Measurement of wind profiles by motion-stabilised ship-borne Doppler lidar

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Abstract

Three months of Doppler lidar wind measurements were obtained during the Arctic Cloud Summer Experiment on the icebreaker Oden during the summer of 2014. Such ship-borne Doppler measurements require active stabilisation to remove the effects of ship motion. We demonstrate that the combination of a commercial Doppler lidar with a custom-made motion-stabilisation platform enables the retrieval of wind profiles in the Arctic atmospheric boundary layer during both cruising and ice-breaking with statistical uncertainties comparable to land-based measurements. This holds particularly within the atmospheric boundary layer even though the overall aerosol load was very low. Motion stabilisation was successful for high wind speeds in open water and the resulting wave conditions. It allows for the retrieval of vertical winds with a random error below 0.2 m s\(^{-1}\), comparable to the measurement error of standard radiosondes. The comparison of lidar-measured wind and radiosoundings gives a mean bias of 0.3 m s\(^{-1}\) (2°) and a mean standard deviation of 1.1 m s\(^{-1}\) (12°) for wind speed (wind direction). The agreement for wind direction degrades with height. The combination of a motion-stabilised platform with a low-maintenance autonomous Doppler lidar has the potential to enable continuous long-term high-resolution ship-based wind profile measurements over the oceans.

1 Introduction

Profiles of wind speed and direction are one of the most fundamental quantities for meteorological studies. Radiosoundings are still the primary source of global wind profiles (WMO, 2014); however, unless exceptional measures are taken to enable simultaneous reception from multiple sondes, they can only provide a time resolution of the order of hours. This may be adequate to provide a reference measurement of general conditions, but for detailed studies of boundary layer processes continuous and much higher time resolution wind profiles are required. Furthermore, radiosounding stations for routine operational observations are mostly land-based. Observations at remote sites are very sparse and almost
non-existent over the oceans. Any additional observations in data-sparse regions are valuable to improve the initial conditions for numerical weather forecasts (Houchi et al., 2010; WMO, 2014; Baker et al., 2014) and for assimilation into reanalysis products for climate research (e.g. Dee et al., 2011).

Over the ocean, remote sensing with a ship-based Doppler lidar provides an attractive alternative to radiosoundings for obtaining profiles with a high time resolution (Tucker et al., 2009; Baker et al., 2014). However, a number of technical challenges must be overcome to obtain high quality measurements. Ship motion, both its mean horizontal velocity when underway and the high frequency motions induced by waves and, in this study, icebreaking, can introduce a mean bias and increase the random error of the raw measurements on a range of temporal scales. These errors may even be larger than the wind velocity being measured. In order to correct for the effects of ship motion, the constantly changing orientation and motion of the measurement platform must be compensated for. This can be done either by measuring the ship’s motions and correcting for this after the fact, or by actively stabilising the instrument for these motions. If the time taken to make a single along-beam Doppler velocity measurement is long enough for the ship motion to change significantly then active motion stabilisation of the instrument is required. This is why only a few studies have used Doppler lidar on ships (Hill et al., 2007; Wolfe et al., 2007; Pichugina et al., 2012). Improvements in technology along with decreasing costs make this an increasingly attractive approach.

Wolfe et al. (2007) and Pichugina et al. (2012) report on a deployment of the NOAA High Resolution Doppler Lidar (HRDL) at sea during the New England Air Quality Study in 2004, along with the first use of a motion compensation system. The motion system combined GPS data with 6-axis accelerometers and rate gyros integrated over time to determine the orientation and motion of the lidar in real time. This information was then used to actively compensate the orientation of the lidar’s scanning unit for the ship’s motion (Hill et al., 2007). The platform velocity component along the lidar beam was calculated and subsequently removed from the Doppler velocity measurement. A pointing accuracy of order 1° was achieved under typical conditions during the cruise. Subsequent deployments (Tucker
et al., 2009) improved on this, achieving an accuracy of $\approx 0.5^\circ$. The estimated noise introduced into each line-of-sight velocity measurement by the motion correction was 0.3 m s$^{-1}$; averaging over a 3 min interval reduced this to 0.015 m s$^{-1}$, with a mean bias of 0.05 m s$^{-1}$ (Pichugina et al., 2012).

Here we present measurements with a motion-stabilised commercial scanning Doppler lidar. Lacking real-time control of the scanning head orientation, as used by Wolfe et al. (2007) and Pichugina et al. (2012), we mount the lidar as a whole in a motion-stabilised platform. The instrument was operated near-continuously over a period of 3 months on a ship in the Arctic Ocean during the summer and autumn of 2014. The wind measurements are compared to 6-hourly radiosoundings and measurements from a sonic anemometer mounted on a mast over the bow of the ship. We give a description of the design and operation of the motion stabilisation platform together with the lidar in Sect. 2. Section 3 presents the evaluation of the lidar wind measurements, an investigation of the measurement error of the motion-stabilised instrument, and the effect of flow distortions caused by the ship. The paper closes with a discussion and summary in Sect. 4.

2 Measurements

The measurements presented here are drawn from the Arctic Cloud Summer Experiment (ACSE), part of the Swedish-Russian-US Arctic Ocean Investigation on Climate-Cryosphere-Carbon (SWERUS-C$^3$), which undertook a 3 month long cruise on the icebreaker Oden. Sailing from Tromsø, Norway, on 5 July 2014, the cruise followed the Siberian Shelf to cross the Barents, Kara, Laptev, and East Siberian Seas to arrive in Barrow, Alaska, on 19 August 2014. The return leg departed Barrow on 20 August 2014 and followed a similar route, slightly further north, back to Tromsø, arriving on 5 October 2014 (Fig. 1). The primary objective of ACSE was to study Arctic clouds and their relation to tropospheric vertical structure, meridional transport and the surface energy balance for a variety of surface conditions, from open ocean, through marginal ice and into dense pack ice. ACSE ran an extensive suite of in-situ and remote-sensing instrumentation.
throughout the full 3 months of the cruise (Tjernström et al., 2015). Here, we focus on measurements with a scanning Doppler lidar and 6-hourly radiosoundings.

### 2.1 Doppler lidar

The lidar used here is a HALO Photonics Stream Line scanning micro-pulsed Doppler lidar (http://halo-photonics.com/; Pearson et al., 2009) that was located on the roof of a container above the laboratory space on the foredeck of Oden (Fig. 2, left) at a height of 12 m a.s.l. The instrument operates at a wavelength of 1.55 µm and uses cloud droplets and aerosols as a tracer for air motion. Cloud layers with significant droplet concentrations produce full signal attenuation, prohibiting the acquisition of data above. Such liquid layers were frequently found near 400–500 m a.s.l. in this Arctic marine environment. The lidar’s range resolution is 18 m, with 533 range gates and a first measurement at 18 m maximum measurement distance of 9.6 km; the Doppler velocity resolution is 0.038 m s\(^{-1}\). An overview of the system parameters is presented in Table 1. Throughout the cruise the lidar was configured to undertake several different scan patterns on a fixed cycle. The wind profile scan ran every 10 min, using a 5-point measurement: a vertical beam and 4 off-vertical measurements at an elevation angle of 70° and azimuth angles at 90° increments. The measurement of velocity along each beam is comprised of 30 000 pulses at 15 kHz, and is thus an average over a 2 s interval. The time taken for the scanning head to move between consecutive beam positions is also approximately 2 s. All the individual measurements used in the calculation of a single wind profile thus take place within a period of approximately 20 s.

### 2.2 Ship-motion stabilisation

The lidar was stabilised against the pitch and roll of the ship by mounting it within a specially constructed motion-stabilised frame (Fig. 2, right). To minimise the torque required, the whole system is balanced so that the axes of rotation pass through the centre of mass of the instrument. The motion of the ship and of the lidar are measured with two Xsens MTi-700-G attitude and heading reference system (AHRS) sensors rigidly mounted to the outer-
and inner-most frames, respectively. The motion-control algorithm takes the raw measurements of the rates of rotation for pitch and roll from the ship-frame sensor (nominal accuracy $0.003^\circ$ at 10 Hz). It drives servo motors at the same rate but in the opposite direction to hold the inner frame steady against the pitch and roll of the ship. This will maintain the orientation with respect to the horizontal that it had when the system started up. In order to force the inner frame towards the horizontal, the specified rates of rotation are modified by the addition of factors proportional to the absolute pitch and roll of the inner-frame. The measurement of the inner-frame attitude uses the solution calculated internally by the Xsens AHRS via a proprietary algorithm which combines all its raw measurements using a Kalman filter (nominal accuracy $0.2^\circ$, precision $0.05^\circ$). The complete measurement and control cycle runs at 10 Hz. Both the lidar data logging system and the motion control system are synchronised hourly to UTC via the ship’s time server. Details on the motion-correction algorithm are given in Appendix A.

Approximately half of the ACSE cruise took place in sea ice where the ship’s pitch and roll are modest (typically less than $2^\circ$) but ship motions can be sudden when breaking ice; the other half was in open water, sometimes near the ice edge and other times hundreds of kilometres distant. Some extensive periods during the second leg were spent in open water under conditions of moderately high winds ($10$ m winds up to $17$ m s$^{-1}$) and waves heights up to several metres. The Oden is designed primarily for working within sea ice and lacks a keel; it thus has rather poor stability in rough seas and suffers substantial roll motions. Figure 3a shows a short portion of the time series of roll angles for the ship and the motion-stabilised lidar from 18 September, during the period of roughest seas encountered, when the greatest ship motion was experienced. The probability distribution of lidar roll angle for the 1 h period with greatest ship roll is shown in Fig. 3b. The maximum ship roll approaches $\pm 8^\circ$ with a period of approximately 8.5 s. The motion stabilised frame keeps the lidar within $0.3^\circ$ of horizontal 96.5 % of the time, and within $0.5^\circ$ of horizontal 99.3 % of the time. At no point does the lidar roll angle exceed $0.9^\circ$.

The residual attitude and 3-dimensional velocity of the stabilised inner frame were calculated and combined with the lidar beam orientation to correct the line-of-sight Doppler
velocity measurement for the ship’s velocity along the beam. **The largest tilts were associated with rotation of the lidar head prior to each new measurement.** This changed the centre of mass inducing a small rotation before the motion control and logging system detected and compensated for this. In principle the complete platform attitude and velocity solution could be obtained directly from the **internal solution of the Xsens AHRS**; however, we had no opportunity to calibrate the magnetic field sensors for the hard-iron distortions induced by the ship, and the Xsens compass heading thus suffered significant errors. We therefore utilised a combination of the high frequency attitude and motion calculated from the raw Xsens AHRS measurements of accelerations (**nominal accuracy** $2.5 \times 10^{-4} \text{ m s}^{-1}$ **at** 10 Hz) and rotation rates, and low frequency horizontal velocity and heading from the ship’s navigation data; the latter are derived from a GPS and gyro compass and have typical accuracies of order $0.02 \text{ m s}^{-1}$ for velocity and $0.5^\circ$ for heading. We calculate attitude and velocity following the complimentary filtering approach of [Edson et al.](1998); this method is routinely used to motion correct ship-borne turbulence measurements (e.g. [McGillis et al.](2001), [Brooks](2008), [Norris et al.](2012), [Yang et al.](2014), [Drennan et al.](2014), [Landwehr et al.](2015), [Prytherch et al.](2015). The ship’s mean horizontal velocity when underway can approach $6 \text{ m s}^{-1}$; the wave induced velocity perturbations in open water were a maximum of approximately $\pm 0.2 \text{ m s}^{-1}$ fore-aft, and $\pm 1 \text{ m s}^{-1}$ in the vertical and port-starboard.

Because the lidar Doppler velocities are 2 s averages, we use a corresponding 2 s averaged platform velocity to correct them; the standard deviation of the individual 10 Hz platform velocity measurements are also calculated as a quality control measure, in order to flag measurements for which the ship motion changes substantially during the lidar measurement interval, and to provide a measure of the noise added to the Doppler winds by the ship motion.

### 2.3 Lidar data processing

The signal-to-noise ratio (SNR) of the Doppler velocity measurement depends on the setup of the instrument and the availability of aerosols and cloud droplets to reflect the laser
beam and act as tracers for atmospheric motion. It is used to separate reliable data from signal noise (Pearson et al., 2009; Schween et al., 2014). Previous studies using HALO Doppler lidar suggest a SNR threshold ranging from $-18.2$ to $-23$ dB (Schween et al., 2014; Barlow et al., 2011; Pearson et al., 2009; Lane et al., 2013; Päschke et al., 2015; Hirsikko et al., 2014). However, these values were derived from measurements at mid-latitudes where aerosol load is generally much higher than in the Arctic. Following the approach of Päschke et al. (2015), we derived a conservative SNR threshold of $-16$ dB based on measurements under relatively steady wind conditions with a vertical wind velocity close to zero. Applying this threshold to our Arctic observations leads us to reject around 18% of data that would be accepted with the commonly used threshold of $-20$ dB. This amounts to rejecting a total of 75% of all individual data points that do not fulfill the SNR criterion. Note that data rejection varies greatly with altitude and atmospheric conditions, and is greatest in the free troposphere where the majority of rejected data points lie. This rejection rate is particularly great for our Arctic observations as we cannot rely on the abundance of scatterers that lead to generally better SNR in observations at mid-latitudes. It is likely that changing the telescope focal length from infinity to 1–2 km (Hirsikko et al., 2014) would improve data collection for conditions of low aerosol load as encountered during ACSE. Unfortunately, the older model of HALO lidar used in ACSE did not allow for overlap adjustment as easily as its successor, and this adjustment was therefore not made.

Wind speed and direction were obtained from the motion corrected HALO Doppler lidar measurements using the five-point geometrical wind solution and the 4-point sinusoidal fit method both described in Werner (2005), assuming no major changes or air motion occur within the scanning volume (Lane et al., 2013). The vertical wind is retrieved as an independent parameter for the sinusoidal fit (Werner, 2005). For the 4-point sinusoidal fit method, we applied the quality assurance criteria described in Päschke et al. (2015), i.e. we tests for horizontal homogeneity of the wind field (Eq. 13 in Päschke et al. 2015, we applied a threshold of $R^2 > 0.95$) and the collinearity of the Doppler velocity measurements used within one scan (Eqs. 14,15 in Päschke et al. 2015). For the latter, we ensured that measurements with gaps in the azimuth scan of larger than 210° were not
included for further data analysis, i.e. scans with less than three out of four points available for analysis.

We also investigated the influence of changes in the heading of the ship during individual scan cycles with and without applying the quality assurance criteria of Päschke et al. (2015). These criteria remove any dependence of wind speed on the change in the ship’s heading between the first and the last measurement used in the retrieval. The issue will be addressed in more detail in Sect. 3.1.

Continuous wind profiles could be retrieved up to a maximum altitude of 1600 m a.s.l. during cloud-free conditions. Data coverage is greatest in the lowermost 200 m (93 %) and decreases exponentially with height to 13 % at 1000 m. This is less than usually observed with the same type of instrument at mid-latitudes (Pearson et al., 2009; Päschke et al., 2015) due to the generally very low aerosol load in the Arctic (e.g. Lannefors et al., 1983; Heintzenberg and Leck, 2012; Birch et al., 2012). However, within the atmospheric boundary layer we yield data coverage comparable to previous studies. The average daytime maximum and minimum atmospheric boundary layer depths during the cruise were 576.3 and 81.4 m, respectively. Averaged over all observations, we find that the maximum height of useful wind data is around 100 m lower for cloudy (but not fully attenuating) conditions than for cloud-free conditions. Most of the observed clouds showed a base height of 300 m or less. Fog was frequently observed during the first leg of the cruise, with fewer fog cases encountered during the second leg. Such conditions typically lead to full attenuation of the lidar signal within the fog. The presence of multiple semi-transparent cloud layers allows for measurements of up to 3000 m on some occasions, leading to data coverage of 5 % at this altitude.

In order to assess the accuracy of the lidar wind retrievals, results have been compared to the 6-hourly radiosoundings. We used Vaisala RS92 radiosondes with a nominal ascent rate of 4 m s$^{-1}$. The manufacturer gives a total measurement uncertainty of 0.15 m s$^{-1}$ and 2$^\circ$ for wind speed and direction, respectively (VAISALA, 2015). Wind profiles from lidar and radiosoundings were interpolated to a common height grid. In addition, lidar winds were averaged over at least 2 scans in the first 30 min after the launch of the radiosonde.
To increase the amount of data for comparison, wind speed has also been compared to sonic anemometer measurements that were extrapolated to 75 m height following the method of Smith (1988) using the neutral drag coefficient, wind speed and surface and air temperatures.

A Metek USA-1 sonic anemometer was mounted approximately 20.6 m (8.6 m) above the water line (above the ship) on a lattice mast installed over the bow (Fig. 2, left). It features a heated sensing head that enables measurements even in severe icing conditions. The motion of the anemometer was monitored with an Xsens MTi-G-700 AHRS mounted at its base. The measurements were corrected for attitude and ship motion following Edson et al. (1998) as well as for the mean wind speed bias and flow height adjustment induced by flow distortion over the ship (Yelland et al., 2002; Yelland et al., 2005). The latter correction uses results from a computational fluid dynamics (CFD) modelling study of the Oden undertaken specifically for this campaign.

The height of 75 m for comparison to the lidar observations was chosen as few lidar measurements below 75 m height passed the quality-assurance criteria. Strictly speaking the logarithmic wind profile should extend only through the surface layer—approximately the lowest 10% of the atmospheric boundary layer. We would expect, however, that the wind speed in the lower half of the atmospheric boundary layer would be very close to that at the top of the surface layer. Here we restrict this comparison to cases for which the boundary layer depth exceeds 200 m so that the 75 m level is well within the lower half of the atmospheric boundary layer. The use of different atmospheric boundary layer heights did not yield significant differences in the results presented below. We estimate that any bias resulting from the extrapolation to this level is less than 10% of the wind speed at the height of the anemometer. The atmospheric boundary layer depth was determined from ceilometer measurements (Vaisala CL31) on Oden using the STRAT-2D algorithm (Morille et al., 2007; Morille et al., 2012). Measurements from the lidar were interpolated to the 20 min averaging interval of the sonic anemometer for the comparison.
3 Results

3.1 Lidar winds evaluation

Figure 4 shows scatter plots of wind-speed and direction for lidar vs. radiosonde using the 4-point sinusoidal fit solution at an altitude of 75 m a.s.l.; and lidar vs. sonic anemometer for wind speed only. The lidar and radiosonde wind directions agree very well for the 5-point geometrical wind solution ($R^2 = 0.96$, not shown) and the 4-point sinusoidal fit ($R^2 = 0.99$, see Fig. 4a). Both methods show negligible bias while a slightly better standard deviation is found for the 4-point sinusoidal fit (Table 2).

Extreme outliers (red points in Fig. 4a and b) were determined through the Grubbs test (Grubbs, 1969) and excluded from the linear fits. The values at around 0 and 360° in Fig. 4a are related to the periodicity of wind direction and do not represent erroneous measurements per se. The sinusoidal fit of 75 m lidar winds to the radiosonde winds (Fig. 4b) gives a larger intercept than that to the extrapolated anemometer wind speeds (Fig. 4c), with the lidar slightly underestimates the radiosondes for winds below about 4 m s$^{-1}$ and overestimates at higher wind speed – by about 2 m s$^{-1}$ at wind speeds of 16 m s$^{-1}$ (Fig. 4b). The lidar slightly overestimates compared with the extrapolated anemometer wind speeds, but by less than 0.5 m s$^{-1}$ at the greatest winds. $R^2 = 0.86$ for fits to both radiosonde and sonic anemometer winds. These results compare well with those of Wolfe et al. (2007); Wolfe et al. (2012), who compared profiles of zonal and meridional wind derived from full 360° velocity azimuth display (VAD) scans of the HRDL lidar with radiosonde profiles.

Linear fit parameters for both geometric and sinusoidal fits, as well as the number of measurements for the comparisons shown in Fig. 4 are given in Table 2.

Both the 5-point geometrical and sinusoidal methods to derive wind speed from the lidar data yield similar results. However, the sinusoidal fit is of advantage for our application as it only requires three input points to provide a solution. This increases the number of measurement intervals that can be used by around 25%. Consequently, sinusoidal fits have been used in the analysis of Doppler lidar measurements during the ACSE cruise. The blue
diamonds in Fig. 4a and b represent observations during which the motion-stabilization platform was not operating. While these are only five individual scans, they do demonstrate that an unstabilised instrument suffers far greater scatter in the measurements.

Figure 5a (blue lines) shows a height-resolved view of the correlation coefficient for the different comparisons between lidar winds and the soundings. The squared correlation coefficient for wind direction is approximately 0.99 and almost constant with altitude up to 400 m a.s.l., decreasing slightly to approximately 0.97 at 700 m a.s.l. Both bias and standard deviation for wind direction increase with altitude (Table 3). This is primarily the result of the drift of the radiosonde and the resulting decrease in collocation of the measurements. For wind speed the squared correlation coefficient’s minimum (0.86 to 0.89) is a minimum at the lowest altitudes and it improves with height to values comparable to that for wind direction. Too few data points are available at altitudes higher than 700 m a.s.l. for an effective comparison.

The squared correlation coefficient for the solution for wind speed improves from 0.86 at 100 to 0.94 at 400 m. In addition, the absolute value of the bias decreases from 0.5 to 0.3 m s$^{-1}$ (Table 3). The change from positive to negative bias with height marks systematically larger wind speed from the radiosoundings compared to the lidar measurement. A detailed overview of the correlation parameters is given in Table 3.

A similar improvement (with respect to values obtained using the quality assurance criterion of Päschke et al., 2015) in the comparison to the radiosonde is obtained when the change in the ship’s heading during one scan is restricted to smaller angles of 5 or 10° rather than 20°. This is expressed by the red and black lines for different cut-off angles presented in Fig. 5. Large changes of the heading of the ship shifts the azimuth angles used in the 4-point sinusoidal fit and leads to non-uniform intervals; this can lead to a degradation of the fit. Fig. 5b shows the normalised RMSE for the comparison of measurements with lidar and sounding at different altitudes. The strongest difference in normalised RMSE for the wind-speed comparison is found at lower levels when using quality assurance according to Päschke et al., (2015) or by restricting the change in the ship’s heading. At the uppermost altitudes considered here, using Päschke et al., (2015) pro-
vides lower normalised RMSE (7%) than the other criteria (11%). The lowest RMSE for wind speed of 1.5% is found at 200 and 400 m height. The comparison for wind direction (normalised RMSE of 3.5% - 5.5%) shows almost no sensitivity to the quality-assurance method and little variation with altitude even though Päschke et al. (2015) performs slightly better.

There are a number of effects that might influence the measurements at low level. The primary source of discrepancy is likely to be the fundamentally different nature of the measurements. The radiosonde follows a unique trajectory resulting from the sum of its buoyant ascent rate and the motion of the air it ascends through. Within the atmospheric boundary layer, turbulence superimposes chaotic perturbations about the mean flow; the largest scale eddies might result in very different trajectories depending on the precise time and location of launch. The lidar, on the other hand, calculates a wind profile from the air motions along each beam, which are separated both in time and in space – increasingly so with increasing altitude. While the sonic anemometer measures the velocity within a small localised sampling volume, with all components being sampled with a period (0.05 s) short enough to be considered instantaneous compared to the lidar. These effects, along with the increasing spatial separation between the radiosonde and the lidar may also cause the slight decrease in the correlation for wind direction with increasing altitude. An additional source of discrepancies is flow distortion around the ship; this would influence low-level measurements from both, with different effects on each due to their different locations.

The radiosonde will furthermore take time to accelerate to the ambient wind speed following launch, and can suffer from pendulum motions as the tether unwinds after launch (see Figure 3 in Marlton et al. (2015)). The latter effect can be particularly pronounced during high wind speed conditions and might affect the calculation of wind speed from consecutive GPS position estimates. The sondes are also launched close to the ship’s superstructure and depending on the ship-relative wind direction, may have been launched from within the local wind-shadow of the ship’s superstructure, delaying its acceleration to match the wind; for a short while after launch its motion can also be affected by the turbulent wake of the ship. The radiosondes’ low-level winds are also affected by the surface winds entered into
the proprietary sounding program; these were obtained from a sonic anemometer mounted on the foremast of the ship (Fig. 2), approximately 20.6 m above the surface (12.4 m above the deck). The wind speed measurements are corrected for flow distortion using the results of a computational fluid dynamics modelling study of flow over the ship following the approach of (Yelland et al., 2002; Moat et al., 2005); however for relative wind directions from aft, there will remain biases in these measurements.

Time series of wind speed and direction at an altitude of 100 m as measured with radiosonde and lidar are shown in Fig. 6. The gap from 4 to 12 August 2014 is due to a change in scanning setup of the lidar; no retrieval of wind speed and direction is possible during this period. During the first leg, the mean horizontal wind speed was 7.2 m s⁻¹, while a slightly larger value of 9.0 m s⁻¹ was obtained for the second leg. Wind direction showed high variability throughout the cruise. However, extensive periods of northerly and south-easterly winds can be identified. The relative difference presented in the bottom panel of Fig. 6 shows that wind direction generally agrees within 10 %. A stronger spread of values is found for the relative difference of wind speed with extreme values of up to 50 % difference. For the average wind speed of 6 to 8 m s⁻¹ and above, the difference between lidar and radiosonde is below 20 %. The mean (median) winds speeds at 100 m a.s.l. are 7.9 ± 3.4 (7.7) m s⁻¹ and 8.2 ± 3.5 (8.1) m s⁻¹ for the lidar and radiosonde, respectively. The relative difference in wind speed follows a Gaussian distribution (not shown) that is centred slightly off zero as winds measured by lidar are on average 0.3 m s⁻¹ lower than those inferred from the radiosoundings. A time series of the absolute differences in wind speed and direction reveal slightly increased scatter in the second part of the cruise during which higher wind speed has been observed.

A typical measurement day of 17 September 2014 is presented in Figure 7. Marine stratocumulus was present for the entire day with cloud base heights descending from 400 m to 200 m during the course of the day. The depolarisation ratio from the Doppler lidar reveals that ice (high values) is precipitating from liquid water clouds (low values) between 06 and 18 UTC. This is also in agreement with the measurements of vertical wind speed (negative values equal downward motion of due to
precipitation) and precipitation rate. Averages of 20 minutes of Doppler lidar measurements around the times of radiosonde launches at 06, 12, and 18 UTC are used for a profile-to-profile comparison of wind speed and direction in Figure 7e and f. No major differences are visible for the height range covered by the Doppler lidar apart from the wind speed in the lowermost 100 m for the 18-UTC sonde.

3.2 Measurement uncertainty

Following the approach of Frehlich (2001) and Pearson et al. (2009), an auto-covariance scheme has been used to determine the standard deviation of the vertical wind measurements with the motion-stabilised lidar during ACSE. The difference between the zeroth lag (first term in the auto-covariance) and the first lag gives a measure of the random error. This value has to be compared to the theoretical standard deviation of the instrument. The theoretical standard deviation has been estimated for SNR values between $-30$ and $16$ dB as described in (Eq. 7 in O’Connor et al. 2010). We used lidar specifications given in Table 1 and a signal spectral width of $2 \text{ m s}^{-1}$ (O’Connor et al., 2010). To determine the standard deviation for observations during ACSE, we only considered wind profiles during relatively steady wind conditions, i.e. during periods for which at least four consecutive lidar wind profiles showed a mean vertical velocity within $\pm 0.25 \text{ m s}^{-1}$ of zero.

The observed standard deviation of the vertical velocity as a function of SNR is presented in Fig. 8 together with the theoretical standard deviation calculated as described above. We find a constant random error range between 0.025 and $0.2 \text{ m s}^{-1}$ above $-16$ dB. This confirms our choice of a conservative SNR threshold of $-16$ dB according to the method of Päschke et al. (2015). SNR larger than 2 dB refer to cloud measurements. The error increases for lower SNR as the result of increasing signal noise. The experimental error exceeds the theoretical values but follows the expected change with SNR. Pearson et al. (2009) reported an error between 0.03 and $0.04 \text{ m s}^{-1}$ for SNR larger than $-10$ dB and errors that increase up to $0.4 \text{ m s}^{-1}$ at $-20$ dB. Our findings compare well with Fig. 2c in Pearson et al. (2009). The larger standard deviation we observe in our measurements is likely to be the result of the limitations of the motion stabilisation. This includes
residual small perturbations about the horizontal and the necessity of correcting the Doppler velocity measurements for ship motion only as an average over the 2 s measurement interval; during this time the high frequency ship motions, induced by waves or icebreaking, can change significantly.

**In addition to the random error we also investigated the measurements of vertical wind speed for systematic errors.** To determine the systematic errors of the measurements, we averaged all data for which steady wind conditions prevailed (about 3000 points at 200 m a.s.l. decreasing down to 200 points at 1000 m a.s.l.). While the average vertical velocity should be close to zero, we derived a mean value of $0.1365 \pm 0.005 \text{ m s}^{-1}$ for the height range up to 1000 m a.s.l. This means that measurements of vertical velocity will be slightly biased upwards. **This constant bias could be due to flow distortions of the ship that are discussed below.**

There are a number of potential sources of real bias in the measured vertical wind. One is the **projection** of horizontal wind into the vertical wind speed measurement as the result of imperfect motion stabilisation or misalignment of the lidar and AHRS units; the latter is estimated to be less than 0.5°. **A comparison of the output of the internal tilt sensor of the lidar with the XSens motion pack unit was performed during installation to level the two with respect to each other.** If the lidar alignment deviates from the horizontal by 0.3 or 0.9° (respectively the typical and maximum limits of the motion stabilisation) for a campaign mean wind speed of 8 m s$^{-1}$, the aliasing effect in the vertical wind will be $\pm 0.04$ or $\pm 0.12$ m s$^{-1}$, respectively. A source of a real upward air motion over the lidar is flow distortion over the ship. This is known to be a cause of significant bias in estimates of the mean wind (**Yelland et al., 1998**; **Moat et al., 2006b**; a) **Moat and Yelland, 2008**) and is now often corrected using the results of CFD modelling studies of the flow over ships (**Yelland et al., 2002**; **Moat et al., 2005, 2006b, 2006a**; **Moat et al., 2008**).

### 3.3 Effect of flow distortion

A CFD study of flow over the *Oden* was undertaken primarily in order to correct the wind measurements used to determine surface exchange coefficients from estimates of turbulent
fluxes. Here we use the CFD model to examine the biases resulting from flow distortion over the lidar location. **These calculations are not used as an active part of the lidar retrieval but rather as a means of assessing lidar data quality.** A commercial CFD code, VECTIS (Ricardo, 2014), was used to model the 3-dimensional flow over the Oden for a wide range of wind directions: every 10° from bow-on flow, through beam-on flow on both port and starboard sides. Additional runs were undertaken for flow from 120, 150 and 180° from the bow. All runs used a 10 m wind speed of 7 m s⁻¹, close to the campaign mean, with one additional (bow on) run being undertaken for \( U_{10} = 15 \) m s⁻¹. **In the model the stratification is neutral, free stream wind profiles are logarithmic with altitude and the far field vertical velocity is zero.** The model domain is centred on the ship and extends 1000 m in length, 1800 m in width, and 250 m in height. The number of computational cells within the domain was around 5 million. The cell size varied throughout the domain, with sizes of 0.12 to 0.25 m at the bow mast instrument location. This increased to around 20 m close to the edges of the domain. A grid independency study showed that a 50 % reduction of cell sizes over the whole domain only resulted in a 1 % change in wind speed bias with respect to the free stream flow at the bow mast anemometer locations.

The ship imposes a significant obstacle to the flow, and forces a strong vertical velocity in the lowest few 10 s of metres above the lidar, which varies with wind direction (Fig. 9a). This effect is slightly asymmetric about the bow because the lidar is situated towards the port side. At 75 m, the lowest level of robust Doppler wind measurements, the vertical velocity varies from about 0.2 to 0.4 m s⁻¹ for \( U_{10} = 7 \) m s⁻¹ and for wind directions for which the superstructure does not directly block the flow; this decreases approximately exponentially with altitude. The mean calculated vertical velocity above 75 m (roughly three times the obstacle height) is 0.04 m s⁻¹ for flow onto the bow, increasing to a little over 0.12 m s⁻¹ for beam-on flow. The CFD run with \( U_{10} = 15 \) m s⁻¹ for bow-on flow showed vertical velocity approximately double that at \( U_{10} = 7 \) m s⁻¹. The altitude-dependent vertical wind speed behaviour derived from CFD modelling was also observed in the Doppler lidar measurements, though with smaller magnitude probably as a result of temporal averaging of turbulent motions and vertical smoothing.
The vertical velocity at the top of the model domain at 250 m is set to zero; in reality a small vertical velocity might extend above this level. The normalised difference between the horizontal wind speed and the far field wind at the top of the domain is non-zero but less than 5% (Fig. 9b), whereas we would expect it to approach zero. This is due to the ship slightly constricting the flow within the domain. Overall the normalised bias (positive) in horizontal wind speed is less than 2% for all wind directions at altitudes above 75 m. Note that the CFD model results apply to the mean flow only and do not account for potential effects on turbulent flow.

4 Conclusions and summary

We have presented Doppler lidar measurements made during the Arctic cruise of the icebreaker Oden in summer and autumn 2014. In contrast to earlier shipborne observations in which data on ship motion was used to correct the alignment of the scanning unit of a Doppler lidar, we placed the instruments on a motion-stabilisation platform that enabled active stabilisation to within 0.3° of horizontal most of the time. Our setup allows for the retrieval of winds that are in good agreement with both radiosoundings and extrapolated measurements from an anemometer on the foremast. The comparison of the stabilised HALO Doppler lidar to independent measurements radiosoundings is comparable to that for land-based investigations (Barlow et al., 2011; Hirsikko et al., 2014; Päschke et al., 2015). Our results also compare well with previous ship-borne deployments of the HRDL Doppler lidar (Wolfe et al., 2007; Pichugina et al., 2012).

The fundamental measurement error of the lidar vertical wind speed was found to be in the range from 0.025 to 0.2 m s\(^{-1}\) for SNR above \(-16\) dB, which is smaller than the discrepancy between the mean wind speed derived from lidar and radiosoundings of 0.3 m s\(^{-1}\) (see Sect. 3.1). Overall, lidar measurements increase in reliability when the change in ship’s heading within a 20 s measurement cycle is at a minimum. The measurement range during fog-free periods was limited primarily by low aerosol concentration limiting the backscatter in clear air; measurements were obtained up to an altitude of 1000 m a.s.l., and up
to 3000 m a.s.l. when multiple layers of transparent clouds were present. Higher altitudes would be reached at mid-latitudes were atmospheric aerosol load is generally higher than in the Arctic (Wolfe et al., 2007; Pearson et al., 2009; Päschke et al., 2015). Data coverage was found to be comparable to previous land- and ship-based Doppler lidar observations. Ship-based Doppler lidar measurements provide a much more detailed, higher time-resolution view of atmospheric boundary-layer processes than can be achieved with radiosondes. At sea and on other moving platforms, motion correction or stabilization is necessary to derive reliable results from Doppler lidar measurements. Combining a commercial Doppler lidar with a custom-made motion-stabilisation platform as presented here forms a reliable and autonomous setup that could be placed on commercial or research ships to provide measurements for a number of applications including studies of marine boundary layer meteorology and air-sea interaction, wind mapping for proposed wind turbine installations, and validation of satellite retrievals such as that of the upcoming ADM-Aeolus mission (ESA, 2008) that features a space borne Doppler lidar. The near-field biases induced by air-flow distortion over the ship are potentially significant, but can and should be accounted for via modelling studies.

Appendix A: Motion-correction algorithm

Our determination of the residual linear velocity of the lidar follows the complementary filtering method of Edson et al. (1998). This utilises a ‘strap down’ motion sensing package that measures 3 axis linear accelerations and angular rotation rates at high frequency (typically $\geq 10$ Hz) within the frame of reference of the instrument, along with the compass heading and horizontal velocity of the ship at low rate ($\leq 1$ Hz), derived from the ship’s navigation data. In principle we require only the linear accelerations and compass heading here, since the platform is stabilised against pitch and roll; however, for the sake of completeness we implement the full calculation, summarised below.

In order to determine the high frequency time varying velocity we first determine the instantaneous orientation of the platform, rotate the measured accelerations from the in-
The orientation of the platform is defined by a set of Euler angles: pitch ($\alpha$), roll ($\beta$), and yaw ($\gamma$) — a set of rotations about non-orthogonal axes where each rotation is about one of the axes resulting from the previous rotation in a specific order. We use a right-handed Cartesian system with $x$ positive towards the bow, $y$ positive to port, $z$ positive upward; roll, pitch, and yaw are then positive for right-handed rotations about the $x$, $y$, and $z$ axes, respectively. In the Earth frame the $x$ and $y$ axes are conventionally positive to east and north, and compass heading is a left-handed rotation, thus $\gamma = 90^\circ$—heading. The orientation of the instrument with respect to the Earth frame is defined by applying the rotations in order: yaw, pitch, roll; to transform the measurements back to the Earth frame, the opposite rotations are applied in reverse order, in vector notation:

$$V = YPR V'$$  \hspace{1cm} (A1)$$

where $V$ is a vector quantity, the prime indicates the measurement frame, and $Y$, $P$, and $R$ are the yaw, pitch, and roll matrices, respectively, defined for rotations from the measurement to the Earth frame as

$$Y = \begin{bmatrix} \cos \gamma & -\sin \gamma & 0 \\ \sin \gamma & \cos \gamma & 0 \\ 0 & 0 & 1 \end{bmatrix},$$

$$P = \begin{bmatrix} \cos \alpha & 0 & \sin \alpha \\ 0 & 1 & 0 \\ -\sin \alpha & 0 & \cos \alpha \end{bmatrix},$$

$$R = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \beta & -\sin \beta \\ 0 & \sin \beta & \cos \beta \end{bmatrix}.$$  \hspace{1cm} (A2)$$

$\alpha$ and $\beta$ can be obtained directly from the XSens motion pack, or can be derived from the integration of the raw rotation rates about the $y$ and $x$ axes over time. To avoid accumulating errors from the integration of any bias or sensor noise the time series are high-pass filtered.
with a cosine roll-off between a pass-band limit of 1/60 Hz and stop-band limit of 1/120 Hz (i.e. periods of 1 and 2 min, respectively). The low frequency components of pitch and roll are obtained from the low-pass filtered components of gravity measured by the $x$- and $y$-accelerometers as a result of their tilt from the horizontal; the filter has complementary pass- and stop-band limits to the high-pass filter used above, i.e. a pass-band limit of 1/120 Hz and a stop-band limit of 1/60 Hz. The tilts of the $x$- and $y$-axes are given by $\theta = \sin^{-1}(a/g)$, where $a$ is the measured acceleration (after low-pass filtering) and $g$ is gravity. The low frequency contributions to the pitch and roll angles are then

$$\alpha_{lo} = \theta_x$$

$$\beta_{lo} = \sin^{-1}\left[\frac{\sin\theta_y}{\cos\theta_x}\right].$$  \hfill (A3)

For small tilts from the horizontal ($\theta < \approx 8^\circ$) we can use the approximation $\beta_{lo} = \theta_y$ introducing an error of less than 0.1°. The full pitch and roll angles are then obtained from the sum of high and low frequency contributions. The yaw angle is similarly obtained from the sum of the high-pass filtered rotation rate about the $z$-axis, and the low-pass filtered ship heading.

Having obtained the full pitch, roll, and yaw angles for each sample interval, the measured accelerations along sensor $x$, $y$, and $z$ axes are rotated into the earth frame, high-pass filtered, and integrated to obtain the high-frequency velocity perturbations about the ship’s mean motion. The low-pass filtered ship’s velocity in the Earth frame is added to these to obtain the final velocity of the measurement platform.

The lidar Doppler velocity measurement is corrected by adding the component of the mean platform velocity along the direction of the beam. We first rotate the platform velocity back into the instrument reference frame

$$V_{\text{inst}} = R' P' Y' V,$$  \hfill (A4)

and then into a reference frame aligned with the lidar beam. The relative pitch, and yaw angles are the negative of the lidar’s elevation and azimuth angles, and roll is zero. The
rotation matrices are calculated as in eq. (A2), and the velocity in the beam’s frame of reference is

\[ V_{\text{beam}} = P'Y'V_{\text{inst}}. \] (A5)

The velocity along the beam is then simply the first \( (x) \) components of the \( V_{\text{beam}} \) vector.

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References

ESA: ADM-Aeolus Science Report, available at: [http://www.esa.int/Our_Activities/Observing the_Earth/The_Living_Planet_Programme/Earth_Explorers/ADM-Aeolus](http://www.esa.int/Our_Activities/Observing the_Earth/The_Living_Planet_Programme/Earth_Explorers/ADM-Aeolus) (last access: 18 August 2015), 2014.


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Table 1. System parameters of the HALO Doppler lidar.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wavelength</td>
<td>1.5 µm</td>
</tr>
<tr>
<td>Pulse repetition rate</td>
<td>15 kHz</td>
</tr>
<tr>
<td>Sampling frequency</td>
<td>50 MHz</td>
</tr>
<tr>
<td>Points per range gate</td>
<td>6</td>
</tr>
<tr>
<td>Number of pulses averaged</td>
<td>30 000</td>
</tr>
<tr>
<td>Averaging time</td>
<td>2 s</td>
</tr>
<tr>
<td>Range resolution</td>
<td>18 m</td>
</tr>
<tr>
<td>Focus</td>
<td>Infinity</td>
</tr>
<tr>
<td>Weight</td>
<td>163 kg</td>
</tr>
</tbody>
</table>
Table 2. Statistics of the comparison between lidar and radiosounding as well as lidar and sonic anemometer on the bow mast. The lidar and radiosounding comparison has been conducted for a height of 75 m. The comparison of lidar and sonic anemometer has been performed for 75 m height with the sonic wind speed adjusted from 20 to 75 m following the method of [Smith, 1988].

<table>
<thead>
<tr>
<th></th>
<th>Wind speed</th>
<th>Wind direction</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Geometrical wind solution</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$N$</td>
<td>175</td>
<td>163</td>
</tr>
<tr>
<td><strong>Standard deviation</strong></td>
<td>$1.3 \text{ m s}^{-1}$</td>
<td>$20 ^\circ$</td>
</tr>
<tr>
<td><strong>Bias</strong></td>
<td>$0.5 \text{ m s}^{-1}$</td>
<td>$-1 ^\circ$</td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.85</td>
<td>0.96</td>
</tr>
<tr>
<td>Intercept</td>
<td>0.71</td>
<td>4.35</td>
</tr>
<tr>
<td>Slope</td>
<td>0.85</td>
<td>0.98</td>
</tr>
<tr>
<td><strong>normalised RMSE</strong></td>
<td>1.7%</td>
<td>4.2%</td>
</tr>
<tr>
<td><strong>Sinusoidal fit</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$N$</td>
<td>229</td>
<td>220</td>
</tr>
<tr>
<td><strong>Standard deviation</strong></td>
<td>$1.2 \text{ m s}^{-1}$</td>
<td>$10 ^\circ$</td>
</tr>
<tr>
<td><strong>Bias</strong></td>
<td>$0.4 \text{ m s}^{-1}$</td>
<td>$0 ^\circ$</td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.86</td>
<td>0.99</td>
</tr>
<tr>
<td>Intercept</td>
<td>0.48</td>
<td>3.53</td>
</tr>
<tr>
<td>Slope</td>
<td>0.89</td>
<td>0.98</td>
</tr>
<tr>
<td><strong>normalised RMSE</strong></td>
<td>5.9%</td>
<td>3.5%</td>
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</table>
Table 3. Statistics of the comparison between lidar and radiosounding at heights of 75, 100, 400, 600, and 700 m.

<table>
<thead>
<tr>
<th>Height (m)</th>
<th>Wind Speed</th>
<th>Wind Direction</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>75 100 200 400 600 700</td>
<td>75 100 200 400 600 700</td>
</tr>
<tr>
<td></td>
<td>229 226 182 90 47 37</td>
<td>220 219</td>
</tr>
<tr>
<td>STD (m s(^{-1}))/(°)</td>
<td>1.2 1.3 1.0 1.0 0.9 0.9</td>
<td>10 10 10 12 13 16</td>
</tr>
<tr>
<td>Bias (m s(^{-1}))/(°)</td>
<td>0.5 -0.3 -0.4 -0.3 0.0 -0.3</td>
<td>0 0 1 -1 2 5</td>
</tr>
<tr>
<td>R(^2)</td>
<td>0.86 0.88 0.94 0.94 0.96 0.96</td>
<td>0.99 0.99 0.99 0.99 0.97 0.97</td>
</tr>
<tr>
<td>Intercept</td>
<td>0.48 0.64 0.45 0.14 -0.48 0.15</td>
<td>3.53 5.12 -0.46 0.43 -5.78 -12.95</td>
</tr>
<tr>
<td>Slope</td>
<td>0.89 0.96 1.00 1.01 1.06 1.03</td>
<td>0.98 0.93 0.99 1.00 1.01 1.03</td>
</tr>
<tr>
<td>normalised</td>
<td>5.9 3.7 3.2 3.4 4.4 6.8</td>
<td>3.5 3.2 1.1 1.4 4.8 6.4</td>
</tr>
<tr>
<td>RMSE (%)</td>
<td>29</td>
<td></td>
</tr>
</tbody>
</table>


Figure 1. Cruise track of the legs from Tromsø to Barrow (red) and back (brown). Ice edges at the times of start and end of the cruise are shown in light and dark blue, respectively.
Figure 2. *Oden* foredeck (left) showing the lidar mounted within its motion-stabilised platform (right) and the Metek USA-1 sonic anemometer mounted on a mast over the bow of the ship.
Figure 3. (a) Time series of ship and lidar roll angles on 18 September 2014 (05:54:10–05:57:30). Horizontal dashed lines indicate ±0.5°. (b) Probability distribution of the lidar roll angle over the hour 05:00–06:00 on 18 September 2014. Red dotted lines indicate ±0.5°, dot-dashed lines indicate ±0.3°.
Figure 4. Doppler lidar evaluation: The sinusoidal fit solution is compared to data from radiosondes launched every 6 h from *Oden* for (a) wind direction and (b) wind speed, and the sonic anemometer on the bow mast (c). Number of points and linear fit parameters are given in Table 2; red points indicate outliers in wind direction. The blue diamonds show comparison points obtained when the stabilization platform was turned off.
Figure 5. Squared correlation coefficient (a) and normalised RMSA (b) of derived wind speed (black) and wind direction (red) from lidar vs. radiosonde for different altitudes. Squares, circles and diamonds refer to cut-off angles of 5, 10 and 20° in the change of heading of the ship during one scan. The blue line refers to findings obtained using the quality assurance criteria of Päschke et al. (2015).
Figure 6. Time series of lidar (black, every 50 min) and radiosonde (red, every 6 h) wind speed (top) and wind direction (middle) at 100 m a.s.l. The lower two panels show the relative and absolute difference for wind speed (blue) and direction (gray).
Figure 7. Example measurement of 17 September 2014: calibrated backscatter coefficients from ceilometer (a) and Doppler lidar (b), depolarisation ratio (c), vertical (d) and horizontal (e) wind speed, wind direction (f) from Doppler lidar, and precipitation amount from a precipitation sensor on the ship (g). The profiles in (e) and (f) show the comparison of horizontal wind speed and direction to the radiosondes launched at 06, 12, and 18 UTC. The ships average speed during that day was 0.5 and 4.5 m s\(^{-1}\) before and after 1500 UTC, respectively.
Figure 8. Standard deviations of the Doppler horizontal velocity determined from the zero leg impulse in the auto-covariance and the theoretical standard deviation (black line) for a signal spectral width of $2 \text{ m s}^{-1}$. The median standard deviation per SNR bin is shown as red line.
Figure 9. CFD study results for $U_{10} = 7 \text{ m s}^{-1}$, above the shipboard lidar location: (a) profiles of vertical velocity above the lidar for various wind directions (port and startboard, relative to the bow). (b) Profiles of the horizontal wind speed, normalised by the free-stream profile for various wind directions (port and starboard) with respect to the bow. The horizontal dotted line indicates 75 m above the surface, the lowest level of reliable Doppler velocity measurements. Data is shown only for altitude > 31.5 m, the approximate level of the first lidar range gate.