Applying receptor models Unmix and PMF on real data set of elements in PM for sources evaluation

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Abstract

Two advanced receptor modeling techniques Unmix and PMF were applied to a data set of daily measurements of 11 elements in particulate matters (PM) of 252 samples. Samples were collected every sixth day as a 24h sample in the 5 year period (1995 – 2000) in the coastal part of the Herceg-Nov town (Montenegro) of the sea costal side region (Southeast Adriatic Sea). In the vicinity of the sampling site road traffic is a permanent.

The application of the receptor models to find the emission sources in the reverse order, using data set of pollutants concentrations measured on the receptor, is not enough to get satisfactory real solution relying only on the results of the applied models even if used the state-of-the-art models such as Unmix and PMF. In this work we applied Unmix and PMF on dataset which already modeled by PCA and EF in order to show how many solutions could be find and how many errors could be made as well as we harmonized these advanced models to find the most realistic solution. The model Unmix has the ability to suggest the solution by self-modeling while PMF model can be adjusted to calculate the solution for the number of emission sources that we have set. Unmix found thirteen solutions in total for several combinations of species, but four solutions satisfy its criteria: Min $R^2 > 0.8$ and Min $S/N > 2$. The PMF model has given 3 possible solutions and by further analysis the best solution of four sources was selected. F-peak refinement enabled finding a more realistic solution. We noticed that for the species with many missing values but, their presence is not desirable because of its harmfulness such as cadmium in this work the knowledge of emission sources is very important. Due to their limitations Unmix
and PMF is not able to give the solution for such cases. Other simple model applied together with advanced models could help to solve similar problems.

**Key words:** Modeling, Unmix, PMF, real data set

**Introduction**

A state-of-the-art multivariate receptor models are applied in the diverse fields of environmentrics, chemometrics, geology and remote sensing. Multivariate receptor modeling is a term applied in the field of air quality for the solution of the general linear mixture problem. For conservative chemical species, i.e. those that do not undergo reactions in the atmosphere, the principle of mass balance is applied. The mass balance for species \( i \) can be written as:

\[
C_{ij} = \sum_{k=1}^{N} a_{ik} S_{kj} \quad i = 1, \ldots, m, \ j = 1, \ldots, n
\]  

(1)

In this equation, \( C_{ij} \) is the observed concentration of species \( i \) in sample \( k \), \( S_{kj} \) is the total amount of particulate mass from source \( k \) in sample \( j \) and \( a_{ik} \) it the composition fraction of species \( i \) from the source \( k \). In air quality studies, the units of \( C_{ij} \) are usually micrograms per cubic meter. Thus, since \( a_{ik} \) is a dimensionless mass fraction, the units of \( S_{k} \) are also micrograms per cubic meter.

Eq. (1) is the physical basis of all receptor models. \( C_{ij} \) is subject to random error and \( a_{ik} \) to random variations (Henry, 2002).

Unmix seeks to solve the general mixture problem where the data is assumed to be a linear combination of an unknown number of sources of unknown composition, which contribute an unknown amount to each sample. Unmix assumes that the data and the compositions of the sources are all strictly positive (because of the effects of errors, small values less than zero are allowed in order to reduce the bias in the results). Unmix further assumes that for each source there are some samples that contain little or no contribution from that source. For a given selection of species, Unmix estimates the number of sources, the source composition, and source contributions to each sample. The usual analytical approach to fitting the model in Eq. (1) is to find the values of \( a_{ik} \) and \( S_{kj} \) that minimize the weighted mean square error \( F \) (Henry, 2002) of the model:

\[
F = \sum_{i=1}^{m} \sum_{j=1}^{n} \left( w_{ij} C_{ij} - \sum_{k=1}^{N} a_{ik} S_{kj} \right)^2 \quad i = 1, \ldots, m, \ j = 1, \ldots, n
\]  

(2)

Unmix diagnostic edges plots are used to show how well-defined one or more edge is by the data. If the edge plots show that all the edges are straight and well defined, then the Unmix
results should be more reliable and should be preferred over the PMF results (Henry and Christensen, 2010).

The General Mixture Problem and the special case of multivariate receptor modeling are ill-posed problems. There are simply more unknowns than equations and thus there are many wildly different solutions that are all equally good in the least-squares sense. In a statistical way these problems are not identifiable. One approach to ill-posed problems is to impose conditions that add additional equations, which then define more realistic solutions to be closer to unique solution. The non-negativity conditions as additional conditions are imposed by the physical nature of the problem (Henry, 2001). Source composition and contributions must be non-negative but non-negativity conditions alone are not sufficient to give a unique solution. More constraints are needed (Henry, 1987). Under certain, rather mild conditions, the data themselves can provide the needed constrains (Henry 1997). This is how Unmix works.

Based on the multivariate factor analysis and the results in factor profiles and contributions, Paatero and Tapper (Paatero and Tapper, 1993; Paatero and Tapper, 1994; Paatero, 1997) established the advanced factor analysis method - positive matrix factorization (PMF). Several features are incorporated in this model:

- weights data points by their analytical uncertainties,
- constrains factor loadings and factor scores to non-negative values and thereby minimizes the ambiguity caused by rotating the factors,
- uses weighted least-squares fits for data,
- expresses factor loadings in mass units, which allows factors to be used directly as source signatures,
- provides uncertainties for factor loadings and factor scores.

In PMF, the matrix $X$ ($n \times m$) includes measured mass concentrations, and is represented as the sum of the product of $G$ ($n \times p$) and $F$ ($p \times m$) matrices and the residual matrix $E$ ($n \times m$), where $n$ is the number of samples, $m$ is the number of chemical species, and $p$ is the number of independent source types. This model can give a solution that can be displayed in matrix form:

$$X = G \cdot F + E \quad (3)$$

The object function $Q$ that is to be minimized is defined as:

$$Q = \sum_{i=1}^{n} \sum_{j=1}^{m} \left( \frac{e_{ij}}{u_{ij}} \right)^{2} \quad (4)$$
where \( u_{ij} \) is the uncertainty of the species \( j \) in a sample \( i \) and residuals \( \epsilon_{ij} \) i.e. the portion of the measured concentration.

In addition, non-negativity constraints should be fulfilled, meaning that all the elements in \( G \) and \( F \) are to be non-negative. The main process of the PMF is minimizing the \( Q \)-value which is defined in the Eq. (4) as the sum of square of the residuals \( (\epsilon_{ij}) \) weighted inversely with uncertainty \( (u_{ij}) \) of the data point (Polissar et al., 1998; Lee and Hopke, 2006).

The solution of Eq. (4) is obtained by iteration until convergence is reached.

Bootstrapping is an advanced analysis that examines the stability of solutions of the tested models. The bootstrap method is essentially based on resampling methods in which “new” data sets that are consistent with the original data are generated. Each “new” data set (which is essentially a subset of the original database), is decomposed into profile and contribution matrices, and the resulting profile and contribution matrices are compared with the base run (Eberly, 2005), giving the distribution for each species to evaluate the stability of the solution.

Numerous studies employing both the PMF and Unmix models have been done in recent years (Pekney et al., 2006; Poirot et al., 2001; Kim et al., 2004; Chen et al., 2007 in: Hegg et al., 2010).

Paatero’s positive matrix factorization (PMF) approach weights the data by the inverse of the measurement error for each observation. A major advantage of this approach is that the missing data can be included as observations with a large error. However, the minimization of \( F \) is still an ill-posed problem, or in other words, the model is not identifiable. Even the inclusion of the non-negative constraints does not provide an identifiable model. Paatero addresses this problem, which he named rotationally indeterminacy, by adding one or more user-selected parameters. Park et al., (2002) have used modern constrained minimization methods on \( F \) along with specific conditions, e.g. each source composition must have at least one species absent from that source. Finally, Paatero has generalized \( F \) in a natural way to include the estimation of even more unknown parameters associated with spatial variations (Henry, 2002).

Multivariate source apportionment models, Unmix and positive matrix factorization (PMF), often produce nearly the same source apportionment, however some investigations have shown that this is not always the case (Henry and Christensen, 2010). These models do not specify a minimum number of samples, but the stability of their solutions increases with the number of samples (Chen et al., 2007). In this study, we calculated sources composition and sources contributions of elements in PM using real data base.
The main aim of this study is to show that a simple application of the most advanced mathematical models may lead to erroneous conclusions because each of these models can provide a larger number of mathematically correct solutions. Which solutions are really true cannot be known only on the basis of the results obtained by modeling, even using models such as Unmix and PMF. Our goal was to apply these state-of-the-art models, respecting their criteria, on data-base previously submitted to other models; Principal Component Analysis (PCA) and Enrichment Factors (EA) to compare, to be able to finding the most accurate solution relying on Unmix self-modeling and PMF application to adjust and confirm the solutions found by Unmix.

Materials and Methods

The sampling site is situated only 10 meters away from the coast of the Adriatic Sea. Samples of PM were subjected to gravimetric analysis for determination of total mass concentrations and subsequently to elemental analysis for Fe, Mn, Ti, Pb, Cr, Cu, Cd, Co, Ni, Hg and Se. Suspended particles were collected using a high-volume Aerosol Sampler, AQUERO model 400XT sampling system with inlet for the total suspended particles, on boron-silicate fiberglass filters every sixth day as a 24h sample in the period of 1995 - 2000. The sampler was located in the town of Herceg-Novи (Fig. 8) 18°33' N, 42°27', Montenegro (Fig. 1). The meteorological station is part of the MED POL program. The nearest road is located about 100 m north of the meteorological station. There are no significant grassy areas around the meteorological station, and there is no considerable construction work in progress. The terrain surrounding the receptor is rocky with some small areas of soil (Đorđević et al., 2004). Filters were digested with HNO3 (ultra pure). A Flame Atomic Absorption Spectrometry (F-AAS), Varian AAS–Spectr AA 55 instrument, was used to measure the concentrations of Cd, Co, Cr, Cu, Ni, Pb, Ti, Fe and Mn. The concentrations of Hg and Se were determined by the hydride vapor AAS method (HV-AAS) (Đorđević et al., 2005). The maximum expanded uncertainty of measurements for all elements was about 5%.

The real data set of 11 trace elements in particulate matter (PM) obtained in 252 observations was analyzed by Unmix 6.0 and PMF 3.0. The applied Unmix and PMF models were available on the EPA Internet site (www.epa.gov).
Unmix and PMF used in this study do not limit the number of factors. The following initial operations were subjected to the Unmix model data: Suggest Exclusion, Initial Species, Additional Species including SAFER and Initial Points. PM was chosen for the total and for the normalization. The data was screened using the signal-to-noise ratio (Min S/N ratio) criteria higher than 2, estimated by Unmix. Only the component with S/N value greater than 2 will be used for sources estimation. The agreement between the true and estimated source contribution (Min R² greater than 0.8) was considered as well (Henry, 2003, EPA/600/R-07/089).

Applying of PMF model the procedure of Polissar et al. (1998) was used in this study to calculate uncertainties in the species concentrations. Briefly, for the data below detection limit (DL), the concentrations were replaced with the value DL/2 and the uncertainty was set as $\frac{5}{6} DL$. For the missing data, concentrations were replaced by the geometric mean and the respective uncertainty was set at four times of this mean concentration. At the first set up all elements are labeled as Strong, since (the signal/noise ratio) S/N > 2 for all of them. Based on input data statistics, residuals show bimodal distribution in the case of Ni, Mn, and Hg, so their uncertainties are increased labeling them as Weak. Selenium is excluded from the model because of a very small contribution and the correlation factor, while for cadmium more than 50% of samples are below the detection limit. The Q value represents the goodness-of-fit and assesses how the model fits the experimental data. Qtrue is calculated taking into account all data points while Qrobust is calculated accounting for outlier points. Data with scaled residuals above 4 are regarded as outlier points. Evaluation of the validity of a solution is possible by using the G-space scatter plot. Scatter plot of one versus the other factor may indicate the existence of a rotational ambiguity. Namely, if the points on this graph fill the entire solution space evenly then the edges of the Scatter Plot correspond to axes. If this is not a case it is indication that there is rotational ambiguity and should be considered the possible rotation of the solution, using the function Fpeak. The F-peak functions is used to rotate the data set, make fine tuning and improvement of the model in the case of data with high noise (positive values F-peak) or clean data (negative values F-peak). Normally, the default settings give satisfactory results, but in some cases subsequent adjustments are needed. To ensure the robustness of statistics, 300 bootstrap runs were performed, while the default value of the minimum correlation (R-Value) of 0.60 was used.
Results and Discussion

We applied the Unmix and PMF models on dataset from our previous work regarding trace elements in the PM (Đorđević et al., 2005). Fig. 2 shows the comparison of measured and the predicted concentrations of trace elements in PM through time series and Min R^2. Model Unmix did not calculate R^2 values for Cd, Co, Hg and Se and neither satisfactory solution included these elements since these variables contain a large number of missing values and outliers. Min R^2 values are given in Table 1.

From statistical parameters displayed for each species, after input data and the following operations: Suggest exclusion, Influential points, Initial species, Additional species and SAFER, Unmix finds six combinations of species that give any kind of solution (Table 2). Min S/N for each principal component and Min R^2 of all combinations of elements estimated by Unmix was selected as good solutions that are in accordance with the Unmix criteria (Henry, 2003). Thirteen solutions in total were found, but four solutions satisfy the above criteria, signed in bold in Table 2. The standard deviation of variable (sigma) is the criterion for evaluation whether the variable eligible for modeling or not. The sigma-based parameters (Significant/Strong Species in Sources) for each of satisfactory solution are also given in Table 2.

Taking into account the calculated good solutions presented in Table 2, the Edges plots were done for these solutions (Fig. 3). The source profile of the solutions chosen according to the criteria S/N > 2 and R^2 > 2 are given in Fig. 4.

In the first solution (combination of species Mn-Ti-Pb-Cr-Cu, 3 Sources Solution) the second and third source are well defined by many points on the y-axis while source 1 has just a few points on the x-axis. Pb is strong in the first source and this source can be attributed to traffic. In the second source Cr and Cu are strong and Ti and Mn are significant. This source can be re-suspension of elements previously settled from anthropogenic sources. In the third source neither element is strong or significant.

The second satisfactory solution is for Fe-Mn-Ti-Pb combination of elements it also found 3 sources (Table 2, Fig. 4b) and does not show good accumulation of points on the x and y axes (Fig. 3). This solution has the best values of Min R^2 and Min S/N compared to all combinations. The first and the third source contain Pb which is a tracer for traffic. In the third source Pb is
strong, and it is reasonable to associate this source with traffic, while the first source could be local re-suspension. The second source in this combination could be a long range transport of Saharan dust since it contains crustal elements.

The third solution (combination of species Fe-Mn-Ti-Pb-Cr-Cu-Ni, 4 Sources Solution) shows the edges on the y-axis defined by many points for the third and the fourth source, but the x-axis has just a few points (Fig. 3).

In the fourth solution (combination of species Fe-Mn-Ti-Pb-Cr-Cu, 3 Sources Solution) good accumulation of points are on the y-axis, for sources 2 and 3 while the x-axis has just a few points for source 1 (Fig. 3).

In the third and the fourth solution, the sources where Pb is strong can be attributed to traffic; namely, source 3 for Fe-Mn-Ti-Pb-Cr-Cu-Ni combination (Table 2, Fig. 4c) and source 1 for Fe-Mn-Ti-Pb-Cr-Cu combination (Table 2, Fig. 4d). Another source in which Pb is present as significant but not strong could be re-suspension. Source 4 for Fe-Mn-Ti-Pb-Cr-Cu-Ni combination and source 2 for Fe-Mn-Ti-Pb-Cr-Cu combination could be attributed to re-suspension, probably from various locations depending on wind directions. Factors containing Cr and Ni indicate the existence of an anthropogenic emission source in the region (Đorđević et al., 2005).

In our previous work (Đorđević et al., 2005) we applied the PCA method on this data set and 4 significant groups of sources contributions were found. The following contribution sources were identified: re-suspension combined with re-suspended Saharan dust that had previously settled (Fe, Mn, Ti) and settled combustion products mostly from traffic, and probably some local stationary source (Cu, Pb). The remaining three factors represent the following combinations F2 by Cr and Ni, F3 by Cd and Se and F4 by Hg and Co.

The EF model revealed that in the region of the investigated receptor, the main contribution source of Fe, Mn and Ti is the process of local re-suspension and that local re-suspension has no influence on the content of Se in the atmospheric aerosol. The re-suspension is the dominant emission source of Cd from the south-southeast direction from the nearby peninsula (Luštica) but this source is not permanent (Đorđević et al., 2005).

The application of positive matrix factorization (PMF) to solve the number and profile of the sources applied to the same database resulted in obtaining possible solutions for 3, 4 and 5 sources. For 6 or more sources the model does not find the convergence of the functions Q,
which implies that the model did not find any minima. Varying simulation conditions did not contribute to significant improvement, even when the uncertainty is significantly increased. Therefore possible solution should be sought among three possible cases. Table 3 shows the categories of elements and the $R^2$ values for each of the three possible solutions. Each of the possible solutions obtained by PMF analysis will be considered. Fig. 5 shows $F$ peak strengths for 3 sources solution (Fig. 5a), 4 sources solution (Fig. 5b) and 5 sources solution (Fig. 5c).

3 Sources Solution: The relatively good correlation was obtained only for Cr and Pb, while bimodal distribution is still present in the case of Co, Ti and Fe. Also, significant outliers are present in the model. In addition, G-Space plots show considerable rotational ambiguity between the sources 1 and 3. Rotational ambiguity, which was found between the sources 1 and 3, decreases when the value of Strength factor reaches -1.2 (Fig. 5a). This is mostly reflected in the increase of Ti concentration in the source 2. However, such large values for $F_{\text{peak}}$ is unlikely because the quality of the fit decreases rapidly. The usually dataset rotations are generally much smaller and they are close to the basic solution.

However, a small degree of correlation between the model and database indicates that the model with three sources is insufficient to adequately describe a number of sources. In this case, only Co, Ni and Fe show relatively good interquartile range of about 20%, while other species show considerable variation and therefore represent a less stable solution. This is especially pronounced in the case of Hg, Cr and Mn. Also, in some cases (Hg, Ti) base run values are not within the interquartile range in the bootstrapping of results. This is probably a consequence of assuming the model with only three sources. Profiles of sources are given in Fig. 6.

4 Sources Solution: The model with four sources shows a significantly better correlation with measured concentrations of elements. Although the agreement of time series for Ti and Cr is excellent ($R^2 > 0.95$), and for Pb satisfactory ($R^2 = 0.70$), in the case of other elements there are still episodes with very high concentrations that this model cannot fit. It should be noted that Cu shows very good agreement between the predicted and observed concentrations, but the
existence of outliers have reduced the correlation to 0.34. A small degree of correlation in the case of Co is the result of a significant number of measurements below the detection limit. Bimodal distribution is still present in the case of Ni and Hg. G-Space plot shows that there is a rotational ambiguity between sources 1 - 3 2 - 3, 3 – 4.

For a model with four sources, rotational ambiguity disappears when the F-Peak strength reaches -0.8 (Fig. 5b). This rotation is mostly reflected in the increase of Ti content in source 1, and largely in sources 2 and 3. On the other hand, this may just mean that the content of titanium in this solution is divided among several sources. As in the case of a solution with three sources, a significant rotation of the dataset (Fpeak = -0.8) is less likely. It is necessary to consider these results carefully and determine whether there is justification for it to be included in further solving of the composition of the sources.

Interquartile range of solutions obtained by bootstrapping in the case of Fe, Pb, Cu and Cr are about 20%, while in the case of other species this range is much higher indicating the instability of the solution. Base run values which are not within the interquartile range in the bootstrapping of the results are, in the case of Cu, Mn, Pb and especially Hg, calculated by the model only in the fourth source.

5 Sources Solution: The model and data from the database show agreement ($R^2$) over 90% for Cr, Ti, Fe and Pb, while just over 50% for Mn. The model also fits Cu real data very well, and the correlation of 0.47 is caused by significant outliers that are related to individual episodes of Cu emissions. In spite of the increased uncertainty Mn, Ni, Co and Hg show a lack of fit.

G-Space plot only shows some rotational ambiguity in the case of sources: 2 – 5, 3 – 5 and 4 – 5. The F-Peak in the range -2 to 2 (Fig. 5c) showed the most impact on the sources of Cu, especially at higher strength values, while the ambiguity between the sources mentioned above still exist. The Peak F-curve is generally symmetrical in the examined interval.

In the case of five sources there are also unmapped results, suggesting a reduced stability of the solution. In general, the most stable solutions are obtained for those elements that are present in the source with the highest percentage. In these cases, the distribution of solutions obtained by bootstrapping lie in the range of 15% of the concentration calculated in the base run. This is the case for Fe, Pb, Ti. A slightly worse result of the bootstrap analysis is obtained for Cu, Mn, Cr, Co and Ni (bootstrapping distribution of solutions equal or higher than 20%). The least stable solution is for Hg with considerable dispersion in the bootstrap analysis solutions.
When discussing the number and origin of pollution sources, it is preferred to take into account the real situation on the field. In this case the following sources that contribute to the overall PM deposition can clearly be predicted: marine aerosols, traffic, re-suspension from the ground, probably some local stationary source, as a shipyard located in the vicinity. Based on these obvious sources, PMF analysis solution with only three sources is exempt from further consideration.

In the case of PMF solution of five sources it may be noted that source No. 5 (Fig. 8), in which Co, Cu, Ni and Mn are present, can be described rather as a splitting factor than as a separate source. The most realistic solution that is imposed upon a detailed analysis is the solution with four sources (Fig. 7).

Identification of sources was carried out and it agrees with the results of the Enrichment Factors analysis well (Đorđević et al., 2005). The F-peak profiles shown in Fig. 7 in rotation of data set for -0.8, increase the contents of Ti, in the case of sources 2 and 4.

Source 1 has been identified as re-suspension in combination with the long-range transport of Saharan dust. The prevailing wind directions are over open sea (Đorđević et al., 2005).

Source 2 is attributed to the re-suspension, indicated in our previous work. Titanium found by F-peak is in better accordance with the EF analysis (Đorđević et al., 2005).

Source 3 corresponds to the composition of the particles that come from some anthropogenic source.

Source 4 with the highest content of Pb, is characteristic for urban traffic. F-peak is increasing the value for Ti which is in better agreement with the traffic profile.

Conclusion

In this work we applied state-of-the-art mathematical models Unmix and PMF on database previously modeled using more simple models (PCA and EF) to be compared. In this study we have shown that only application Unmix and PMF for sources apportionment is not guarantee to obtain the unique realistic solution. Thirteen solutions in total were found, but four solutions satisfy the Unmix criteria: three solutions with three sources and one with four sources. In terms of modeling all four solutions found by Unmix are satisfactory. PMF model has given three possible solutions: one with three sources, one with four sources and one with five sources. By further analysis of the results of PMF model the best solution with four sources was selected. F-
peak refinement was enabled to find a more realistic solution. Also we have shown that due to their limitations Unmix and PMF were unable to calculate Cd and Se in used database, due to large number of missing values. For example, although the presence of cadmium in terms of concentration is negligible and there are many missing values the knowledge of emission sources is very important regarding its harmfulness. The simple model of EF applied could help to solve similar problem. For obtaining the best results using Unmix and PMF models our recommendation is to start modeling by Unmix relying on its self-modeling to estimate all possible types of sources and then apply PMF for confirmation. For the species that are important and that cannot be modeled by advanced models like Unmix and PMF should be apply other, even, the simple model.

Acknowledgment
The authors gratefully acknowledge the financial support of the Ministry of Education and Science of the Republic of Serbia, which supported this research within the project 172001. The authors are gratefully acknowledged to Saša Savić as well, for language improving.

References


Tables

Table 1. $R^2$ values obtained by Unmix of measured and the predicted concentrations of PM and trace elements in PM

<table>
<thead>
<tr>
<th></th>
<th>PM</th>
<th>Fe</th>
<th>Mn</th>
<th>Ti</th>
<th>Pb</th>
<th>Cr</th>
<th>Cu</th>
<th>Ni</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R^2$</td>
<td>0.46</td>
<td>0.75</td>
<td>0.92</td>
<td>0.66</td>
<td>0.83</td>
<td>0.40</td>
<td>0.99</td>
<td>0.00</td>
</tr>
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</table>
Table 2. All combination of elements for solutions obtained by calculation by Unmix

<table>
<thead>
<tr>
<th>Combination of species</th>
<th>Number of sources</th>
<th>Min R²</th>
<th>Min S/N</th>
<th>Significant/Strong Species in Sources (sigma-based)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mn-Ti-Pb-Cr-Cu</td>
<td>3</td>
<td>0.84</td>
<td>2.49</td>
<td>Source 1: *Strong – Pb; Source 2: *Strong - Cr, Cu, **Significant - Ti, Mn; Source 3: *Strong – None, **Significant - None</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>0.89</td>
<td>1.94</td>
<td></td>
</tr>
<tr>
<td></td>
<td>5</td>
<td>0.90</td>
<td>1.59</td>
<td></td>
</tr>
<tr>
<td>Cr-Cu-Pb-Ti-Mn-Se-Cd-Co-Fe</td>
<td>3</td>
<td>0.68</td>
<td>2.41</td>
<td>Source 1: *Strong – None, **Significant - PM, Pb, Fe</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>0.76</td>
<td>2.13</td>
<td></td>
</tr>
<tr>
<td>Cu-Ti-Fe-Mn-Pb-Cr-Hg-Se</td>
<td>2</td>
<td>0.56</td>
<td>2.29</td>
<td>Source 1: *Strong – None, **Significant - PM, Pb, Fe, Fe</td>
</tr>
<tr>
<td>Fe-Mn-Ti-Pb</td>
<td>3</td>
<td>0.90</td>
<td>2.85</td>
<td>Source 1: *Strong – None, **Significant - PM, Pb, Fe, Mn; Source 3: *Strong - Pb, Mn, **Significant - Ti, Fe</td>
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<tr>
<td></td>
<td>4</td>
<td>0.76</td>
<td>2.20</td>
<td>Source 1: *Strong - Cr, Ni, **Significant – None</td>
</tr>
<tr>
<td></td>
<td>5</td>
<td>0.89</td>
<td>1.67</td>
<td>Source 2: *Strong – None, **Significant – Cu; Source 3: *Strong – Pb, **Significant - PM, Cr, Cu, Ti, Fe, Mn; Source 4: *Strong – Ti, **Significant - PM, Cr, Pb, Fe</td>
</tr>
<tr>
<td>Fe-Mn-Ti-Pb-Cr-Cu-Ni</td>
<td>4</td>
<td>0.83</td>
<td>2.18</td>
<td>Source 1: *Strong - Pb, **Significant – Cu; Source 2: *Strong – None, **Significant - Cu; Source 3: *Strong – Pb, **Significant - PM, Cr, Cu, Ti, Fe, Mn</td>
</tr>
<tr>
<td></td>
<td>5</td>
<td>0.89</td>
<td>1.67</td>
<td>Source 3: *Strong – None, **Significant - PM, Cr, Cu, Ti, Fe, Mn</td>
</tr>
<tr>
<td>Fe-Mn-Ti-Pb-Cr-Cu</td>
<td>3</td>
<td>0.83</td>
<td>2.57</td>
<td>Source 1: *Strong - Pb, **Significant – Cu; Source 2: *Strong – None, **Significant - Cu; Source 3: *Strong – None, **Significant - PM, Cr, Pb, Ti, Fe; Source 3: *Strong – None, **Significant - PM, Cr, Cu, Ti, Fe, Mn</td>
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<tr>
<td></td>
<td>4</td>
<td>0.88</td>
<td>1.97</td>
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<tr>
<td></td>
<td>5</td>
<td>0.90</td>
<td>1.62</td>
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</tbody>
</table>

* Source Composition $\geq$ 1 sigma

**Source Composition $\geq$ 2 sigma
Table 3. $R^2$ values obtained by PMF of measured and the predicted concentrations

<table>
<thead>
<tr>
<th>Species</th>
<th>Category</th>
<th>$R^2$</th>
<th>3 sources</th>
<th>4 sources</th>
<th>5 sources</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cr</td>
<td>Strong</td>
<td>0.617</td>
<td>0.980</td>
<td>0.998</td>
<td></td>
</tr>
<tr>
<td>Ti</td>
<td>Strong</td>
<td>0.381</td>
<td>0.962</td>
<td>0.959</td>
<td></td>
</tr>
<tr>
<td>Fe</td>
<td>Strong</td>
<td>0.401</td>
<td>0.472</td>
<td>0.942</td>
<td></td>
</tr>
<tr>
<td>Pb</td>
<td>Strong</td>
<td>0.695</td>
<td>0.701</td>
<td>0.905</td>
<td></td>
</tr>
<tr>
<td>Mn</td>
<td>Weak</td>
<td>0.394</td>
<td>0.340</td>
<td>0.528</td>
<td></td>
</tr>
<tr>
<td>Cu</td>
<td>Strong</td>
<td>0.345</td>
<td>0.337</td>
<td>0.473</td>
<td></td>
</tr>
<tr>
<td>Ni</td>
<td>Weak</td>
<td>0.027</td>
<td>0.031</td>
<td>0.025</td>
<td></td>
</tr>
<tr>
<td>Co</td>
<td>Weak</td>
<td>0.006</td>
<td>0.013</td>
<td>0.018</td>
<td></td>
</tr>
<tr>
<td>Hg</td>
<td>Weak</td>
<td>0.002</td>
<td>0.005</td>
<td>0.003</td>
<td></td>
</tr>
</tbody>
</table>

Figure Legends

Fig. 1 Sampling site and prevailing wind directions
Fig. 2 Predicted and measured concentrations
Fig. 3 Edge plots for chosen solutions that satisfy the conditions of Min S/N and Min $R^2$
Fig. 4 Source profiles for selected solutions that are in accordance with the Unmix criteria
Fig. 5 F-peak analysis for three a), four b) and five c) source solutions. The red mark represents the value of F-peak Strength, at which the rotational ambiguity disappears.
Fig. 6 Profiles in the case of three sources solutions. Comparison of base run profile and F-peak run profile with the strength of -1.2 (disappearance of rotational ambiguity).
Fig. 7 Profiles in the case of three sources solutions. Comparison of base run profile and F-peak run profile with the strength of -0.8 (disappearance of rotational ambiguity).
Fig. 8 Profiles in the case of three sources solutions. Comparison of base run profile and F-peak run profile with the strength of -2.0 where it can be seen that F-peak Strength does not affect the existing rotational ambiguity.
Interactive comment on
“Applying receptor models Unmix and PMF on real data set of elements in PM for sources evaluation of the sea coastal side region (Southeast Adriatic Sea)” by
D. Đorđević et al.
Anonymous Referee #2
Received and published: 5 November 2013

In the study presented by Đorđević et al., a characterization of the possible sources of TSP (?) was carried out in a coastal area (Southeast Adriatic Sea). An attempt to identify the PM sources is made using two receptor modelling techniques (UNMIX and PMF). The results obtained by both techniques are compared with the results obtained using other models like Enrichment Factors (EF) and Principal Component Analysis (PCA). From my point of view the main problem of the article, is that it is not clear what the objective of the manuscript is. It seems that both models (PMF and Unmix) are used to find a solution similar to that found in the previous article written by the authors (Đorđević et al 2005). If that is the aim then the article does not add anything new to the scientific knowledge which already exists on this subject. If however the overall objective is to present a new attempt to identify the PM sources in the region, the article should be re-written in a different way. In this case, the results of the best solution of both models can then be compared with the result obtained using the other models.

In this manuscript were not only made an attempt to identify the PM sources using two receptor modeling techniques (UNMIX and PMF) and these results compared with the results obtained using other models like Enrichment Factors (EF) and Principal Component Analysis (PCA) but our main goal was to show how many mistakes could be made during the modeling even using the state-of-the-art models such as Unmix and PMF. We corrected the manuscript in this manner including the correction of Abstract, Main goals, Discussion and the Conclusion as well as the title of the Manuscript.

Another thing that concerns me is the use of only 11 elements for the determination of the possible sources affecting the study region. Some of the 11 sources are normally below the MDL (Co, Hg, Cd, Se), so the analysis is mainly done with 7 elements only. I am not sure that the results obtained are meaningful. This should be commented throughout article. I have serious doubts that this article is suitable for publication in this journal. I recommend a major revision of the article including a complete restructuring of the contents.

This data base was chosen because of measurements over longer period of time allow the greater accuracy than one obtained in a shorter time period. We also, modeled other data sets with large number of variables but we didn’t get
satisfactory solutions, even we didn’t get any solution due to a large number of excluded variables by the model because of a lot of outliers or missing values. So this data set has got the most representative solutions although with 11 elements.

Specific comments: The abstract should be rewritten. The location of the measurements, duration of the sampling campaign, sampling time, PM inlet used should be included. The remainder of the abstract should be completed once the aim of article is clarified. The same can be applied to the introduction. Both models are described in quite a lot of detail. That can be replace for some references.

The Abstract has rewritten and the location of the measurements, duration of the sampling campaign, sampling time added. PM inlet have included in the Material and Methods section in the part P4948L6. In the manuscript it is highlighted in yellow.

The Introduction has shortened.

Part of the introduction, like the Polissar criteria, should be in the experimental section.

It is moved to Material and Methods part along with another the paragraph which belong to this section

The procedure of Polissar et al. (1998) was used in this study to calculate uncertainties in the species concentrations. Briefly, for the data below detection limit (DL), the concentrations were replaced with the value DL/2 and the uncertainty was set as $\frac{5}{6}DL$. For the missing data, concentrations were replaced by the geometric mean and the respective uncertainty was set at four times of this mean concentration.

At the first set up all elements are labeled as Strong, since (the signal/noise ratio) $S/N > 2$ for all of them. Based on input data statistics, residuals show bi modal distribution in the case of Ni, Mn, and Hg, so their uncertainties are increased labeling them as Weak. Selenium is excluded from the model because of a very small contribution and the correlation factor, while for cadmium more than 50% of samples are below the detection limit.

Depending on the aim, the rest of the introduction should be changed to include more important references. A detailed main goal should appear at the end of this section. The materials and methods section should be expanded. Detailed information about the sampling point, the PM inlet used, sampling period, etc… are needed. A description of how the models are configured is also needed (Initial operations of the Unmix model,
data preparation for the PMF model, S/N ratio, Min R^2, IM, IS, G-space plots, ...). A table with the data (geometric mean, max, min, standard deviation, number of samples under the mdl) should be added as well. It is not usual to use the values of FPEAK of -0.8, -1 and -1.2 to eliminate the rotational ambiguity. An explanation for that should be added because it is not evident how you have used Fpeak and the G-space plots. What should be done is to use G-space plots of the base run to identify possible rotations in the solution.

It is corrected:
In addition, G-Space plots show considerable rotational ambiguity between the sources 1 and 3. ... However, such large values for Fpeak are unlikely because the quality of the fit decreases rapidly. The usually dataset rotations are generally much smaller and they are close to the basic solution. ...
G-Space plot shows that there is a rotational ambiguity between sources 1 - 3 2 - 3, 3 – 4. .... As in the case of a solution with three sources, a significant rotation of the dataset (F peak = -0.8) is less likely.

Corresponding G-space plots of F peak solution factors should be examined to see if any edges viewed in the base runs are more or less evident in the F peak runs. Additionally, profiles and contributions should be examined for species that deviate from the base run to ensure that they are reasonable.

It was observed that all the basic solutions cases of 3, 4 and 5 sources, the analysis of G-space plots there are couples of factors which indicate rotational ambiguity. It is improved – highlighted in the yellow in the new Manuscript. In the new part Results and Discussion in the part of PMF modeling for results for 3, 4 and 5 sources now is existing. These cases were analyzed using F-peak function and the solutions were analyzed. It is improved – highlighted in the yellow in the new Manuscript. In the new part Results and Discussion in the part of PMF modeling for results for 3, 4 and 5 sources now is existing.

The conclusion should also be rewritten once the objective of the article has been clarified. The conclusion is not a summary of the results and discussion sections. It should answer the objective proposed in the introduction. About the figures: Figure 1 is very small and the units are not present. Figure 5, 6, 7: There are some errors in the axis labels. The errors of the concentrations should be added. The caption in Figure 6 should state “four” instead of “three”.

The conclusion is corrected
The errors in the axis labels of Figures 5, 6, and 7 are corrected, now these Figures are 6, 7 and 8.