text{Thin}}$ derived from lidar observations when $T_{\text{Thin}}^\circ > 0^\circ\text{C}$ show excellent agreement with measurements made by CERES ($R = 0.94$; Fig. A6).

6.3 Evaluation of the OLR over Thin clouds

We saw that the theoretical linear expression of $\text{OLR}^{\circ}_{\text{Thin}}$ for a fixed $\varepsilon_{\text{Thin}}$ overestimates the simulated relationship, by up to $+10 \text{W}\cdot\text{m}^{-2}$ in many cases (Section 4.1). This is partly due to the linear theoretical expression not taking into account the scattering of the LW radiation within the clouds. This may partially explain why $\text{OLR}^{\#\text{LID}}_{\text{Thin}}$ is larger than the measured $\text{OLR}^{\#\text{CERES}}_{\text{Thin}}$ (Fig. 6b). However, we do not think this should substantially affect the global scale partitioning of $\text{CRE}^{\#\text{LID}}_{\text{Total}}$.
between \( \text{CRE}_{\text{opaque}} \) and \( \text{CRE}_{\text{Thin}} \) because replacing \( \text{CRE}_{\text{Thin}} \) by the difference \( \text{CRE}_{\text{Total}} - \text{CRE}_{\text{opaque}} \) only increases the contribution of Opaque clouds to the total CRE to 74 %, instead of 73 %. Also, the value of \( e^{\text{Thin}}_w \) used to construct \( \text{OLR}_{\text{Thin}}^{\text{LID}} \) does not account for Thin cloud single columns where no "Clear" bin is found below the cloud (these clouds are not present in the \( e^{\text{Thin}}_w \) PDFs of Fig. 4d). This happens when very low clouds are present in the lowest 480 m bin, and so, emissivities of Thin clouds close to the surface are not taken into account in the averaged \( e^{\text{Thin}}_w \). But since all these "missed" cloud emissivities are from clouds near the surface, their temperature is certainly close to the surface temperature and their LW CRE should be small. So, this effect should have no significant impact on the presented results.

Further, applying \( \text{OLR}_{\text{Thin}} \) Eq. (4) to \( 2^\circ \times 2^\circ \) gridded variables introduces errors since the equation is non-linear (the product of \( T^{\text{Thin}}_w \) and \( e^{\text{Thin}}_w \)) unlike Eq. (5) for the \( \text{OLR}_{\text{opaque}} \) which is linearly dependent on \( T^{\text{opaque}}_w \). However, the comparison of the computed gridded \( \text{OLR}_{\text{Total}}^{\text{LID}} \) against the measured \( \text{OLR}_{\text{Total}}^{\text{CERES}} \) has shown very good agreement.

Finally, since one of the objectives of the GOCCP product was to avoid false cloud detections during both nighttime and daytime conditions, the signal threshold chosen for cloud detection is quite large, meaning that high clouds with optical depths smaller than about 0.07 are absent from GOCCP (Chepfer et al., 2010, 2013). These subvisible cirrus clouds are therefore excluded from this study, but as their emissivities are very small (smaller than about 0.03), they would likely not impact our results.

### 6.4 Gridded OLR

Concerning gridded OLR, we used monthly mean \( \text{OLR}_{\text{clear}}^{\text{CERES}} \) from CERES-EBAF in Eqs. (4-5) instead of instantaneous \( \text{OLR}_{\text{clear}}^{\text{CERES}} \) from C3M since this product is only available up to April 2011. Clear sky OLR from CERES-EBAF data is derived only from measurements over Clear sky atmospheric columns which are generally drier than the clear part of a cloudy atmospheric CERES column. Because a drier atmospheric column leads to a stronger OLR (e.g. Spencer and Braswell, 1997; Dessler et al., 2008; Roca et al., 2012), \( \text{OLR}_{\text{clear}}^{\text{CERES}} \) from CERES-EBAF should overestimate \( \text{OLR}_{\text{clear}}^{\text{C3M}} \) from C3M on average. The diurnal cycle, which is taken into account in \( \text{OLR}_{\text{clear}}^{\text{CERES}} \) from CERES-EBAF but not in \( \text{OLR}_{\text{clear}}^{\text{C3M}} \) from C3M (since we only used nighttime observations) could also play a role in the difference. We found an increase of 0.6 W m\(^{-2}\) for the global mean \( \text{OLR}_{\text{Total}}^{\text{LID}} \) computed with \( \text{OLR}_{\text{clear}}^{\text{CERES}} \) from CERES-EBAF compared to \( \text{OLR}_{\text{Total}}^{\text{LID}} \) computed with \( \text{OLR}_{\text{clear}}^{\text{C3M}} \) from C3M for the 2008–2010 period.

Differences between \( \text{OLR}_{\text{Total}}^{\text{LID}} \) and \( \text{OLR}_{\text{Total}}^{\text{CERES}} \) could also be related to multi-layer clouds in atmospheric single columns, to cloud microphysical properties, and to differences in local atmospheric properties. However, using this very simple expression for the OLR give an excellent correlation (\( R = 0.95 \)) between monthly mean \( \text{OLR}_{\text{Total}}^{\text{LID}} \) and \( \text{OLR}_{\text{Total}}^{\text{CERES}} \) and a good agreement of the linear regression with the identity line (appendix C, 2D distribution of monthly means \( 2^\circ \times 2^\circ \) gridded measured and computed OLR is given in Fig. A6).

### 6.5 Sensitivity to \( Z_{\text{opaque}} \) and to the multiple scattering factor

We also checked the sensitivity of \( \text{OLR}_{\text{Total}}^{\text{LID}} \) to the uncertainty in the altitude of full attenuation of the lidar signal. To do this, we conducted a test by moving \( Z_{\text{opaque}} \) one bin up (480 m) in all Opaque single columns (as moving \( Z_{\text{opaque}} \) one bin down would have led to negative values for some \( Z_{\text{opaque}} \)). This changes the Opaque cloud radiative temperature, the \( \text{OLR}_{\text{opaque}} \), and so the \( \text{OLR}_{\text{Total}}^{\text{LID}} \). Results show that after this change the global mean \( \text{OLR}_{\text{Total}}^{\text{LID}} \) is decreased by 0.9 W m\(^{-2}\) (appendix D, Fig. A7a).
Finally, a fixed multiple scattering factor $\eta$ is used for the retrieval of the Thin cloud emissivity, whereas there is evidence of a dependence on cloud temperature (Garnier et al., 2015). This could also play an important role in the differences between computed $\text{OLR}^\odot_{\text{Thin}}^{(\text{LID})}$ and measured $\text{OLR}^\odot_{\text{Thin}}^{(\text{CERES})}$. We tested the sensitivity of variability in $\eta$ on the computed $\text{OLR}^\oplus_{\text{Total}}^{(\text{LID})}$ by modifying the value of $\eta$ from 0.6 to 0.5. This reduced the global mean $\text{OLR}^\oplus_{\text{Total}}^{(\text{LID})}$ by 1.1 W·m$^{-2}$ (appendix D, Fig. A7b), which we consider negligible compared to the global mean value of $\text{CRE}^\oplus_{\text{Total}}^{(\text{LID})}$ equal to 28.4 W·m$^{-2}$. 
7 Conclusion

Simple radiative transfer models that estimate outgoing radiation at the TOA from a limited number of variables are useful to build a first-order decomposition of climate feedbacks. Such simple models exist in the SW domain, but not in the LW domain because LW fluxes are sensitive to the cloud vertical distribution, making the definition of such a simple model more challenging. In this work, we propose a simple LW radiative model which derives the LW CRE from five variables: two describing Opaque clouds (Opaque cloud cover and Opaque cloud radiative temperature) and three which describe semi-transparent clouds (Thin cloud cover, Thin cloud radiative temperature, and Thin cloud emissivity).

The originality of our approach lies in how the cloud vertical distribution is described in this simple radiative transfer model. We have used three altitude levels which can be precisely measured by spaceborne lidar to describe the cloud vertical distribution within the simple radiative model. Our approach contrasts with techniques based on passive spaceborne sensors that retrieve effective cloud heights rather than profile information on the cloud vertical distribution. Our approach also contrasts with techniques based on full-profile lidar/radar measurements using 40 levels of altitude (or more) to describe cloud vertical distribution in the troposphere. In this work, we have taken advantage of the precision and accuracy of spaceborne lidar to describe cloud vertical structure, but have retained only three levels of altitude to describe the cloud vertical distribution. Considering three levels of altitude allows us build a simple radiative model, useful for first-order cloud feedback analysis, given that the more complex radiative transfer models using all altitude levels cannot be used for this purpose. We have selected the three levels of altitude that influence the OLR the most: 1) cloud top altitude $Z_{\text{top}}$, 2) the level of full attenuation of the lidar laser beam $Z_{\text{opaque}}$, in single columns containing an Opaque cloud, and 3) cloud base $Z_{\text{base}}$, in single columns containing semi-transparent Thin cloud. These three altitudes are first-order drivers of the LW CRE, and have been measured precisely and unambiguously over a decade with the CALIPSO spaceborne lidar.

Using radiative transfer computations, we found that the OLR above an opaque cloud can be expressed linearly as a function of the “Opaque temperature”: $\text{OLR}^{(\text{LID})}_{\text{opaque}} = 2.0 T_{\text{opaque}} - 310$, where $T_{\text{opaque}}$ is obtained from the combination of the cloud top altitude $Z_{\text{top}}$, the level of full attenuation of the lidar laser beam $Z_{\text{opaque}}$, and a temperature profile taken from a reanalysis product. This simple relationship predicts that if the altitude an Opaque cloud increases so as to decrease its $T_{\text{opaque}}$ by 1 K, then the OLR is decreased by 2 W m$^{-2}$. Using this linear relationship together with CALIPSO and CERES observations, we estimated that Opaque clouds, which cover 35 % of the ice-free ocean, contribute to 73 % of the global mean CRE whereas Thin clouds, which cover 36 %, contribute to 27 %.

We checked the robustness of this linear relationship against observations at two different space and time scales. Using instantaneous collocated observations from the CALIPSO lidar and CERES broadband radiometer data at the sensor spatial scale (20 km), we found a correlation coefficient of 0.95 between the lidar derived $T_{\text{opaque}}$ and the OLR measured by the broadband radiometer CERES. Averaging the same data monthly within 2° latitude × 2° longitude grid boxes, our derived OLR differs by 0.1 W m$^{-2}$ from the OLR measured by CERES.

To conclude, this paper proposes a simple approximate solution to the complex problem of radiative transfer in the LW domain, which could be used to explore first-order LW cloud feedbacks in both observations and climate model simulations. On the observational side, future work will analyze the inter-annual variability of the record collected by spaceborne lidars and broadband radiometers: CALIPSO/CERES in the A-train (10+ years), followed by EarthCARE (Illingsworth et al., 2014) to be launched in 2018. On the climate model simulation side, this new framework will be included in the Cloud Feedback Model Intercomparison Project (CFMIP) Observation Simulator Package (COSP; Boda-Salcedo et al., 2011) lidar simulator (Chepfer et al., 2008) and applied to climate model outputs in order to quantify the contribution of each cloud property to the simulated cloud feedbacks.
Appendix A: Radiative cloud temperature

Schematically, if we consider an optically uniform cloud, i.e. the LW optical depth $\tau_{\text{LW}}$ increases linearly through the cloud, with a cloud total LW optical depth $\tau_{\text{Cloud}}$, we can compute the upward LW radiative flux emitted by the cloud at the top of the cloud ($\tau_{\text{LW}} = 0$). Neglecting the cloud particle reflectivity in the longwave domain, from the integral form of the Schwarzschild’s equation, we can express the upward zenithal spectral radiance $I_{\uparrow}^1$ emitted by the cloud at the top of the cloud:

$$I_{\uparrow}^1_{\text{cloud}}(\tau_{\text{LW}} = 0) = \int_0^{\tau_{\text{Cloud}}} B_\nu \left(T(\tau_{\text{LW}})\right) e^{-\tau_{\text{LW}}} d\tau_{\text{LW}} \quad \text{[W m}^{-2}\text{sr}^{-1}\text{m}^{-1}] \quad (A1)$$

Considering a linear increase of the temperature with $\tau_{\text{LW}}$ from the cloud top to the cloud base ($T(\tau_{\text{LW}}) = k_1\tau_{\text{LW}} + k_2$) and integrating $I_{\uparrow}^1_{\text{cloud}}$ throughout the whole LW spectrum (using Stefan-Boltzmann law $\int B_\nu \, d\nu = \sigma T^4 / \pi$), we can write the LW radiance $F_{\uparrow}^{\text{LW}}$ emitted by the cloud at the top of the cloud as:

$$F_{\uparrow}^{\text{LW}}(\tau_{\text{LW}} = 0) = \int_0^{\tau_{\text{Cloud}}} \frac{T}{\pi} (k_1\tau_{\text{LW}} + k_2) e^{-\tau_{\text{LW}}} d\tau_{\text{LW}} \quad \text{[W m}^{-2}\text{sr}^{-1}] \quad (A2)$$

Assuming that the cloud emits as a Lambertian surface, the upward LW radiative flux $F_{\uparrow}^{\text{LW}}$ emitted by the cloud at the top of the cloud is given by:

$$F_{\uparrow}^{\text{LW}}(\tau_{\text{LW}} = 0) = \int_0^{\tau_{\text{Cloud}}} \sigma (k_1\tau_{\text{LW}} + k_2) e^{-\tau_{\text{LW}}} d\tau_{\text{LW}} \quad \text{[W m}^{-2}] \quad (A3)$$

Then, for specific values of coefficient $k_1$ and $k_2$, which determine the gradient of temperature in the cloud and the cloud top temperature (and so the cloud base temperature knowing $\tau_{\text{Cloud}}^{\text{LW}}$), it is possible to compute $F_{\uparrow}^{\text{LW}}(\tau_{\text{LW}} = 0)$ and then solve the equation $F_{\uparrow}^{\text{LW}}(\tau_{\text{LW}} = 0) = \varepsilon_\sigma (T_{\text{rad}}^1) = \left(1 - e^{-\tau_{\text{Cloud}}^{\text{LW}}}\right)\sigma (T_{\text{rad}}^1)$ to find the corresponding equivalent cloud radiative temperature $T_{\text{rad}}^1$.

Appendix B: Vertical distributions of clouds directly observed by CALIOP

For 3 regions, as for Fig. 4, Fig. A1 shows distributions of the distance between cloud top and $Z_{\text{opaque}}^1$ and the distance between cloud top and cloud base. In the 3 regions, when an Opaque cloud (Fig. A1a) is penetrated by the laser beam of the lidar, $Z_{\text{opaque}}^1$ is mostly found in the 1st km below $Z_{\text{Top}}^1$ (30% in the tropical convective region, 52% in the mid-latitudes region and 75% in the tropical subsiding region). The frequency distribution collapses after 1 km (note the logarithmic y-axis). The greater altitude differences between $Z_{\text{Top}}^1$ and $Z_{\text{opaque}}^1$ can be due to a more vertically spread cloud or to multiple cloud layers. If we look at the dashed lines, which represent the part of the PDF considering only profiles without multilayers, we can see that the curves of the 3 regions fall to zero around 4–5 km. This means that all the part of PDFs over 5 km are due to multi-layer clouds.

Regarding Thin clouds (Fig. A1b), we mostly found $Z_{\text{Base}}^1$ in the 1st km below $Z_{\text{Top}}^1$ (49% in the tropical convective region, 68% in the mid-latitudes region and 76% in tropical subsiding region). The frequency distribution collapses after 1 km (again, note the logarithmic y-axis). The part of the PDF of profiles without multilayer (dashed lines), i.e. single columns which contain only one optically thin cloud layer and so directly represent the geometrical thickness of Thin clouds, fall to zero around 4–5 km. This means, as for Opaque clouds, that all the part of PDFs over 5 km are due to overlap of multi-layer clouds. Furthermore, as PDFs collapse after 1 km in both figures A1a and A1b and for all regions, it suggests that the laser beam is almost every time totally attenuated when exceeding 1 km thickness.
Appendix C: Verification of the lidar-derived gridded OLR against CERES observations

Figure A7 shows the correlation between the OLR computed from lidar observations \( \text{OLR}_{\text{Total}}^{(\text{LID})} \) and the OLR measured by the CERES radiometer on-board the Aqua satellite on which we extract only footprints collocated with the CALIPSO ground track \( \text{OLR}_{\text{Total}}^{(\text{CERES})} \) for nighttime and over ice-free oceans on 2°×2° monthly means for the 2008. We found an excellent correlation \( R = 0.95 \) and the regression slope is near the one-to-one line which reinforces our confidence in this simple OLR expression to correctly estimate the observed OLR.

Appendix D: Sensitivity of the lidar-derived gridded OLR to \( Z_{\text{opaque}} \) and to the multiple scattering factor

Figure A8a shows the difference between lidar-derived gridded \( \text{OLR}_{\text{Total}}^{(\text{LID})} \) shown in Fig. 7a and the one which would be obtain if \( Z_{\text{opaque}}^{\dagger} \) was found 480 m higher. To do this, we replaced the altitude \( Z_{\text{opaque}}^{\dagger} \) of each Opaque cloud single column found with the lidar by the bin above, so the altitude of \( Z_{\text{opaque}}^{\dagger} \) is systematically increased by 480 m. We then recomputed \( \text{OLR}_{\text{Total}}^{(\text{LID})} \) in the exact same way as described in this paper. The effect of an increase in the altitude of \( Z_{\text{opaque}}^{\dagger} \) is a global mean decrease in \( \text{OLR}_{\text{Total}}^{(\text{LID})} \) by 0.9 W·m\(^{-2}\). Areas where \( \text{OLR}_{\text{Total}}^{(\text{LID})} \) is the most affected correspond to areas with large values of Opaque cloud cover (patterns for 2008–2015 period on Fig. 2a are quite similar to those for the year 2008) except for the stratocumulus regions off the West coasts of the African, the American and the Oceanian continents where \( C_{\text{opaque}} \) is large but where \( \text{OLR}_{\text{Total}}^{(\text{LID})} \) change is not very pronounced. A higher \( Z_{\text{opaque}}^{\dagger} \) increases the level of the radiative temperature of the Opaque clouds, so decreases this temperature and then weakens \( \text{OLR}_{\text{Total}}^{(\text{LID})} \). Since \( \text{OLR}_{\text{Total}}^{(\text{LID})} \) is not affected as much in the stratocumulus regions, this suggests that vertical temperature gradient where these clouds are founded must be weak.

Figure A8b shows the difference between lidar-derived gridded \( \text{OLR}_{\text{Total}}^{(\text{LID})} \) shown in Fig. 7a and the one which is obtain using a fixed multiple scattering factor \( \eta = 0.5 \) instead of \( \eta = 0.6 \). Decreasing \( \eta \), increases the retrieved emissivity of the Thin clouds by 0.05. Consequently, areas where Thin cloud cover is large and where they are high and cold, so where they have a strong cloud radiative effect, are regions where \( \text{OLR}_{\text{Total}}^{(\text{LID})} \) is the most affected by this change (in the multiple scattering factor), up to a decrease of 3.5 W·m\(^{-2}\) in the Indonesian region.

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**Opaque**

(a) \( Z_{\text{Top}}^{\dagger} - Z_{\text{opaque}} \)

- **Tropics** \( \omega_{\text{top}} < 0 \) hPa·day\(^{-1} \) (↑)
- **Tropics** \( \omega_{\text{top}} > 0 \) hPa·day\(^{-1} \) (↓)
- Mid-Latitudes (N & S)
- no multilayers

**Thin**

(b) \( Z_{\text{Top}}^{\dagger} - Z_{\text{base}} \)

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Fig. A1. Distributions of (a) the distance between cloud top and \( Z_{\text{opaque}} \) among Opaque clouds and (b) the distance between cloud top and cloud base among Thin clouds in three regions: same as Fig. 4. Dashed lines represent the distribution only among single columns.
where a unique cloud layer was found (no multiple cloud layers). Only nighttime conditions over ice-free oceans for the 2008–2015 period are considered.

Fig. A2. Comparison between observed and lidar-derived OLR, at CERES footprint scale, as a function of $T_{\text{Thin}}^\odot$ and $\varepsilon_{\text{Thin}}^\odot$. Results obtained from CERES (dots) and CALIOP (lines) collocated measurements. Theoretical expressions are from Eq. (4). Same results as in Fig. 6b but only for measurements where $\text{OLR}_{\text{Clear}}^\odot$ is close to 280 W·m$^{-2}$ selected ($\text{OLR}_{\text{Clear}}^\odot \in [275–285]$ W·m$^{-2}$), in order to only see the contribution of $T_{\text{Thin}}^\odot$ and $\varepsilon_{\text{Thin}}^\odot$ on the OLR. Only nighttime conditions over ice-free oceans for January 2008 are considered.
FIG. A3. Same as Fig. 7 but using $OLR_{\text{Total}}^{(LID)}$ from CERES-EBAF instead of $OLR_{\text{Total}}^{(LID)}$ from CERES-Aqua in the calculation of $OLR_{\text{Total}}^{(LID)}$. 
Fig. A4. (a) and (b) are the same as Fig. 6a and 6b. They are decomposed here into (c, d) single-layer cloud situations and (e, f) multi-layer cloud situations.

Fig. A5. As Fig. A4e but with multi-layer cloud considered in the computation of $T^l_{\text{opaque}}$, considering that the cloud layers above the optically opaque cloud (below) have an equivalent emissivity $\varepsilon_{\text{above}} = 0.3$: $T^l_{\text{opaque}} = (1 - \varepsilon_{\text{above}})T^l_{\text{below}} + \varepsilon_{\text{above}}T^l_{\text{above}}$ where

$$T^l_{\text{below}} = \frac{T^l_{\text{top, below}} + T^l_{\text{opaque}}}{2} \quad \text{and} \quad T^l_{\text{above}} = \frac{T^l_{\text{top, above}} + T^l_{\text{base, above}}}{2}.$$
Fig. A6. As Fig. 6b but only with $T_{Thin} > 0 \, ^\circ C$ which could be liquid broken Opaque clouds misclassified as Thin clouds.
Fig. A7. Comparison between observed and lidar-derived OLR at monthly mean 2°×2° gridded scale. Only nighttime conditions over ice-free oceans for the 2008-year period are considered.

(a) Sensitivity to $Z_{\text{Opaque}}^{1} = Z_{\text{Opaque}}^{1} + 480$ m

(b) Sensitivity to $\eta = \eta - 0.1$

Fig. A8. Sensitivity of the lidar-derived annual-mean gridded $OLR_{\text{Total}}^{(LID)}$ to the altitude of full attenuation of the lidar into Opaque clouds $Z_{\text{Opaque}}^{1}$ and to the multiple scattering factor $\eta$: (a) difference between $OLR_{\text{Total}}^{(LID)}$ of Fig. 7a and $OLR_{\text{Total}}^{(LID)}$ which would be obtain if $Z_{\text{Opaque}}^{1}$ was found a 480 m-bin upper and (b) difference between $OLR_{\text{Total}}^{(LID)}$ of Fig. 7a and $OLR_{\text{Total}}^{(LID)}$ which is obtain using a fixed multiple scattering factor $\eta = 0.5$ instead of $\eta = 0.6$. Only nighttime conditions over ice-free oceans for the 2008 year are considered.
References


