Interactive comment on “A Bayesian model to correct underestimated 3D wind speeds from sonic anemometers increases turbulent components of the surface energy balance” by John M. Frank et al.

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The present manuscript proposes a novel method to correct eddy covariance fluxes from sonic anemometers. It works by jointly estimating “true” standard deviation of components of wind field, a parameter related to the precision of the standard deviation of the un-corrected observations, and a matrix of correction parameters (which contains correction terms for different wind directions).

It is clear that a lot of work went into a paper and the results present a clear improvement over a previously used Kaimal correction. The method is innovative, however it is extremely slow to implement. (This may be solved by potential future numerical improvements or by an increase in computing power).

Before publication, several points need to be ironed out.

First, no cross-validation of the correction field has been performed. Such a cross-validation is recommended before the method can be generalized to other datasets.

Second, the MCMC chains are very short, even though they use more than a hundred of parameters. Short chains might be prone to misconvergence. In my practice, I needed hundreds of thousands of samples to achieve robust results for around just 10 parameters. Even though the results look similar for different priors, this shortcoming needs to be at least mentioned.

Some of the mathematical notation is confusing; for example the difference between the upper and lower case subscripts need to be better explained. In addition, more attention can be given to explaining the dimensionality of variables (e.g., scalar, matrix, vector).

I encourage the authors to take a final look at the paper to correct some typos. e.g., l. 103 statistics is singular not plural l. 107 data are plural not singular
Though it would be possible to conduct a statistical cross-validation of our model by using the other 95% of the available data, we decided against doing this. First, the 5% of the available data we used was equally distributed from the entire dataset, meaning it is effectively a random subsample and should be representative of any other subset of data selected for validation. We acknowledge that this is only an assumption. Second, as it is, the Bayesian analysis took $\approx 2$ months to complete, thus we decided not to run extra analyses for the purpose of cross-validation. Similar to our response to Anonymous Referee 2, we would have loved to analyze more of the available data, be it for a more extensive estimate of the posterior correction or for cross-validation purposes. But, we have to weigh the potential knowledge gained by analyzing another 5% or 10% of the available data against adding 2-4 months of computer run-time to complete this study.

Taking the reviewer's comments into consideration, we decided to use a different approach to validate the posterior correction by conducting a simple field experiment. The benefit of this is that we could both validate and test the reproducibility of our results. It is a powerful statement if the posterior correction can independently explain similar observations from a different field site, over completely different vegetation, and using different equipment. We also extended our methodology by testing a new manipulation (i.e., askew) which is unique from anything the posterior correction was optimized for. With regards to validation and reproducibility, we contend that this field experiment was a success. The results from the askew test were less definitive, illustrating that there is currently much uncertainty in the posterior correction that needs to be improved by testing more manipulations.

These changes are described in the methods (lines 265-286), results (lines 380-403), discussion (lines 580-613), and table 3.
are essentially multidimensional arrays. When the same letter appears as both an uppercase and lowercase subscript, this refers to the $c^{th}$ element of dimension C.

We conducted several preliminary Bayesian analyses, and used trace plots and tests for autocorrelation to determine that 10,000 steps was sufficient for convergence for most of the 138 state variables defining $\alpha_T$. Most of these parameters required little or no thinning to reduce autocorrelation between steps and could have remained as MCMC chains with 1,000-10,000 steps. Yet, since the goal was to create a complete 3D correction, we decided to thin all state variables equally. Even though diagnostic tests showed that all parameters, including those with high autocorrelation, appeared to converge within 10,000 steps, it is possible that these chains are still too short for proper convergence. One safeguard against this is confirming that the results from the three chains all result in similar posterior distributions (see section 3.3).

2.4 Validation experiment

We conducted a validation experiment of the posterior 3D correction at the Colorado State University, Agricultural Research Development and Education Center (ARDEC), Fort Collins, CO, USA (40° 39' 7.9" N 104° 59' 45.7" W) from October 7-14, 2016. Three CSAT3 sonic anemometers were mounted on an east-west boom 2 m above a pasture of short grass and $\approx$36 m south of a mature corn field. Typical winds at this site are from the north, so in this experiment we refer to cardinal u, v, and w where the measurements have been rotated to north-south (u), west-east (v), and down-up (w). One anemometer (S/N 0869) was vertically mounted in the center of the boom and aimed north, a second (S/N 1560) was 0.62 m to the east and horizontally mounted (i.e., 90° rotation around its u-axis) and aimed north, and a final instrument (S/N 2385) was 0.58 m to the west and mounted askew (Fig. S1). The askewing is unique to this validation experiment and can be defined with the unit vectors $u^{\text{askew}} = 2/3u - 1/3v - 2/3w$, $v^{\text{askew}} = 2/3u + 2/3v + 1/3w$, and $w^{\text{askew}} = 1/3u - 2/3v + 2/3w$. All wind velocity measurements were converted from sonic to cardinal coordinates, and all tilt angles were measured with a digital level to 0.1° precision such that any mounting imperfections were taken into account. Data were measured at 20 Hz on a CR3000 micrologger (Campbell Scientific, Inc.). In post processing, both the Kaimal correction and the posterior 3D correction were applied to the 20 Hz data. Data were summarized every 5 minutes as the standard deviation of wind velocity along the cardinal directions, $\sigma_u$, $\sigma_v$, and $\sigma_w$.

Differences between anemometers are presented as root-mean-square of the relative error (RMSE) between measurements from the manipulated anemometers and the vertically mounted one.

3.6 Validation of the posterior correction

The validation experiment was conducted during excellent fall weather with no precipitation, where winds averaged 2.0 ± 1.2 m s$^{-1}$, maximum sustained gusts were 7.8 m s$^{-1}$, 38% of the winds were from the northeast (45°) to north-northwest (337.5°), 25% of the winds were from the southeast (135°) to south (180°), and during the other times there were some occasional westerly winds. Results are summarized in Table 3. The RMSE differences between a horizontally mounted anemometer and a vertically mounted anemometer were large (12.6-16.5%) for uncorrected measurements. Applying the Kaimal correction to these anemometers reduced the RMSE differences in $\sigma_u$ and $\sigma_v$ (8.5 and 11.4%) but increased the difference in $\sigma_w$, (17.5%). Compared to the uncorrected data, the average posterior correction decreased the RMSE differences in all directions, though only the reduction in $\sigma_u$ (8.0-12.2%) was statistically lower (i.e., 95% credible interval). Compared to the Kaimal correction, the average posterior correction was larger for $\sigma_u$ but lower for $\sigma_v$ and $\sigma_w$, with the reduction in $\sigma_w$ (11.8-15.9%) being statistically lower than with the Kaimal corrected data. The RMSE differences between an askew mounted anemometer and a vertically mounted anemometer were

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small/moderate for \( \sigma_u \) and \( \sigma_v \) (6.7% and 11.3%) and large for \( \sigma_w \) (14.7%) for uncorrected measurements. Applying the Kaimal correction to these anemometers reduced the RMSE differences in all directions (4.4-13.5%). The standard deviations for the RMSE differences using the posterior correction was higher for the askew manipulation (1.5-2.4%) than they were for the horizontal manipulation (1.1-1.3%). Compared to the uncorrected data, the average posterior correction increased the RMSE difference for \( \sigma_u \) (6.8%) but decreased the differences for \( \sigma_u \) and \( \sigma_w \) (10.3% and 13.9%), though none of these changes were statistically significant. Compared to the Kaimal correction, the average posterior correction increased the RMSE differences for all directions, with the differences in \( \sigma_u \) (6.2-11.6%) and \( \sigma_v \) (7.2-13.5%) being statistically larger.

Sonic anemometer corrections should be verified and validated. There is an opportunity to statistically cross-validate the posterior 3D correction with subsets of the other 95% of available data; we decided against this because the 5% used was already partitioned equally throughout the full dataset, plus, analyzing multiple rounds of training and validation datasets would take additional months of computation. Instead of a statistical cross-validation analysis, we conducted a validation field experiment to determine if (1) our results are reproducible and (2) if they can explain other manipulations. From this, we first conclude that our results are reproducible. In both our main experiments at GLEES and the validation experiment at ARDEC, there was improved agreement between vertically and horizontally mounted anemometers when using the posterior correction versus the Kaimal correction or no-correction (Table 3). The largest differences between anemometers was for \( \sigma_u \) (11.1% and 16.5%, Fig. 2d, Table 3) which were reduced with the Kaimal correction (6.6% and 11.4%, Fig. 4d, Table 3) and then further improved with the posterior correction (4.4% and 9.8%, Fig. 10d, Table 3). In both analyses, the differences in \( \sigma_w \) were reduced with either correction, but the best performance was the Kaimal prior (Figs. 4b versus 10b, Table 3). Finally, in both cases the differences in \( \sigma_w \) were smallest using the posterior correction (Figs. 4f versus 10f, Table 3). Moreover, we justify our validation because it involved an independent dataset that was collected at a different field site, over radically different terrain and vegetation, and using anemometers with different serial numbers. We are less confident that our posterior correction can explain all manipulations. The differences in \( \sigma_u \) and \( \sigma_v \) between vertically and askew mounted anemometers were significantly better with the Kaimal correction (Table 3). It is important to note, however, that these differences were the smallest of all the comparisons (Uncorrected column in Table 3); i.e., it may be inconsequential that the Kaimal correction outperforms the posterior correction for measurements that were fairly good to begin with. Meanwhile, the difference in \( \sigma_w \) was large, though it is unclear if the posterior correction makes this significantly better or worse (Table 3). This lack of clarity means the askew manipulation cannot be used to validate or falsify the posterior correction. This is not surprising, because the posterior correction was estimated without data from or knowledge of such a unique manipulation, and as it is, much of the posterior correction contains a large uncertainty (Fig. 7a). Though the posterior correction is too uncertain to explain the askew manipulation, this does not mean our estimates of \( H + LE \) at various field sites are flawed because these estimates account for the fact that much of the posterior is uncertain. We expect that expanding our Bayesian analysis to include data from more manipulations, e.g. the askew example, would further constrain the regions of uncertainty found in the current posterior correction.

[Table 3]
(see supplemental pdf for Table 3)

Please also note the supplement to this comment:
http://www.atmos-meas-tech-discuss.net/amt-2016-145/amt-2016-145-AC1-supplement.pdf