Carbon Monitoring Satellite (CarbonSat): assessment of scattering related atmospheric CO$_2$ and CH$_4$ retrieval errors and first results on implications for inferring city CO$_2$ emissions

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Abstract

Carbon Monitoring Satellite (CarbonSat) is one of two candidate missions for ESA’s Earth Explorer 8 (EE8) satellite – the selected one to be launched around the end of this decade. The objective of the CarbonSat mission is to improve our understanding of natural and anthropogenic sources and sinks of the two most important anthropogenic greenhouse gases (GHG) carbon dioxide (CO$_2$) and methane (CH$_4$). The unique feature of CarbonSat is its “GHG imaging capability”, which is achieved via a combination of high spatial resolution (2 km $\times$ 2 km) and good spatial coverage (wide swath and gap-free across- and along-track ground sampling). This capability enables global imaging of localized strong emission source such as cities, power plants, methane seeps, landfills and volcanos and better disentangling of natural and anthropogenic GHG sources and sinks. Source/sink information can be derived from the retrieved atmospheric column-averaged mole fractions of CO$_2$ and CH$_4$, i.e. $X_{CO_2}$ and $X_{CH_4}$, via inverse modeling. Using the most recent instrument and mission specification, an error analysis has been performed using the BESD/C retrieval algorithm. We focus on systematic errors due to aerosols and thin cirrus clouds, as this is the dominating error source especially with respect to $X_{CO_2}$ systematic errors. To compute the errors for each single CarbonSat observation in a one year time period, we have developed an error parameterization scheme based on six relevant input parameters: we consider solar zenith angle, surface albedo in two bands, aerosol and cirrus optical depth, and cirrus altitude variations but neglect, for example, aerosol type variations. Using this method we have generated and analyzed one year of simulated CarbonSat observations. Using this data set we estimate that scattering related systematic errors are mostly (approx. 85%) below 0.3 ppm for $X_{CO_2}$ (< 0.5 ppm: 99.5%) and below 2 ppb for $X_{CH_4}$ (< 4 ppb: 99.3%). We also show that the single measurement precision is typically around 1.2 ppm for $X_{CO_2}$ and 7 ppb for $X_{CH_4}$ (1-sigma). The number of quality filtered observations over cloud and ice free land surfaces is in the range 33–47 million per month depending on month. Recently it has been shown that terrestrial Vegetation
Chlorophyll Fluorescence (VCF) emission needs to be considered for accurate $XCO_2$ retrieval. We therefore retrieve VCF from clear Fraunhofer lines located at 755 nm and show that CarbonSat will provide valuable information on VCF. The VCF single measurement precision is approximately 0.3 mW m$^{-2}$ nm$^{-1}$ sr$^{-1}$ (1-sigma). As a first application of the one year data set we assess the capability of CarbonSat to quantify the $CO_2$ emissions of large cities using Berlin, the capital of Germany, as an example. We show that the precision of the inferred Berlin $CO_2$ emissions as obtained from single CarbonSat overpasses is in the range 5–10 Mt $CO_2$ yr$^{-1}$ (10–20 %). We found that systematic errors could be on the same order depending on which assumptions are used with respect to observational and biogenic $XCO_2$ modeling errors.

1 Introduction

Carbon dioxide ($CO_2$) and methane ($CH_4$) are the two most important anthropogenic greenhouse gases (GHG) contributing to global warming (Solomon et al., 2007). Their concentration in the atmosphere significantly increased during the previous decades and still continues to increase (e.g. Francey et al., 2013; Olivier et al., 2012; Schneising et al., 2011; Dlugokencky et al., 2009, and references given therein). Despite their importance, our knowledge on their sources and sinks has significant gaps (e.g. Canadell et al., 2010; Rigby et al., 2008; Stephens et al., 2007).

Global satellite observations of $CO_2$ and $CH_4$ can help to close important knowledge gaps on $CO_2$ and $CH_4$ regional-scale sources and sinks (e.g. Guerlet et al., 2013a; Basu et al., 2013; Maksyutov et al., 2012; Bergamaschi et al., 2009; Rayner and O’Brien, 2001). Knowledge gaps also exist on smaller scales, e.g. for $CO_2$ emitting power plants (e.g. Krings et al., 2011; Velazco et al., 2011; Bovensmann et al., 2010, and references given therein), $CO_2$ emissions from cities or large urban agglomerations (e.g. Schneising et al., 2013, 2008; Keppel-Aleks et al., 2012; Kort et al., 2012, and references given therein), and various local industrial and geological sources of methane (e.g. Krings et al., 2013; Leifer et al., 2013; Bovensmann et al., 2010, and references
Satellite observations of greenhouse gases are also required to contribute to the verification of international climate agreements (e.g. NRC, 2010, and references given therein). These applications require high precision and accuracy, good spatio-temporal coverage and sensitivity to near-surface concentration variations (e.g. Buchwitz et al., 2011, 2013; Chevallier et al., 2007; Meirink et al., 2006). The Carbon Monitoring Satellite (CarbonSat) (Bovensmann et al., 2010) mission and instrument concept is addressing these needs. The objective of the CarbonSat mission is to determine and separate natural and anthropogenic CO₂ and CH₄ sources and sinks. CarbonSat will contribute to the quantification of natural fluxes of CO₂ and CH₄ (e.g. biospheric CO₂, wetland CH₄) but also to a much better estimation of anthropogenic emissions than possible with any of the other existing or planned satellite missions. This will be achieved via a unique feature of CarbonSat, which is its “GHG imaging capability”. GHG imaging is achieved via a combination of high spatial resolution (2 km × 2 km) and good spatial coverage achieved by a relatively wide swath and no gaps between adjacent (across-track and along-track) ground pixel. The width of the across-track swath has not yet been finally decided. Here we present results for two swath widths: 240 km (CarbonSat’s breakthrough requirement) and 500 km (goal requirement). This capability enables global imaging of localized strong emission sources such as cities, power plants, methane seeps, landfills and volcanos and a better disentangling of anthropogenic and GHG natural sources and sinks.

The main data products of CarbonSat are atmospheric column-averaged dry-air mole fractions of CO₂ and CH₄, denoted XCO₂ and XCH₄. These data products are also generated or are planned to be generated, from other past, present and future greenhouse gas missions such as SCIAMACHY (Burrows et al., 1995; Bovensmann et al., 1999; Buchwitz et al., 2005), GOSAT (Kuze et al., 2009; Yoshida et al., 2011) and the upcoming OCO-2 mission (XCO₂ only) (Crisp et al., 2004; Boesch et al., 2011). Compared to these missions, CarbonSat aims at better disentangling natural and anthropogenic sources and sinks of CO₂ and CH₄ due to its GHG imaging capability.
CarbonSat has been selected by the European Space Agency (ESA) to be one of two candidate missions for ESA’s Earth Explorer 8 (EE8) satellite. The other candidate mission is the FLuorscencence EXplorer (FLEX) (Rascher, 2007; ESA, 2008). The selected mission will be launched around the end of this decade (i.e. around 2020).

Near-surface sensitivity is achieved by measuring spectra of solar radiation reflected at the Earth’s surface and backscattered into the atmosphere to space using spectral regions sensitive to CO$_2$ and CH$_4$ absorption. These spectra are also influenced by atmospheric scattering by air molecules (Rayleigh scattering), aerosols and clouds. Scattering influences the light path and needs to be appropriately considered when retrieving CO$_2$ and CH$_4$ information from the measured spectra. The focus of this manuscript is to address this aspect. It is well known that unaccounted variability of atmospheric scattering by aerosols and clouds, especially undetected thin cirrus clouds, are a major error source for satellite CO$_2$ and CH$_4$ retrieval in the solar spectral region (e.g. Guerlet et al., 2013b; Heymann et al., 2012a,b; Oshchepkov et al., 2012; O’Dell et al., 2012; Reuter et al., 2011; Butz et al., 2011). It is therefore important to assess to what extent a particular type of measurement (here the proposed measurements of CarbonSat) may suffer from this error source. To evaluate this, we have conducted an assessment based on simulated CarbonSat observations. We focus on errors due to aerosols and cirrus clouds assuming that scenes contaminated by thick clouds have already been identified (e.g. by pre-processing O$_2$ A-band spectra) and removed (similar to that currently done for SCIAMACHY (e.g. Heymann et al., 2012a,b; Reuter et al., 2011) and GOSAT (e.g. Cogan et al., 2012; O’Dell et al., 2012; Crisp et al., 2012; Butz et al., 2011).

Initial error analysis results for CarbonSat concerning aerosols and cirrus clouds have already been presented in Bovensmann et al. (2010), focusing on one application, namely to infer CO$_2$ emissions of coal-fired power plants from single overpass CarbonSat XCO$_2$ observations. Here we extend this analysis by computing and analyzing errors for one year of global simulated CarbonSat observations. For this purpose we have developed an error parameterization method which permits fast computation
of random and systematic $XCO_2$ and $XCH_4$ errors as a function of several critical input parameters such as aerosol Optical Depth (OD), cirrus OD and cirrus altitude. The error analysis is based on the most recent instrument and mission specification and uses the latest version of the BESD/C “full physics” algorithm (Bovensmann et al., 2010) for retrieving geophysical parameters from CarbonSat radiances.

This manuscript is structured as follows: in Sect. 2 the CarbonSat instrument concept is described and in Sect. 3 the retrieval algorithm is briefly presented focusing on recent improvements. In Sect. 4 the error analysis and error parameterization approach is described. The error parameterization method permits fast computation of random and systematic $XCO_2$ and $XCH_4$ errors and averaging kernels and has been used to generate one year of simulated CarbonSat observations. How this data set has been generated is described in Sect. 5. As a first application the data set is used to assess to what extent CarbonSat can quantify the anthropogenic $CO_2$ emissions of cities using Berlin as an example (Sect. 6). This assessment is based on single Berlin overpass data by analyzing CarbonSat derived “$XCO_2$ images”. In Sect. 7, an analysis of the global data is presented. This comprises spatio-temporally averages and assessments for various regions as relevant for the application to quantify natural $CO_2$ and $CH_4$ fluxes on regional scales. Limitations of our approach and an outlook to future work are shortly discussed in Sect. 8. A summary and conclusions are given in Sect. 9.

2 CarbonSat mission and instrument concept

CarbonSat aims to deliver $XCO_2$ (in ppm) and $XCH_4$ (in ppb) at a high spatial resolution of $2\text{ km} \times 2\text{ km}$ and good spatial coverage via continuous imaging across a 240 km swath width (CarbonSat’s “breakthrough requirement”; the more demanding “goal requirement” is 500 km). The orbit will be sun-synchronous. For this study we assume that the orbit will be similar to NASA’s Terra satellite (www.nasa.gov/terra/) but with an equator crossing time of 11.30 a.m. (Local Time Descending Node – LTDN). CarbonSat’s main mode will be the nadir (downlooking) mode. CarbonSat will also obtain
solar spectra and perform observation in sun-glint mode, especially to improve the quality of the observations over water and snow and ice covered land surfaces, which are poor reflectors in the Short-Wave-Infra-Red (SWIR) spectral region outside of sun-glint conditions. As the sun-glint observation strategy has not yet been finally decided and because the BESD/C retrieval algorithm has not yet been optimized for sun-glint conditions, the CarbonSat sun-glint observations are not considered in this study. Here we focus on nadir mode observations over snow and ice free land surfaces.

The CarbonSat imaging spectrometer will cover three spectral bands (Table 1). The Near-Infra-Red (NIR) band covers the O$_2$ A-band spectral region (747–773 nm) at 0.1 nm spectral resolution (approx. 1.7 cm$^{-1}$). This band permits one to obtain information on aerosols, clouds, surface pressure and Vegetation Chlorophyll Fluorescence (VCF). The first SWIR band (SWIR-1) covers the 1590–1675 nm spectral region at 0.3 nm spectral resolution (approx. 1.2 cm$^{-1}$). This spectral region contains important absorption bands of CO$_2$ and CH$_4$ but is otherwise quite transparent and therefore permits one to deliver information on CO$_2$ and CH$_4$ columns with high near-surface sensitivity. The “strong CO$_2$ band” SWIR-2 covers the 1925–2095 nm region with spectral resolution of 0.55 nm (approx. 1.4 cm$^{-1}$). It contains additional information on CO$_2$ but also on water vapor and cirrus clouds, the latter from the saturated water band located at 1940 nm. The basic idea is to retrieve CO$_2$ and CH$_4$ columns from the transparent SWIR-1 band but to use in addition the partly non-transparent NIR and SWIR-2 bands located at smaller (NIR) and longer (SWIR-2) wavelengths to obtain information on atmospheric scatterers at 0.76 µm (NIR) and 2 µm (SWIR-2) to constrain the CO$_2$ and CH$_4$ retrieval at 1.6 µm (SWIR-1). In practice, all the needed information will essentially be retrieved simultaneously by applying an appropriate retrieval algorithm to all three bands (see Sect. 3).

For this study we use the latest specification of the CarbonSat imaging spectrometer currently available. Some further optimization of instrument requirements might be possible during mission development. The CarbonSat instrument specification as used for this study is similar but not exactly identical as the one described in Bovensmann et al.
(2010). The most relevant differences are: (i) the spectral resolution is somewhat lower compared to that assumed in Bovensmann et al. (2010), esp. in the NIR and SWIR-2 bands, driven by reduction in instrument complexity; (ii) the spectral coverage has been enlarged for the NIR band to include more clear Fraunhofer lines as recommended by Frankenberger et al. (2012), and also for the SWIR-2 band to cover a saturated water band at 1940 nm for improved cirrus detection similar as also done for SCIAMACHY (Heymann et al., 2012b) and GOSAT (Guerlet et al., 2013b); and (iii) the signal-to-noise ratio (SNR) has been enhanced to compensate for the reduced spectral resolution. For this study we use the required threshold (i.e. minimum) SNR performance of CarbonSat (see Table 1) and not, as in Bovensmann et al. (2010), a SNR model.

The instrument parameters (Table 1) are used by a CarbonSat instrument model, which converts high spectral resolution spectra as computed with the radiative transfer model SCIATRAN (Rozanov et al., 2005; Rozanov and Kokhanovsky, 2006) into simulated CarbonSat observations taking into account the relevant instrument characteristics as listed in Table 1. As an example, Fig. 1 shows a simulated CarbonSat nadir radiancespectrum, the solar irradiance, the corresponding sun-normalized radiances and signal-to-noise ratio (SNR) spectra for a scene with vegetation albedo (NIR: 0.2, SWIR-1: 0.1, SWIR-2: 0.05) and a solar zenith angle (SZA) of 50°.

3 BESD/C retrieval algorithm description

For this study the BESD/C retrieval algorithm (Bovensmann et al., 2010) has been used. The acronym BESD stands for “Bremen optimal ESTimation DOAS”. BESD/C retrieves $X_{CO_2}$ and $X_{CH_4}$ and additional parameters (e.g. for aerosols and cirrus clouds) from a simultaneous analysis of the three CarbonSat bands NIR, SWIR-1 and SWIR-2. BESD/C is described in detail in Bovensmann et al. (2010). Therefore we here give only a short overview focusing on recent improvements.
3.1 General description

BESD/C is similar but not exactly identical to the BESD algorithm used for SCIAMACHY XCO₂ retrieval (Reuter et al., 2010, 2011). BESD/C and BESD are “full physics” (FP) retrieval algorithms. As shown in Bovensmann et al. (2010), BESD/C also permits one to perform “proxy” (PR) retrievals. BESD/C retrieves CO₂ and CH₄ vertical columns (in molecules per cm²), which are converted into dry air column-averaged mole fractions or mixing ratios, i.e. XCO₂ (in ppm) and XCH₄ (in ppb), by dividing the retrieved GHG columns by the dry air column (in number of air molecules, except water vapor, per cm²). For a FP algorithm, the (dry) air column is obtained from retrieved surface pressure, e.g. obtained from the O₂ A-band spectral region, or from surface pressure obtained from meteorological analysis fields (corrected for water vapor using retrieved or meteorologically analyzed water vapor columns). Essentially both sources of information are used to compute the dry air column as the retrieval will use meteorological information as first guess and a priori information. For a PR algorithm, the air column is obtained from a reference gas, which is CO₂ in case of PR XCH₄ (e.g. Frankenberg et al., 2005; Schneising et al., 2011; Krings et al., 2013) or CH₄ in case of PR XCO₂ (see Bovensmann et al., 2010; Krings et al., 2011). The reference gas should be less variable than the target gas (or can be modelled with sufficient accuracy). Typically PR retrievals require a correction procedure for variations of the reference gas using a model (see also Schepers et al., 2012), for a discussion of FP versus PR retrievals).

If a PR method can be used depends on the application, whereas the FP method is always applicable as it does not require any assumptions on the reference gas. In this study we focus on FP retrievals and discuss PR retrievals only briefly. Despite the mentioned limitations, PR retrievals have the advantage that systematic errors caused by, e.g. clouds and aerosols, cancel to a large extent when the GHG column ratio is computed (we illustrate this using one example). For some applications (e.g. Bovensmann et al., 2010; Krings et al., 2011, 2013) this is advantageous as it enhances the accuracy.
BESD/C is based on “Optimal Estimation” (OE) (Rodgers, 2000) and uses a priori information to constrain the retrieval. BESD/C has already been applied to simulated CarbonSat observations as shown in Bovensmann et al. (2010). In that publication BESD/C has been used via a fast non-iterative look-up-table approach. For the results presented here, BESD/C has been improved to enhance the accuracy. This has been achieved by fully coupling BESD/C to the radiative transfer model (RTM) SCIATRAN (Rozanov et al., 2005; Rozanov and Kokhanovsky, 2006) as this permits an iterative retrieval by calling the RTM with updated parameters after each iteration step. During the iteration, the BESD cost function (see Eq. 7, Bovensmann et al., 2010) is minimized. The method used to minimize the cost function is based on Levenberg–Marquardt and is identical for BESD and BESD/C and described in Reuter et al. (2011). This (or an equivalent) iterative procedure improves the accuracy of the retrieved \(^{12} \text{CO}_2\) and \(^{18} \text{CH}_4\) in the presence of variable (and unknown) amounts of aerosols and cirrus clouds and is essentially the standard method also used by other algorithms (e.g. O’Dell et al., 2012; Butz et al., 2011; Reuter et al., 2010, 2011).

Compared to the BESD/C version described in Bovensmann et al. (2010), the BESD/C state vector, which contains all elements to be retrieved via the OE retrieval procedure, has been extended. All state vector elements are listed in Table 2. For each state vector element the derivative of the radiance with respect to the state vector element is needed to characterize the change of the radiance due to a change of that state vector element. These derivatives define the Jacobian matrix, which contains the derivative spectra in each of its columns (for the BESD/C Jacobian matrix, see matrix \(K\) described in Bovensmann et al., 2010). For BESD/C the derivative spectra are computed (quasi-analytically) by SCIATRAN. A typical BESD/C Jacobian matrix as used for this study is shown in Fig. 2. Note that each spectrum has been scaled such that the spectra do not overlap in this figure and that it is not possible to see all relevant details in Fig. 2. For example, for AOD retrieval, two Jacobians are shown, namely “AODNIR” and “AODSW2”. AODNIR covers the NIR and SWIR-1 bands (and is zero in the SWIR-2 band), whereas AODSW2 covers the SWIR-2 and SWIR-1 bands (an is
zero in the NIR band). The spectral variations of these two Jacobians in the SWIR-1 band are difficult to see in this figure as the amplitude of these Jacobians is much larger in the two “strongly absorbing” NIR and SWIR-2 bands (in the NIR due to strong O$_2$ absorption; in the SWIR-2 due to strong CO$_2$ and H$_2$O absorption). This indicates that AOD information can primarily be derived (only) from the NIR and SWIR-2 bands. The coupling with the SWIR-1 band ensures (at least to some extent) that AOD information obtained from the NIR and SWIR-2 bands is “made available” in the SWIR-1 band (the AOD information content of SWIR-1 band is negligible, especially if only “differential” information is used – BESD/C DOAS polynomial, as the AOD Jacobian correlates with other Jacobians, e.g. with the CO$_2$ Jacobian).

BESD/C as described here has been applied to a number of scenarios to quantify random and systematic $X$CO$_2$ and $X$CH$_4$ errors. Results of this exercise are presented and discussed in Sect. 4 focusing on aerosol and cirrus related errors. Before the error analysis results are presented we discuss one additional aspect, namely how to consider potential issues related to Vegetation Chlorophyll Fluorescence (VCF) emission, which also needs to be considered, as it influences the radiance in the NIR band of CarbonSat.

### 3.2 Consideration of terrestrial Vegetation Chlorophyll Fluorescence (VCF)

Recently it has been shown that terrestrial Vegetation Chlorophyll Fluorescence (VCF) emission needs to be considered for accurate $X$CO$_2$ retrieval (Frankenberg et al., 2012). BESD/C has therefore been improved to consider this. As can be seen from Table 2, VCF is a state vector element for the version of BESD/C used in this study. In order to provide the radiative transfer model with a reasonable VCF first guess value, a simple but very fast “Dedicated VCF” (DVCF) retrieval scheme has been implemented. It is not based on full SCIATRAN computations but uses only a few constant pre-computed spectra (plus a low order polynomial) to model the sun-normalized radiance via scaling these spectra using a simple but fast OE retrieval scheme. The method
we use is similar to the methods described in Joiner et al. (2011) and Frankenberg et al. (2011).

The following spectra are used for DVCF pre-processing:

- A high spectral resolution solar irradiance spectrum. We use the “OCO Toon spectrum” described in O’Dell et al. (2012). This spectrum is the most important spectrum as required for VCF retrieval based on clear solar Fraunhofer lines.

- A low order polynomial to consider spectrally broad-band radiances due to, e.g. aerosols, clouds and surface albedo or residual calibration issues.

- A surface emission VCF spectrum (Rascher et al., 2009). Note however that only a small spectral region is used by the DVCF algorithm (749–759 nm) and that the VCF spectrum is essentially constant (or varies only linearly) in this narrow spectral range and that therefore the retrieval results are essentially independent of the VCF spectrum used.

- A water vapor absorption spectrum computed off-line with SCIATRAN using HITRAN 2008 spectroscopic line parameters (Rothman et al., 2009). Note that the underlying water absorption in the DVCF retrieval window is very weak and that including water absorption only slightly improves the quality of the spectral fit but hardly changes the retrieved VCF values.

These spectra are used at present by a simple but very fast non-iterative OE scheme to retrieve VCF essentially as a scaling factor of the VCF Jacobian. Atmospheric absorption and scattering are neglected by the currently implemented DVCF retrieval method.

A DVCF example fit is shown in Fig. 3. The CarbonSat nadir radiance ($L$, top panel a, black line) has been computed with the latest version of the SCIATRAN radiative transfer model, which takes all relevant processes including (multiple) scattering and surface emission by VCF into account. As can be concluded from the similarity between the (scaled) solar irradiance ($F$, top panel, red line) and the (scaled) nadir radiance, the
spectral region used for DVCF retrieval is essentially free of atmospheric absorption features (even water vapor absorption is very small in this region). The difference between the two (scaled) spectra is primarily due to terrestrial vegetation fluorescence emission at the surface, which causes a (tiny) filling-in of the solar Fraunhofer lines (most clearly seen for the two strongest lines located at 749.7 and 751.3 nm) and a slope change over the spectral region (note that $L$ and $F$ have seen scaled to 1.0 at the lowest wavelength shown in Fig. 3). Panel b of Fig. 3 shows the corresponding sun-normalized radiance (black line) and its measurement error (1-sigma noise level, grey vertical bars) and the fitted simple DVCF model (red line). As can be seen, the fit is good but not perfect. Especially the amplitude of the peaks do not match perfectly. This is due to the currently used fast and simple (e.g. non-iterative) DVCF model, which is not based on the full VCF Jacobian computed by SCIATRAN (note that SCIATRAN is not used for the DVCF retrieval). As a result, the retrieved VCF is somewhat underestimated for VCF values larger than the used a priori value (of 0.8 mW m$^{-2}$ nm$^{-1}$ sr$^{-1}$) and overestimated for VCF values less than the used a priori value (at the a priori value the error is zero). The deviation is to a good approximation linear and scenario independent and therefore a simple linear correction is used. This can be improved using a more advanced algorithm, e.g. by using SCIATRAN for DVCF retrieval, but this would require more computational resources. For the purpose of this study, the currently implemented fast DVCF retrieval method is used. The retrieved VCF is used as a first guess and a priori value for the full 3-band BESD/C retrieval.

The DVCF retrieval method has been used to retrieve VCF from a large number of scenarios taking into account different SZA, aerosol amounts and cirrus parameters. Figure 4 shows the results for 180 scenarios (the parameters which have been varied are listed in Fig. 4, see blue text in panel a). As can be seen, a very good correlation between the retrieved and the true VCF exists ($r = 0.99$). As can also be seen, the standard deviation of the difference is 0.19 mW m$^{-2}$ nm$^{-1}$ sr$^{-1}$ (less than approx. 20% except for very low VCF emission (see panel b). Also listed is the single observation
retrieval precision, which is $0.233 \pm 0.031 \text{ mW m}^{-2} \text{ nm}^{-1} \text{ sr}^{-1}$ (mean and standard deviation as obtained from all 180 scenarios).

4 XCO$_2$ and XCH$_4$ error analysis and parameterization

In this section we present and discuss our error analysis and error parameterization approach for scattering related errors. We focus on systematic XCO$_2$ and XCH$_4$ retrieval errors but also discuss random errors due to instrument noise. There are several other error sources, such as residual calibration errors, which contribute to systematic (and random or quasi random) errors. These error sources have been considered when formulating the CarbonSat mission and instrument requirements but are not discussed here. The main goal of the error parameterization described here is to compute random and scattering related systematic errors for each single CarbonSat observation for a one year time period. Due to the large number of CarbonSat observations, this requires an appropriate, i.e. very fast but sufficiently accurate, scheme to compute these errors. How this has been achieved is described in the following.

4.1 General considerations

Systematic retrieval errors especially for scattering parameters depend significantly on parameters such as the amount of aerosol (characterized by, e.g. Aerosol Optical Depth, AOD, at the relevant wavelengths), Cirrus Optical Depth, COD, and altitude – Cirrus Top Height, CTH) and surface spectral reflectance (characterized by, e.g. Lambertian surface albedo). An initial error analysis of CarbonSat XCO$_2$ and XCH$_4$ errors due to aerosols and clouds has already been presented in Bovensmann et al. (2010), focusing on CarbonSat power plant overpasses. Here we present an extension of that analysis to assess the quality of the global data. We aim at estimating random and systematic XCO$_2$ and XCH$_4$ errors for one year of CarbonSat global observations. Ideally, this should be done by applying the retrieval algorithm to all individual observations.
However, due to the large amounts of data, CarbonSat will generate, and because the retrieval program BESD/C as currently implemented is quite slow, this is not yet possible. Reducing the processing time is an important task for the future. For the purpose of this study we have developed an error parameterization scheme, which is described in this section. This scheme permits one to compute the $X_{CO_2}$ and $X_{CH_4}$ errors as a function of several scattering related critical input parameters. A similar approach has also been used by Hungershofer et al. (2010) to assess the impact of satellite $X_{CO_2}$ errors for CO$_2$ surface flux inversions.

The goal of this study is to realistically estimate the expected CarbonSat performance in terms of $X_{CO_2}$ and $X_{CH_4}$ random and systematic errors. Random errors are primarily determined by the instrument signal-to-noise performance. It is believed that random errors can be reliably quantified already at this early stage (note that the instrument design is still being optimized) assuming, for example, that detectors will not dramatically improve in the near future. Systematic errors however also depend critically on the retrieval algorithm and its parameter settings. It is expected that the BESD/C algorithm will be significantly further improved in the coming years, e.g. by better exploiting the strong water band in the 1940 nm spectral region for cirrus detection (e.g. Heymann et al., 2012b), or by further improving the aerosol retrieval method by also retrieving an aerosol size parameter (e.g. Butz et al., 2011). One way to consider future improvements could be to reduce systematic errors by a certain factor. Such a factor can however not be reliably estimated. For this study we use BESD/C as is. However, we solve a somewhat simplified retrieval problem, e.g. by focusing only on a few parameters, which are known to be critical ones. Our approach is more advanced than the relatively simple approach for other dedicated GHG satellite missions as used by Hungershofer et al. (2010), as we consider more parameters, but it is still quite simple, as we neglect, for example, microphysical parameter variations for aerosols (this aspect is further discussed in Sect. 8).

Another question is which a priori information to use for scattering related and other parameters. Very likely the future operational CarbonSat algorithm will use a priori
information for several parameters, as this will reduce systematic GHG retrieval errors. This is also the approach used by the operational GOSAT algorithm (Yoshida et al., 2011, 2013). Here we utilize the following simple approach: We use constant a priori values for COD, CTH and AOD but to compensate for this we assume good knowledge of the surface albedo by using the true albedo in each band as first guess value. Note that BESD/C retrieves surface albedo (see ALB state vector elements listed in Table 2) and first guess values are obtained using a pre-processing scheme based on transparent spectral regions as located in each of the three bands. Nevertheless, systematic $X_{CO_2}$ and $X_{CH_4}$ retrieval errors are reduced if surface albedo is well known, especially for low albedo scenes, where aerosols and cirrus may significantly influence the backscattered radiance.

4.2 Error analysis based on individual BESD/C retrieval

For the error analysis (and the error parameterization, see following section) a number of scenarios have been defined using different combinations of COD, CTH, AOD, surface albedo and SZA. They are shown in Fig. 5. For each scenario high spectral resolution radiance spectra have been computed with SCIATRAN and converted to simulated CarbonSat spectral observations using the CarbonSat instrument model mentioned in Sect. 2. BESD/C has been applied to each simulated observation to retrieve $X_{CO_2}$ and $X_{CH_4}$ and to determine their errors. Random errors depend primarily on the signal-to-noise performance of the instrument and the OE retrieval method permits one to map this error from radiance space to state vector (i.e. retrieval parameter) space. Systematic $X_{CO_2}$ and $X_{CH_4}$ errors are computed as “retrieved minus true”, where the true values are the known values from the model atmosphere. After BESD/C retrieval, a quality flag is set, which depends on the retrieved scattering parameters. Here we only flag those retrievals as “good” for which the sum of the retrieved aerosol optical depth (at NIR wavelength) and cirrus optical depth is less than 0.3 (i.e. $AOD(NIR) + COD < 0.3$). This filtering criterium is similar as used, for example, for GOSAT $X_{CO_2}$ retrieval (Guerlet et al., 2013b; O’Dell et al., 2012). Applying such
a criterium requires that COD and AOD (or strictly speaking their sum) can be retrieved with sufficient accuracy.

As shown in Fig. 5a, COD can be retrieved very well. This is shown by the typically very good agreement between retrieved COD (black dots) and true COD (green line). The retrieved AOD correlates with the true values but the absolute retrieved values are not perfect; typically the full variability is not captured by the retrieval. This shows that COD can be retrieved with higher accuracy than AOD. The reason for this is that the AOD changes are primarily due to changes of the aerosol amount in the boundary layer, which has less impact on the radiance than COD changes in the upper troposphere. As can also be seen in Fig. 5b, CTH can also be retrieved quite well at least if COD is not too low. Note that for this error analysis, as already explained, we only study very thin clouds as it is assumed that all ground pixels with significant cloud contamination have already been identified and removed (see also Sect. 5).

Figure 6 shows the corresponding $X_{CO_2}$ and $X_{CH_4}$ random and systematic errors for the same scenarios as shown in Fig. 5. The results for all scenarios are shown as light red line and the quality filtered, i.e. “good”, retrievals are shown as red diamonds. Figure 7 is a zoom into Fig. 6 to show more details for all those scenarios, which correspond to a SZA of 50°.

As can be seen, the $X_{CO_2}$ random error is typically around 1 ppm except for low surface albedo (see WAT50 scenarios in Figs. 6 and 7 corresponding to a water albedo of 0.03 in all spectral bands and a SZA of 50°), where the precision is close to 2 ppm, and for some high SZA scenarios (VEG75, i.e. vegetation albedo and SZA 75°, as shown in Fig. 6), where the $X_{CO_2}$ precision exceeds 2 ppm for high COD. The $X_{CH_4}$ random error has a similar scenario dependence. It is typically between 5–10 ppb except for the WAT50 and VEG75 scenarios, where it is typically between 15–20 ppb or even larger for VEG75, if COD is high.

The systematic errors are more complex as they depend more strongly on the scenario, especially for low albedo (WAT50) and high SZA (75°) scenarios (e.g. SAS75, corresponding to sand/soil albedo, and VEG75). For the “less extreme” albedo and
SZA scenarios (i.e. DES00, where DES is desert albedo, SAS25, VEG20, SAS50, and VEG50) the systematic $XCO_2$ error is a few tenths of a ppm and the systematic $XCH_4$ error is a few ppb. For the “more extreme” scenarios WAT50, SAS75 and VEG75, the systematic error can be much larger, up to about 3 ppm for $XCO_2$ and nearly 20 ppb for $XCH_4$. Also the dependence on cirrus OD, cirrus altitude and AOD is much larger for these scenarios. Because low albedos such as water (or snow and ice in the SWIR bands) result in large errors, we focus in this manuscript on (snow and ice free) land surfaces. It is believed that this will be much better when exploiting the CarbonSat sun-glint observations but a discussion of this is out of the scope of this study. The large variation of the errors at high SZA is also a potential problem. Therefore we limit the further analysis as presented in Sect. 5 and following sections to a maximum SZA of 70°.

4.3 Error parameterization

In order to generate one year of simulated CarbonSat observations we have developed an error parameterization scheme to parameterize the $XCO_2$ and $XCH_4$ random and systematic errors and their averaging kernels (which describe the change of the retrieved quantity, e.g. $XCO_2$, due to a change of the true quantity caused by a perturbation at a given altitude (e.g. the perturbation of the CO$_2$ mixing ratio). For this purpose we defined a number of regression functions and applied a linear regression scheme to the quality filtered, i.e. “good”, retrievals, as shown in Figs. 6 and 7 (red diamonds) as already discussed in the previous section. The used error parameterization formulas and resulting regression coefficients are reported in Appendix A.

The error parameterization results for the $XCO_2$ and $XCH_4$ errors are shown in Figs. 6 and 7 (black dots). The error parameterization computes the desired output parameters based on 6 input parameters. The input parameters are the parameters which define the scenarios shown in Fig. 5, i.e. SZA, albedo in the NIR and SWIR-1 bands, COD, CTH and AOD (at 550 nm). These parameters are assumed to be the 6 most critical ones. Note that the errors also depend on other parameter not explicitly
considered here. One example is SWIR-2 albedo. SWIR-2 albedo variations have been considered for the retrieval simulations but not for the error parameterization. We assume here that the SWIR-1 and SWIR-2 albedos are sufficiently well correlated.

As can be seen from Figs. 6 and 7, the errors computed with the error parameterization method (black dots) capture the variability of the “real errors” (red diamonds) reasonably well. Less good is the agreement for very low surface albedos (WAT50 scenarios) and for scenarios where the SZA is large, i.e. the SAS75 and VEG75 scenarios. Figure 7, which is a zoom into Fig. 6, shows more details for the scenarios corresponding to a SZA of 50°. As can be seen most clearly in Fig. 6, the error parameterization tends to overestimate the random and systematic errors for typical land surfaces and tends to underestimate the errors for retrievals over water (i.e. for very low albedo scenes). As the focus of this manuscript is on observations over land, the error parameterization results are quite conservative as they tend to overestimate the random and systematic errors as computed using full BESD/C retrievals. In this context it shall be mentioned that also other error parameterization schemes have been investigated based on tabulating the errors obtained by BESD/C retrievals combined with a multi-dimensional interpolation scheme. The agreement of the results obtained with this scheme was however worse than for the scheme used here, especially for systematic errors, which exhibit complex dependencies on the various input parameters, and are therefore quite difficult to model. The main reason why the table-based interpolation scheme did not work well is because of problems related to the quality flagging, which essentially does not permit the generation of a table, which is based on a regular grid of input parameters.

The regression scheme also permits one to parameterize the $X_{CO_2}$ and $X_{CH_4}$ averaging kernels. The corresponding results are shown in Fig. 8. Shown are “real” (red diamonds) and parameterized (black dots) averaging kernel values at the surface (panels a and b) and at $p/p_o = 0.5$ (panels c and d), where $p$ is the pressure level and $p_o$ denotes surface pressure. As can be seen, the averaging kernels are nearly ideal, i.e. 1.0 at the surface for $X_{CO_2}$ and $X_{CH_4}$.
In the following section it is described how the error parameterization has been used to generate one year of simulated global CarbonSat observations.

5 Generation of simulated global CarbonSat observations

To generate a data set useful for global regional-scale inversion studies and other applications (see, e.g. Sect. 6) and to obtain statistical results for various regions (see Sect. 7), a one year global data set of simulated CarbonSat observations has been generated. This data set (“Level 2 error” – L2e – files) contains for each single CarbonSat observation the time and location of the measurement (for the reference year 2008), the relevant angles (e.g. solar and viewing zenith and azimuth angles) and various geophysical parameters such as AOD, COD and CTH. The files do not contain the $X_{CO_2}$ and $X_{CH_4}$ errors and the averaging kernels. Instead, these files contain all the needed information (for each ground pixel) to compute the corresponding values using the error parameterization method discussed in the previous section. The files also do not contain absolute $X_{CO_2}$ and the $X_{CH_4}$ values. These values are expected to come from a (global or regional) model as used for the analysis of the CarbonSat data. The model data are expected to be “perturbed”, using the provided error characteristics (and averaging kernels) to generate appropriate simulated observations consistent with the model used.

The L2e files have been generated assuming an orbit similar as NASA’s Terra satellite (sun-synchronous, descending, equator crossing 10.30 a.m., see www.nasa.gov/terra/) except for the equator crossing time, which is assumed to be 11.30 a.m. for CarbonSat, i.e. one hour later than Terra. One year of Terra data (year 2008) has been used to generate the L2e files. Geolocation information available in the Terra files has been used for the L2e files. The time information and related quantities, e.g. SZA, has been adjusted to consider the different equator overpass times.

The MODIS Terra MOD35 data product with a spatial resolution of about 1km x 1km has been used to identify and filter out cloud contaminated CarbonSat ground pixels.
Only those (2 km × 2 km) CarbonSat ground pixels are classified as cloud free for which all four corresponding MODIS pixels were cloud free. The L2e files only contain the cloud free CarbonSat data as determined using the described procedure. Nevertheless, it can be expected that some cloud contamination remains, in particular thin (sub-visual) cirrus clouds. In order to obtain the cirrus parameters COD and CTH, a “climatology” has been generated using CALIPSO (Winkler et al., 2009). The used CALIPSO data product (CAL LID L2 05kmCLay-Prov-V3-01) provides information on COD with a horizontal resolution of 5 km by 70 m. This data product has been processed as described in Heymann et al. (2012a). The CALIPSO data set provides binary information about cloud coverage. Consequently, the relative frequency of cloud occurrence has been computed for every grid box and is used as Cloud Fractional Coverage (CFC) data set. Using CALIPSO derived COD and CFC, “effective COD”, eCOD (= COD × CFC), has been computed. The (sparse) CALIPSO eCOD and CTH data sets have been spatio-temporally smoothed with a Hann-window with an effective width of 8° × 8° and 3 months, i.e. the cirrus data sets used for this study are at much lower spatio-temporal resolution than the CarbonSat observations.

For aerosols the “GEMS aerosol product” (obtained from http://data-portal.ecmwf.int/data/d/gemsreanalysis/) as described and used in Heymann et al. (2012a), has been utilized. This data product is based on the assimilation of MODIS data. The time resolution is 12 hourly and the spatial grid is 1.125° × 1.125°. For this study primarily the AOD at 550 nm has been used.

For surface albedo, NASA’s filled surface albedo data product has been used. This product is based on a climatology (2000–2004) of MODIS MOD43B3 data (http://modis-atmos.gsfc.nasa.gov/ALBEDO/index.html). This climatology removes snow-covered pixels, which is not a problem for this study, as we limit the analysis to snow and ice free land surfaces. For the NIR band we use the MODIS albedo at 860 nm.

A number of other parameters are also stored in the L2e files. One example is near surface wind speed (obtained from ECMWF meteorological data). This parameter is relevant, for example, for the analysis of sun-glint observations over water. It is however
not used for this study, which focuses on non-glint observations over land surfaces. Using these input parameters (all stored in the L2e files) and the error parameterization scheme, the $X_{CO_2}$ and $X_{CH_4}$ errors have been computed for each single CarbonSat ground pixel.

Figure 9 illustrates this by showing the greenhouse gas errors as computed using the error parameterization scheme described in Appendix A for a single CarbonSat overpass over Germany. Figure 10 shows several other parameters for the same overpass, which are used as input parameters for the error parameterization scheme: albedo, AOD, COD and CTH. The assumed swath width is 500 km (CarbonSat’s goal swath width) corresponding to (at maximum, if all cloud free) 250 across-track ground pixels of size 2km × 2km. Gaps are due to thick clouds and additional quality filtering: Only those pixels are classified “good” for which the following conditions are all simultaneously met (simulated retrievals have shown that the quality of the retrievals is low if these conditions are not met):

- Cloud free (i.e. no thick clouds, see above),
- SZA < 70°,
- Albedo(NIR) > 0.05,
- Albedo(SWIR-1) > 0.05,
- Albedo(NIR)/Albedo(SWIR-1) < 4, and
- AOD(550 nm) + COD < 0.4 (approximately equivalent to AOD(NIR) + COD< 0.3 (see Sect. 4) assuming a wavelength dependence of the aerosol extinction inversely proportional to wavelength).

As can be seen, the $X_{CO_2}$ random error (i.e. the 1-sigma single measurement precision) is close to 1.2 ppm (Fig. 9a) with only some variations correlated with SWIR-1 albedo (Fig. 10a), as expected. This is also true for the $X_{CH_4}$ random error (Fig. 9c), which is close to 7 ppb. The $X_{CO_2}$ systematic error (Fig. 9b) typically differs from zero...
and is about 0.3 ppm on average. Variations around the mean value of 0.3 ppm are in the range ±0.3 ppm also correlated with albedo (Fig. 10a), but likely also to some extent with AOD (Fig. 10c), COD (Fig. 10c) and CTH (Fig. 10d), although this is not so obvious, as these correlations are quite low. Note that the spatial fine structure of all errors is primarily due to surface albedo variations (in the NIR and SWIR bands) but not due to aerosols and cirrus, as these data sets were only available at quite low resolution (especially for cirrus) as already explained. This is assumed to be appropriate for regional-scale inversion studies (assuming that essentially only the “average error” matters) but not necessarily for “point sources” (see following section) such as power plants (e.g. Bovensmann et al., 2010; Krings et al., 2011) or cities (e.g. Kort et al., 2012; Schneising et al., 2013). This aspect is further discussed in the following section.

As can be seen from Fig. 9, the $X_{CO_2}$ and $X_{CH_4}$ errors are highly correlated, as both gases suffer from the same underlying error sources (either instrument noise or systematic scattering related errors). The results shown in Fig. 9 are based on BESD/C “Full Physics” (FP) retrievals. To a good approximation the data shown in Fig. 9 can be used to estimate the corresponding errors for “Proxy” (PR) retrievals. For PR retrieval, the “dry air column” needed to convert the vertical column of the target gas (as given in, for example, number of molecules per cm$^2$) to a column-averaged mole fraction or mixing ratio (ppm or ppb), is not obtained from surface pressure (and the retrieved water column) but using a reference gas with (approximately) known mixing ratio, here either CO$_2$ or CH$_4$, as already explained above. PR retrievals do not require the use of the O$_2$–A (i.e. NIR) band of CarbonSat. PR retrievals are therefore essentially based on the retrieved column ratio of the two gases (times a correction factor). In order to estimated PR retrieval errors using given FP retrieval errors, the following approach can be used:

The ratio of $X_{CH_4}/X_{CO_2}$ defines a conversion factor $C$ between these two quantities, e.g. $C = 4.34$ ppb/ppm (= 1694.0 ppb/390.0 ppm) for the model atmosphere used here. Using this conversion factor, the $X_{CO_2}$ random error for a PR retrieval is given by $\sqrt{\sigma_{CO_2,FP}^2 + (\sigma_{CH_4,FP}/C)^2}$, where $\sigma_{CO_2,FP}$ is the $X_{CO_2}$ FP random error and $\sigma_{CH_4,FP}$
is the $X_{\text{CH}_4}$ FP random error. The corresponding formula for the $X_{\text{CH}_4}$ PR random error is $\sqrt{\sigma^2_{\text{CH}_4,\text{FP}} + (\sigma_{\text{CO}_2,\text{FP}} \times C)^2}$. The $X_{\text{CO}_2}$ PR systematic error can be estimated via $\epsilon_{\text{CO}_2,\text{FP}} - \epsilon_{\text{CH}_4,\text{FP}} / C$, where the $\epsilon$ are the corresponding FP systematic errors. As can be seen from this formula, the $X_{\text{CO}_2}$ PR error would be zero if the two systematic errors (after conversion of $X_{\text{CH}_4}$ FP error to the corresponding $X_{\text{CO}_2}$ error) are identical. For example, if the $X_{\text{CO}_2}$ FP error is $+1\%$ ($+3.9$ ppm) and the $X_{\text{CH}_4}$ FP error is also $+1\%$ ($+16.94$ ppb corresponding to $+3.9$ ppm after conversion), the $X_{\text{CO}_2}$ PR error would be zero. If however, in this case, the $X_{\text{CH}_4}$ error would be $-1\%$ instead of $+1\%$, the two errors would not cancel but add to a $+2\%$ ($+7.8$ ppm) $X_{\text{CO}_2}$ PR error. The $X_{\text{CH}_4}$ PR systematic error can be estimated using an analogue formula via $\epsilon_{\text{CH}_4,\text{FP}} - \epsilon_{\text{CO}_2,\text{FP}} \times C$.

Figure 11 illustrates this. The “PR errors” shown Fig. 11 are the “FP errors” shown in Fig. 9 but converted to PR errors using the formulas given here. As can be seen, the PR random errors are larger than the FP errors, but the systematic PR errors are much smaller compared to the corresponding FP errors due to cancellation of errors, as expected. For the systematic $X_{\text{CO}_2}$ errors the variation over the scene is only about 0.2 ppm, i.e. about a factor of four smaller compared to the FP errors. For $X_{\text{CH}_4}$ the results are similar; the systematic $X_{\text{CH}_4}$ PR error varies only about 1 ppb over the scene, which is also about four times smaller compared to the FP error. For random errors the opposite is true: the PR random errors are about 83% larger for $X_{\text{CO}_2}$ (2.2 ppm instead of typically 1.2 ppm for FP retrievals) and about 28% larger for $X_{\text{CH}_4}$ (9 ppb instead of typically 7 ppb).

In the following section, the data set shown in Fig. 9 is further discussed by using it to investigate to what extent CarbonSat can contribute to quantify anthropogenic $\text{CO}_2$ emissions of large cities using Berlin, the capital of Germany, as an example.
6 First application: Berlin CO₂ emissions from single “XCO₂ images”

In this section the data set presented in the previous section is used to investigate how accurately and precisely the anthropogenic CO₂ emissions of large cities can be derived from single overpass CarbonSat XCO₂ data, i.e. from so-called “XCO₂ images” as shown in, for example, Fig. 9.

Cities and large urban areas are home to the majority of today’s world population and are responsible for more than two thirds of the global energy-related CO₂ emissions. As pointed out in NRC (2010), and Kort et al. (2012) many cities have emission reduction policies in place, but lack objective, observation-based methods for verifying their outcomes. In a recent study, McKain et al. (2012), argue that observations of column-averaged carbon dioxide, e.g. from space, are presumably the most suitable method to detect emissions and emission trends from urban regions.

However, none of the existing satellites has been designed for such an application. Nevertheless, first attempts have been made to detect and quantify anthropogenic urban area CO₂ emissions using existing space-based observations. Schneising et al. (2008), analyzed three years of SCIAMACHY XCO₂ retrievals and showed that regionally elevated CO₂ over the highly populated region of western central Germany and parts of the Netherlands (“Rhine-Main area”) correlate with anthropogenic CO₂ emissions. In a follow-on study, Schneising et al. (2013), extended this analysis by also studying other regions and using a longer SCIAMACHY time series. They found, for example, for the highly populated Yangtze River Delta in China that a distinct positive trend of the regional XCO₂ enhancement exists, which is quantitatively consistent with anthropogenic emissions in terms of relative increase per year. Other studies focused on individual cities, primarily megacities such as Los Angeles (Wunch et al., 2009). Kort et al. (2012), found that by differencing GOSAT observations over megacities with those in nearby background, robust, statistically significant XCO₂ enhancements of 3.2 ± 1.5 ppm for Los Angeles and 2.4 ± 1.2 ppm for Mumbai can be derived. They conclude that these enhancements can be exploited to track anthropogenic emission
trends over time. Keppel-Aleks et al. (2012), studied to what extent space-based observations of $XCO_2$ help to constrain fossil fuel CO$_2$ emissions by using model simulations and GOSAT $XCO_2$ retrievals. They discuss how their approach can be used as a policy tool to verify national fossil emissions, as it provides an independent, observational constraint. They conclude that their model simulations clearly show the potential of their proposed approach but that their analysis using real GOSAT data is limited by the sparseness of the GOSAT data.

CarbonSat will deliver several orders of magnitude more data than GOSAT. One GOSAT observation requires 4 s but CarbonSat will deliver several hundred observations each second. In the following we present a first analysis aiming to answer the question of how accurately, precisely and frequently CarbonSat will be able to deliver information on city CO$_2$ emissions. For this purpose we show first results for Berlin. Berlin is a typical large city but not a megacity. Therefore Berlin has been selected but also because it is the capital of Germany, the home country of most of the authors of this study. Berlin is located in the north-east of Germany, covers a size of approximately 892 km$^2$, and has about 3.5 million inhabitants. Berlin is relatively well isolated, i.e. not a part of a large agglomeration of several cities. This is an advantage for the purpose of this study as it permits to clearly identify the anthropogenic CO$_2$ emission plume of Berlin in single CarbonSat “$XCO_2$ images”.

For this study we used a relatively high-resolution CO$_2$ modeling system and resulting data set for Europe as described in Pillai et al. (2010). The modeling system is based on the (Eulerian) high-resolution transport model WRF (Weather Research and Forecasting) coupled to a diagnostic vegetation model, the Vegetation Photosynthesis and Respiration Model (VPRM), to obtain a realistic distribution of atmospheric CO$_2$. The model set up utilizes high-resolution fossil fuel emission data at a spatial resolution of 10 km, prescribed from IER (Institut für Energiewirtschaft und Rationelle Energieanwendung), University of Stuttgart, Germany (http://carboeurope.ier.uni-stuttgart.de) to account for anthropogenic fluxes. Initial and lateral CO$_2$ tracer boundary conditions are calculated by the global atmospheric tracer transport model, TM3 (Heimann et al.,
2003), operated by MPI-Biogeochemistry (MPI-BGC) in Jena. These simulations are utilized to infer the Berlin emissions using a simple inverse modelling scheme based on linear least-squares with two free parameters: a constant offset for the entire analysed scene and a scaling factor for the anthropogenic $X_{CO_2}$ spatial pattern. We consider systematic errors of the CarbonSat $X_{CO_2}$ retrievals and also quantify the systematic error of the inferred emission caused by biogenic $X_{CO_2}$ variations. This is considered appropriate for the purpose of this study, which focuses on CarbonSat related errors, especially on estimating how random and systematic $X_{CO_2}$ errors map onto emission errors. For the future it is planned to use a more sophisticated inverse modelling method, for example, based on STILT (the Stochastic Time-Inverted Lagrangian Transport model) following the method described in Pillai (2011), using the inversion scheme of Gerbig et al. (2003) and Lin et al. (2004). STILT can be used as an adjoint of the Eulerian modelling system WRF-VPRM to derive biosphere-atmosphere exchange on local to regional scales (depending on the information content of the observations) from measured CO$_2$ mixing ratios (Pillai et al., 2012).

For this study we use WRF-VPRM simulations at 10km × 10km hourly resolution for three days mainly analyzing the data around local noon. These three days, in the following referred to as “scenarios” S1, S2, and S3, are described in Table 3. Scenarios S1 and S2 correspond to typical weekdays, where the anthropogenic (fossil) CO$_2$ emission of Berlin is assumed to be approximately 54 MtCO$_2$ yr$^{-1}$ (according to IER). The $X_{CO_2}$ enhancement of the CO$_2$ emission plume of Berlin relative to the background $X_{CO_2}$ is 1.47 ppm (at 10km × 10km resolution) for S1, where the near-surface wind speed is around 4.5 ms$^{-1}$ (Table 3). As expected (see, e.g. Bovensmann et al., 2010), the amplitude of the emission plume is approximately inversely proportional to near-surface wind speed. Therefore, for scenario S2, where the wind speed is 7.4 ms$^{-1}$, the $X_{CO_2}$ enhancement is reduced to 0.88 ppm. Scenario S3 corresponds to a Sunday. During Sundays the emissions are typically much lower than during weekdays, namely 31 MtCO$_2$ yr$^{-1}$ for S3 (according to IER for the day studied). The wind speed for S3 is 5.1 ms$^{-1}$ and the $X_{CO_2}$ enhancement due to the Berlin emissions is 0.54 ppm.
Figure 12 shows the $XCO_2$ contribution at 10km x 10km resolution of the biogenic fluxes (computed via VPRM, see above), the anthropogenic CO$_2$ emissions (using IER) and the corresponding anthropogenic $XCO_2$ contribution to the total $XCO_2$ for the three scenarios S1, S2 and S3 as computed with the WRF-VPRM modelling system. Berlin is located in the centre of the region shown in Fig. 12. Also shown (as a white rectangle) is the “target region” used for inferring the Berlin anthropogenic CO$_2$ emissions from the CarbonSat observation. The centre of the target region is Berlin (latitude 52.5° N, longitude 13.4° E) and the spatial extent is 3° x 3°.

As can be seen from Fig. 12, the modeled biogenic component of the $XCO_2$ is negative because in summer atmospheric CO$_2$ is taken up by growing vegetation resulting in a CO$_2$ flux from the atmosphere to the surface. More important for the purpose of this study is the spatial variation of the “disturbing” biogenic $XCO_2$ in the target region. As can be seen, the biogenic $XCO_2$ varies over the target region by about 0.5–2 ppm depending on scenario. Most critical for the purpose of this study are correlations of the biogenic $XCO_2$ pattern (Fig. 12, left panels) with the anthropogenic $XCO_2$ pattern (Fig. 12, right panels). The lower the correlations, the better the two components can be disentangled and the lower the systematic error of the CarbonSat-inferred anthropogenic CO$_2$ emissions. Note that the distance of the target centre to one of its boundaries, which is 1.5°, roughly corresponds to 150 km, which corresponds to approx. 8 h for air parcels travelling with 5 m s$^{-1}$. This means that the CO$_2$ emission plume is not only determined by the emission at the time of the overpass but by the (time dependence of) the emission during a time interval of several hours before the time of the overpass. This is considered when modelling the CO$_2$ emission plume. For the inversion results shown here it is assumed that the time dependence of the emissions in the time period of up to several hours before the overpass is sufficiently well known.

In the following we focus on investigating the impact of various systematic errors on the derived Berlin emissions. However, also the statistical (random) error of the derived emission is presented and discussed. It originates primarily from the random error of the measured $XCO_2$ which in turn is primarily due to instrument (detector) noise (but
which also to some extent depends on the retrieval algorithm). The $XCO_2$ random error is shown in Fig. 13, which is essentially a zoom into the data shown in Fig. 9a.

Systematic CarbonSat $XCO_2$ errors for scenario S1 are shown in Fig. 14 (left row). The top left panel is essentially a zoom into Fig. 9b, i.e. the error is the error as computed via the error parameterization using the smooth aerosol input data as shown in Fig. 10b. The top right panel shows the “observed $XCO_2$” in the Berlin centered target region, computed using the modeled $XCO_2$ plus the systematic error as shown in the top left panel. Here the modeled $XCO_2$ is the anthropogenic $XCO_2$ component only (model “A”), see middle right panel of Fig. 12. An offset (0.22 ppm, see figure annotation) has been subtracted. Here it is essentially assumed that the $XCO_2$ variability in the target region is dominated by anthropogenic CO$_2$ emissions and that, for example, $XCO_2$ from biogenic fluxes is essentially constant over the target region or that this component can be subtracted from the observations (we also investigate what happens if this assumption is not valid, see below). The Berlin assumed anthropogenic CO$_2$ emission is 54.80 MtCO$_2$ yr$^{-1}$ (see annotation).

Two additional numbers are listed in Fig. 14, which have been computed using the CO$_2$ emission inversion scheme: the random error (RE, in red) of the Berlin CO$_2$ emission as obtained by inverting the CarbonSat observations and the systematic error (SE, in black). These numbers have been obtained via the simple inversion scheme explained above. The basic assumption is that the spatial $XCO_2$ pattern can be modeled sufficiently well, not however its amplitude, which depends on the unknown anthropogenic CO$_2$ emission of Berlin. As explained, the inversion model has two free parameters: an offset and a second parameter, which scales the modeled anthropogenic $XCO_2$ spatial pattern. The offset considers the variable and not well known CO$_2$ background concentration. If the observed $XCO_2$ (Fig. 14, top right panel) differs from the modeled anthropogenic $XCO_2$ pattern, the retrieved CO$_2$ emission will typically differ from the true emission. In this case a systematic error of the retrieved CO$_2$ emission results. The size of this error depends on how much the $XCO_2$ systematic error correlates with the modeled $XCO_2$ pattern as used by the least squares procedure. Here the
systematic error (SE) is $+0.66\,\text{MtCO}_2\,\text{yr}^{-1}$ ($+1.2\%$) as shown in the figure annotation. It originates from the fact that the CarbonSat $X\text{CO}_2$ systematic error to some extent correlates with the Berlin CO$_2$ emission plume. The random error (RE) of the inferred emission is $4.53\,\text{MtCO}_2\,\text{yr}^{-1}$ (8.3%). It originates from the $X\text{CO}_2$ random error shown in Fig. 13.

These results have been obtained using the systematic error computed using the (quite low resolution) AOD data shown in Fig. 10b. This systematic CarbonSat $X\text{CO}_2$ error is in the following referred to as “$H_0$”. These AOD data are assumed to be appropriate for large-scale inversion studies (as explained above) but not necessarily for point sources and cities. The reason is that one would expect that the Berlin pollution plume contains not only additional CO$_2$ (relative to the background) but also additional aerosols. Therefore the potential impact of high spatial resolution aerosol variations has also been studied. A similar assessment has been made in Bovensmann et al. (2010) and Krings et al. (2011). To convert a local $X\text{CO}_2$ enhancement to a local AOD enhancement (at 550 nm), Bovensmann et al. (2010) used an AOD enhancement of 0.5 per 1% (4 ppm) $X\text{CO}_2$ enhancement. Krings et al. (2011), argue that this estimate is much too conservative and use an AOD enhancement of 0.05 per 1% $X\text{CO}_2$ enhancement. For this study we use a value in between, namely $\Delta\text{AOD}(550\,\text{nm}) = 0.2$ per 4 ppm $\Delta X\text{CO}_2$, i.e. anthropogenic $X\text{CO}_2$ enhancement. We have used the error parameterization formula (Appendix A) to compute the derivative of the $X\text{CO}_2$ systematic error due to an AOD enhancement, $\Delta\text{AOD}$, for each single CarbonSat observation shown in Fig. 9 and have multiplied these values with the modeled anthropogenic $X\text{CO}_2$ plume to get a likely more realistic $X\text{CO}_2$ systematic error (“$H_1$”; Fig. 15 shows the difference between the systematic errors $H_1$ and $H_0$). Note that we consider the worst case situation as it is assumed here that the aerosol error is perfectly correlated with the Berlin CO$_2$ plume. The results are shown in the middle row of Fig. 14. As can be seen, the systematic error of the inferred CO$_2$ emission of Berlin is $4.98\,\text{MtCO}_2\,\text{yr}^{-1}$ (9.1%), i.e. significantly larger than for error $H_0$ assumed for the results shown in the top row.
So far we have assumed that the spatial $XCO_2$ variability in the target region is only due to anthropogenic $CO_2$ (which is not true, see Fig. 12, left panels) or that other contributions, most notably biogenic $XCO_2$, can be accurately modeled (at least apart from a constant scaling factor for the spatial pattern of the biogenic $XCO_2$, which could be added as an additional parameter in the inversion scheme; this however has not been done for the results shown here). For the results shown in the bottom row of Fig. 14 we assume the other extreme, namely that the biogenic $XCO_2$ is a perturbation that cannot be modeled at all and therefore is not considered in the least squares inversion model but is present in the observed $XCO_2$ (see Fig. 14, bottom right), which is modeled using “model AB”, which computes $XCO_2$ as the sum of the anthropogenic and the biogenic $XCO_2$. As can be seen, the systematic error of the Berlin emission is $8.83 \text{MtCO}_2 \text{yr}^{-1}$ (16.1 %) in this case. Note that here we also use the worst case assumption of additional aerosols perfectly correlated with the Berlin $CO_2$ emission plume (i.e. systematic $XCO_2$ error “H1”) as also used for the results shown in the middle row. The results shown in the bottom row of Fig. 14 are therefore a worst-case estimate of the systematic error of the inferred $CO_2$ emission of Berlin for a single CarbonSat Berlin overpass.

We have performed the same investigation for the scenarios S2 (Fig. 16) and S3 (Fig. 17). The results for all three scenarios are summarized in Table 4. Comparing the random errors (precision) listed in Table 4 with the near-surface wind speeds for S1, S2 and S3 listed in Table 3, one finds that the random errors is proportional to wind speed and that, consistent with the results shown in Bovensmann et al. (2010), the random emission error is approximately $1 \text{MtCO}_2 \text{yr}^{-1}$ per $1 \text{m s}^{-1}$ wind speed (i.e. approximately $5 \text{MtCO}_2 \text{yr}^{-1}$ for $5 \text{m s}^{-1}$, etc.). For the real CarbonSat data the systematic emission error will likely be in between the quite extreme cases studied here. Note that the assumption used for “model A”, namely that only the anthropogenic $XCO_2$ pattern is relevant, can be tested using real CarbonSat data (when available) by subtracting the modeled biogenic $XCO_2$ from the Carbonsat observations and investigating if the
remaining $X_{CO_2}$ pattern is consistent with the expected $CO_2$ anthropogenic city emission plume or not.

We have analyzed the entire one year data set of CarbonSat observations using the 9 cases listed in Table 5. For case S1_H1_A, i.e. using scenario S1, systematic error H1, and model A, detailed results are shown in Fig. 18. Shown are the random and systematic $CO_2$ emission errors for all days where a “good” overpass occurred (defined by a sufficiently large number of observations at and around Berlin). The results are shown for a swath width of 240 km (black) and 500 km (green). The number of good overpasses is 22 for a swath width of 240 km and 39 for a swath width of 500 km. Also listed are a number of statistical figures of merit characterizing the random and systematic errors for both swath widths. The analysis as presented in Fig. 18 has been conducted for all 9 cases and the results are summarized in Table 5.

It has to be pointed out that the model simulations used here are at 10km x 10km resolution, which is coarser that the CarbonSat resolution of 2km x 2km. Efforts are underway to fully exploit the high resolution observations of CarbonSat by using a higher resolution modeling and inversion system. It can be expected that using higher resolution (inverse) modeling, systematic error can be reduced by better disentangling biogenic $X_{CO_2}$ variations from anthropogenic $X_{CO_2}$ signals but to what extent this is possible needs to be quantified in a future study.

Overall it can be concluded from the results shown here that by using CarbonSat single overpass $X_{CO_2}$ one can detect and quantify the anthropogenic $CO_2$ emissions of cities such as Berlin. The single observation random error is approximately 5–10 Mt$CO_2$ yr$^{-1}$ (10–20 % for Berlin). Systematic errors are expected to be on the same order. Their magnitude depends on which assumptions are used for the observational and modeling errors.
7 Analysis of global data

The CarbonSat observations will also be used to quantify CO$_2$ and CH$_4$ fluxes globally at regional scale spatial resolution and approximately monthly time resolution. In this section we present an overview about the global data. We discuss spatio-temporal averages of the $X$CO$_2$ and $X$CH$_4$ random and systematic errors, obtained from averaging the data contained in the L2e files, and also present detailed results for selected regions.

Figure 19 shows spatio-temporally averaged errors for July for a spatial grid of 5° × 5°. As can be seen, the mean $X$CO$_2$ random error (panel a) is typically close to 1.1 ppm, except for highly reflecting surfaces such as the Sahara, where the mean precision is in the range 0.5–0.8 ppm (simple direct average, i.e. not divided by the square root of the number of observations or equivalent). The mean systematic $X$CO$_2$ error (panel b) is typically within ±0.3 ppm but may reach or even exceed 0.4 ppm (positive and negative biases). The mean $X$CH$_4$ random error (panel c) is typically close to 7 ppb, except for highly reflecting surfaces such as the Sahara, where the mean precision is as low as approximately 4 ppb. The mean systematic $X$CH$_4$ error (panel d) is typically within ±2 ppb but also reaches approximately –4 ppb over large parts of central Africa. The number of observations is very large as shown in Fig. 20. Depending on the month, the number of quality filtered observations over snow and ice free land surfaces is in the range of 33–46 million per month. As described, the random and systematic errors are caused by and depend on critical parameters which have been used as input for the error parameterization scheme. For comparison with Fig. 19, these input parameters are shown in Fig. 21.

Finally, we present detailed results for selected regions, which are listed in Table 6. For each of these regions cumulative error distributions have been computed as shown in Figs. 22 and 23 and summarized in Table 6. As can be seen, systematic errors are mostly (approx. 85 %) below 0.3 ppm for $X$CO$_2$ (< 0.5 ppm: 99.5 %) and below 2 ppb for $X$CH$_4$ (< 4 ppb: 99.3 %). This finding together with the high single measurement...
precision and the large amounts of data to be expected from CarbonSat indicates that CarbonSat will be able to make significant contributions for improving our knowledge on the sources and sinks of these two very important greenhouse gases.

8 Limitations and outlook to future work

The error parameterization scheme permits one to compute random and systematic scattering related \(X_{\text{CO}_2}\) and \(X_{\text{CH}_4}\) errors for the six input parameters solar zenith angle, surface albedo in two bands, aerosol and cirrus optical depth, and cirrus altitude. As already pointed out, this scheme is more complex that previously used error parameterization schemes developed for other satellite missions (e.g. Hungershoefer et al., 2010) but it is still quite simple. For example, aerosol type variations are neglected and it is assumed that aerosol variability is confined to the boundary layer (here the lowest 2 km of the atmosphere).

For the error parameterization the aerosol type “Continental Average” (CA) from OPAC (Hess et al., 1998) is used as implemented in the radiative transfer model SCIA-TRAN (Rozanov and Kokhanovsky, 2006; Kauss, 1998). This aerosol type consists of a mixture of three components: “soot” (fraction: 0.541987), “water-soluble” (0.457987), and “dust-like” (0.000026). While this is assumed to be a reasonable choice for “average conditions” for observations over land, this does not cover, for example, more polluted scenes. To estimate the impact of this assumption we have performed a limited number of simulated retrievals. For example, when applying the BESD/C retrieval algorithm to a combination of different AODs, CODs and CTHs (45 combinations) we found for the VEG50 scenario (i.e. vegetation albedo and SZA 50°) that the mean \(X_{\text{CO}_2}\) bias and its scatter (1 sigma) is \(-0.18 \pm 0.27\) ppm for CA aerosol \((X_{\text{CH}_4}: -1.11 \pm 1.83\) ppb). When generating the simulated CarbonSat observations assuming that the aerosol is OPAC “Continental Polluted” (CP), the biases are very similar as for CA aerosols: \(-0.14 \pm 0.31\) ppm for \(X_{\text{CO}_2}\) and \(-1.09 \pm 1.69\) ppb for \(X_{\text{CH}_4}\) (for the CP aerosol the errors are even somewhat smaller but note that this is not a comparison between identical
scenes because of the quality filtering). The main difference between the two aerosol types are: CP aerosols contain more “soot” (69 % compared to 54 % for CA) but less “water-soluble” aerosol (31 % compared to 46 % for CA). However, aerosols are highly variable and errors can be larger depending on aerosol type. For example aerosol type “Desert”, which consists of much larger particles than CA and CP aerosols (composition: 87.1 % “water soluble” 11.7 % “mineral/nuclei mode”, 1.1 % “mineral/accumulation mode”), the biases are $0.54 \pm 0.40$ ppm for $XCO_2$ and $2.63 \pm 2.10$ ppb for $XCH_4$ as determined using the version of the BESD/C algorithm and its parameter settings including filtering criteria as used in this publication. Here a clear tendency for a high bias can be observed. This is partly because of a high bias (outliers) for certain scenes which are not filtered out (i.e. detected) by the currently used quality filtering scheme. Larger errors may also occur if the aerosol profile variability is not dominated by variability in the boundary layer (here: 0–2 km) but by variations in higher altitudes. For example, if we generate simulated CarbonSat observation with CP aerosols using extinction profiles which peak in the 2–4 km region the biases are $0.41 \pm 0.71$ ppm for $XCO_2$ and $1.96 \pm 3.16$ ppb for $XCH_4$ (for the retrieval we assume, as usual, CA aerosols mainly in the 0–2 km region). This shows that aerosol (and cirrus) type and vertical profile variations cannot be neglected. To better address these aspects will be a focus of our future activities.

We also plan to improve the analysis of how accurately, precisely and frequently anthropogenic $CO_2$ emissions of large cities such as Berlin can be derived from CarbonSat observations. This will include the study of other cities but also a refinement of the initial results presented here for Berlin. The latter will comprise detailed modelling of the anthropogenic and biogenic $XCO_2$ pattern for each single overpass instead of analyzing a limited number of scenarios as done here. It is expected that this will result in a somewhat reduced number of “good overpasses” as estimated here due to the possible inclusion of less favorable conditions (e.g. wind directions which do not permit one to clearly separate the Berlin emission plume from non-Berlin anthropogenic $XCO_2$ contributions).
9 Conclusions

The objective of the CarbonSat mission is to improve our understanding of natural and anthropogenic sources and sinks of the two most important anthropogenic greenhouse gases (GHG) carbon dioxide (CO$_2$) and methane (CH$_4$). The unique feature of CarbonSat is its “GHG imaging capability”, which is achieved via a combination of high spatial resolution (2km x 2km) and good spatial coverage achieved by a relatively wide swath and no gaps between ground pixel. The width of the across-track swath has not yet been finally decided. Here we presented results for two swath widths: 240 km (CarbonSat’s breakthrough requirement) and 500 km (goal requirement). This capability enables global imaging of localized strong emission sources such as cities, power plants, methane seeps, landfills and volcanos and better disentangling of natural and anthropogenic GHG sources and sinks.

Source/sink information can be derived from the retrieved atmospheric column-averaged mole fractions $X_{CO_2}$ and $X_{CH_4}$ (Level 2 products) via inverse modeling. We have presented an error analysis for CarbonSat $X_{CO_2}$ and $X_{CH_4}$ retrievals focusing on scattering related errors due to clouds and aerosols. The results have been obtained using the BESD/C “full physics” (FP) retrieval algorithm and using the most recent instrument and mission specification.

Errors due to aerosols and thin cirrus clouds are expected to dominate the error budget especially for $X_{CO_2}$ systematic errors. In order to quantify random and systematic errors, a one year data set of simulated CarbonSat nadir mode observations over land has been generated and analyzed. This has been achieved by developing an error parameterization scheme, which permits fast computation of random and systematic $X_{CO_2}$ and $X_{CH_4}$ retrieval errors and averaging kernels. The method is based on applying the BESD/C FP algorithm to simulated CarbonSat observations. The resulting $X_{CO_2}$ and $X_{CH_4}$ errors and averaging kernels have been parameterized using a linear regression method.
We have focused on scattering related errors obtained with the BESD/C FP retrieval method and using an error parameterization scheme which permits one to compute random and systematic errors for one year of simulated CarbonSat observations. Using this method, we have shown that systematic errors are mostly (approx. 85%) below 0.3 ppm for $X_{CO_2}$ (< 0.5 ppm: 99.5%) and below 2 ppb for $X_{CH_4}$ (< 4 ppb: 99.3%). The single measurement precision is typically 1.2 ppm for $X_{CO_2}$ and 7 ppb for $X_{CH_4}$ (1-sigma). For “proxy” (PR) retrievals, which are based on the retrieved $CH_4$ to $CO_2$ column ratio (or its inverse, depending on application), it has been estimated that the systematic errors are about a factor of four smaller compared to FP retrievals but that the PR random errors are about 83% larger for $X_{CO_2}$ (2.2 ppm instead of typically 1.2 ppm for FP retrievals) and about 28% larger for $X_{CH_4}$ (9 ppb instead of typically 7 ppb). We also have shown that the number of quality filtered observations per month over cloud and ice free land surfaces is in the range 33–46 million per month depending on month.

CarbonSat will also provide valuable information on Vegetation Chlorophyll Fluorescence (VCF) retrieved from clear Fraunhofer lines located around 755 nm. We estimate that the VCF single measurement precision is approximately 0.3 mWm$^{-2}$nm$^{-1}$sr$^{-1}$ (1-sigma) at 755 nm. For GOSAT, Frankenberg et al. (2012) found that the achieved single measurement precision is 0.5 mWm$^{-2}$nm$^{-1}$sr$^{-1}$ (1-sigma) at 755 nm. According to Guanter et al. (2010), VCF retrieval errors less than about 0.5 mWm$^{-2}$nm$^{-1}$sr$^{-1}$ would be valuable measurements as, for example, the expected signal variation at 760 nm is assumed to be in the range 0–4 mWm$^{-2}$nm$^{-1}$sr$^{-1}$.

Systematic VCF errors as determined using the very fast but simple retrieval method presented here are typically less than 0.2 mWm$^{-2}$nm$^{-1}$sr$^{-1}$. This systematic error estimate however does not include potential other error contributions such as intensity offsets (due to imperfect calibration). It also does not include possible errors due to Rotational Raman Scattering (RRS), which are expected to be small but may not be entirely negligible (Vasilkov et al., 2013).
As a first application the data set has been used to assess the capability of CarbonSat to quantify the \( \text{CO}_2 \) emissions of large cities using Berlin, the capital of Germany, as an example. It has been shown that the precision of the inferred Berlin \( \text{CO}_2 \) emissions obtained from single CarbonSat overpasses is in the range 5–10 \( \text{MtCO}_2 \text{ yr}^{-1} \) (10–20 %). Systematic errors could be on the same order. Our estimates depend on which assumptions are used with respect to observational systematic errors and biogenic \( \text{XCO}_2 \) modeling errors.

The results presented here indicate that CarbonSat will be able to make significant contributions to improving our knowledge on the sources and sinks of these two very important greenhouse gases. The data set presented here is currently being evaluated using global regional-scale inverse modeling to quantify this statement.

Finally, we have pointed out some of the limitations of the error parameterization method. Our scheme is more complex than previously used error parameterization schemes developed for other satellite missions (e.g. Hungershoefer et al., 2010) but it is still quite simple. For example, aerosol type variations are neglected and it is assumed that aerosol variability is confined to the boundary layer. To better address these aspects will be a focus of our future activities.

Appendix A

Error parameterization

Linear regression has been used to parameterize the \( \text{XCO}_2 \) and \( \text{XCH}_4 \) random and systematic errors (four quantities) and their averaging kernels. The averaging kernels (AK) as a function of pressure level (\( p \), used as vertical coordinate), \( \text{AK}(p) \), are approximated by a low-order polynomial defined by the three polynomial coefficients \( P_0, P_1, P_2 \), such that \( \text{AK}(p) = P_0 + P_1*p/p_0 + P_2*(p/p_0)^2 \), where \( p_0 \) is surface pressure. Three coefficients are used for the \( \text{XCO}_2 \) AK and three for the \( \text{XCH}_4 \) AK. In total 10 quantities have been parameterized.
The regression function used for the parameterization of each parameterized quantity $Q$ is:

$$Q = \sum_{i=0}^{7} C_i X_i.$$  \hspace{1cm} (A1)

Here $Q$ is any of the 10 to-be-parameterized quantities and $X_i$ is the $i$-th regression function and $C_i$ the corresponding regression coefficient. The regression functions are identical for all 10 quantities but the regression coefficients differ for each quantity. The regression functions are listed in Table 7 and the corresponding coefficients in Table 8. Regression function $X_0$ is a constant (offset). Each of the regression functions $X_1$-$X_7$ correspond to one of the six key inputs parameters (e.g. SZA, NIR albedo) or a combination of them ($X_7$) as listed in Table 7. Table 7 also lists the valid range of these input parameters (for example, the regression should not be used for SZA larger than about 80°).

After computation of $Q$ according to Eq. (A1), some further computations are needed to compute the final values of the $X_{CO_2}$ and $X_{CH_4}$ random and systematic errors: random errors: if the $X_{CO_2}$ or $X_{CH_4}$ random errors are less than (the pre-defined minimum value of) 0.7 ppm for $X_{CO_2}$ and 4.2 ppb for $X_{CH_4}$, the corresponding values should be set to these minimum values. This avoids unrealistically small (or even negative) random errors. Systematic errors: For the $X_{CO_2}$ and $X_{CH_4}$ systematic errors a “SZA bias correction” should be applied as follows: For $X_{CO_2}$ the term SZA/70-0.2 should be subtracted, and for $X_{CH_4}$ the term 8.0 × SZA/70.0-1.0. Without this correction the global bias maps (e.g. Fig. 9b and d) would show an obvious SZA dependent bias at high SZA, which could very likely be identified and corrected for when analyzing real CarbonSat data. More advanced bias correction schemes such as the ones currently used for, e.g. real GOSAT data (e.g. Crisp et al., 2012; Cogan et al., 2012), are however not used in this study.
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Table 1. CarbonSat instrument spectral parameters as used for this study.

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<th>NIR</th>
<th>Spectral band</th>
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<td>Spectral resolution</td>
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<td>FWHM (nm)</td>
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<td>160 at 1 × 10^{12}</td>
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<td>SNR (per spectral element) given as ( \text{SNR}<em>{\text{ref}} ) at ( L</em>{\text{ref}} ), where ( L_{\text{ref}} ) is a reference radiance value in ( \text{photons} , \text{cm}^{-2} , \text{nm}^{-1} , \text{sr}^{-1} ). Radiance ( (L) ) dependence of SNR: ( \text{SNR}(L) = \text{SNR}<em>{\text{ref}} \times \sqrt{L/L</em>{\text{ref}}} ) if ( L \geq L_{\text{ref}} ) and ( \text{SNR}(L) = \text{SNR}<em>{\text{ref}} \times L/L</em>{\text{ref}} ) if ( L &lt; L_{\text{ref}} ).</td>
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Table 2. BESD/C state vector elements (default settings). The corresponding spectra (columns) of the Jacobian matrix are shown in Fig. 2. For the retrieval the following 3 layers are used: Lower Troposphere (LT, ".00"), Upper Troposphere (UT, ".01"), Stratosphere (ST, ".02"). (*) The a priori surface albedo is obtained via a pre-processing step from the (nearly absorption free) continuum radiance in each band.

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<td>0.05 (rel.(*))</td>
</tr>
<tr>
<td>18</td>
<td>ALB_00</td>
<td>Surface albedo NIR band</td>
<td>0.05 (rel.(*))</td>
</tr>
<tr>
<td>19</td>
<td>CTH_00</td>
<td>Cirrus top height</td>
<td>0.1 (rel.)</td>
</tr>
<tr>
<td>20</td>
<td>COD_00</td>
<td>Cirrus optical depth</td>
<td>1.0 (rel.)</td>
</tr>
<tr>
<td>21</td>
<td>WOD_00</td>
<td>(Low lying thin) water cloud optical depth</td>
<td>1.0 (rel.)</td>
</tr>
<tr>
<td>22</td>
<td>AOD_SW2</td>
<td>AOD SWIR-2 band</td>
<td>0.5 (rel.)</td>
</tr>
<tr>
<td>23</td>
<td>AOD_NIR</td>
<td>AOD NIR band</td>
<td>0.5 (rel.)</td>
</tr>
<tr>
<td>24</td>
<td>H2O_00</td>
<td>Scaling parameter for water vapor profile</td>
<td>1.0 (rel.)</td>
</tr>
<tr>
<td>25</td>
<td>TEM_00</td>
<td>Shift parameter for temperature profile</td>
<td>0.1 (rel.)</td>
</tr>
<tr>
<td>26</td>
<td>VCF_00</td>
<td>Scaling factor for Vegetation Chlorophyll Fluorescence</td>
<td>variable (via DVCF retrieval pre-processing)</td>
</tr>
<tr>
<td>27</td>
<td>PRE_00</td>
<td>Surface pressure</td>
<td></td>
</tr>
<tr>
<td>28</td>
<td>CH4_02</td>
<td>Methane sub-column layer ST</td>
<td>0.001 (rel.)</td>
</tr>
<tr>
<td>29</td>
<td>CH4_01</td>
<td>Methane sub-column layer UT</td>
<td>0.005 (rel.)</td>
</tr>
<tr>
<td>30</td>
<td>CH4_00</td>
<td>Methane sub-column layer LT</td>
<td>0.10 (rel.)</td>
</tr>
<tr>
<td>31</td>
<td>CO2_02</td>
<td>CO2 sub-column layer ST</td>
<td>0.005 (rel.)</td>
</tr>
<tr>
<td>32</td>
<td>CO2_01</td>
<td>CO2 sub-column layer UT</td>
<td>0.005 (rel.)</td>
</tr>
<tr>
<td>33</td>
<td>CO2_00</td>
<td>CO2 sub-column layer LT</td>
<td>0.10 (rel.)</td>
</tr>
</tbody>
</table>
Table 3. Description of the three scenarios S1, S2, S3 as used for the Berlin CO₂ emission inversion study. For each scenario the used anthropogenic (fossil fuel) CO₂ emission of Berlin is listed and the resulting XCO₂ enhancement above the XCO₂ background value (see Fig. 12, right panels). The last column reports if the scenario corresponds to a weekday or not. Also listed is the near-surface wind speed (at 240 m; note that the wind speed is similar at other near-surface levels, e.g. 4.70 m s⁻¹ at 700 m for S1; S2: 7.55 m s⁻¹; S3: 5.29 m s⁻¹).

<table>
<thead>
<tr>
<th>Scenario</th>
<th>Berlin CO₂ emission (MtCO₂ yr⁻¹)</th>
<th>Anthropogenic XCO₂ peak enhancement (ppm)</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>S1</td>
<td>54.80</td>
<td>1.47</td>
<td>Weekday, wind speed 4.51 m s⁻¹</td>
</tr>
<tr>
<td>S2</td>
<td>53.89</td>
<td>0.88</td>
<td>Weekday, wind speed 7.44 m s⁻¹</td>
</tr>
<tr>
<td>S3</td>
<td>31.35</td>
<td>0.54</td>
<td>Sunday, wind speed 5.07 m s⁻¹</td>
</tr>
</tbody>
</table>
Table 4. Results of the Berlin CO$_2$ emission study. The first column lists the “case” defined by the scenario (S1, S2 or S3; see Table 3), the assumed systematic error of the CarbonSat XCO$_2$ retrievals (“H0” or “H1”; see below) and the assumed modeling error (“A” or “AB”; see below). The second column lists the used scenario. The third column reports which method has been used to compute the systematic XCO$_2$ error: the “default” error (“H0”) is the error computed via the error parameterization method using the input parameters, e.g. for AOD, as given in the L2e files (see Sect. 6). Because the AOD input parameters are only available at quite low resolution, error “H1” contains an additional aerosol related error which correlates perfectly with the Berlin anthropogenic CO$_2$ emission plume (worst case scenario; see also Fig. 15). This additional aerosol related error has been computed assuming ΔAOD(550 nm) = 0.2 per 1 % (4 ppm) ΔXCO$_2$ enhancement, where ΔXCO$_2$ is the XCO$_2$ enhancement relative to the background due to anthropogenic CO$_2$ emissions. The fourth column lists which assumption has to be used with respect to biogenic XCO$_2$ modeling errors: “A” means that it is assumed that the spatial pattern (not however the amplitude) of the anthropogenic CO$_2$ emission plume of Berlin can be accurately modeled in addition to accurate modeling of the spatial XCO$_2$ pattern due to biogenic emissions; modeling error “AB” assumes the other extreme: here it is assumed that the biogenic pattern cannot be modeled at all resulting in a significant systematic error of the modeling of the spatial XCO$_2$ pattern. The last two rows list the random and systematic errors of inferred Berlin anthropogenic CO$_2$ emission derived from a single overpass of CarbonSat over Berlin.

<table>
<thead>
<tr>
<th>Case</th>
<th>Scenario</th>
<th>Systematic XCO$_2$ error</th>
<th>Biogenic XCO$_2$ error</th>
<th>CO$_2$ emission error random (precision) (MtCO$_2$ yr$^{-1}$)</th>
<th>CO$_2$ emission error systematic (bias) (MtCO$_2$ yr$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>S1_H0_A</td>
<td>S1</td>
<td>default (H0)</td>
<td>no (A)</td>
<td>4.53 (8.3 %)</td>
<td>0.66 (1.2 %)</td>
</tr>
<tr>
<td>S1_H1_A</td>
<td>S1</td>
<td>additional aerosol (H1)</td>
<td>no (A)</td>
<td>4.83 (9.0 %)</td>
<td>4.98 (9.1 %)</td>
</tr>
<tr>
<td>S1_H1_AB</td>
<td>S1</td>
<td>additional aerosol (H1)</td>
<td>yes (AB)</td>
<td>5.34 (9.7 %)</td>
<td>8.83 (16.1 %)</td>
</tr>
<tr>
<td>S2_H0_A</td>
<td>S2</td>
<td>default (H0)</td>
<td>no (A)</td>
<td>6.70 (12.4 %)</td>
<td>-2.18 (-4.0 %)</td>
</tr>
<tr>
<td>S2_H1_A</td>
<td>S2</td>
<td>additional aerosol (H1)</td>
<td>no (A)</td>
<td>7.24 (13.4 %)</td>
<td>2.03 (3.8 %)</td>
</tr>
<tr>
<td>S2_H1_AB</td>
<td>S2</td>
<td>additional aerosol (H1)</td>
<td>yes (AB)</td>
<td>9.45 (17.5 %)</td>
<td>14.16 (26.3 %)</td>
</tr>
<tr>
<td>S3_H0_A</td>
<td>S3</td>
<td>default (H0)</td>
<td>no (A)</td>
<td>5.87 (18.7 %)</td>
<td>3.61 (11.5 %)</td>
</tr>
<tr>
<td>S3_H1_A</td>
<td>S3</td>
<td>additional aerosol (H1)</td>
<td>no (A)</td>
<td>6.45 (20.6 %)</td>
<td>6.10 (19.5 %)</td>
</tr>
<tr>
<td>S3_H1_AB</td>
<td>S3</td>
<td>additional aerosol (H1)</td>
<td>yes (AB)</td>
<td>4.16 (13.3 %)</td>
<td>-7.75 (-24.7 %)</td>
</tr>
</tbody>
</table>
Table 5. Results of the time series analysis with respect random and systematic errors of the Berlin CO$_2$ emissions for all 9 cases obtained from analyzing the one year data set of CarbonSat XCO$_2$ error simulations (detailed results for case S1_H1_A are shown in Fig. 18). The assumed swath width is 240 km. Note that the “Number of good overpasses” is not constant even for a given scenario (e.g. S3). This is because a “good” overpass is determined by the requirement that the uncertainty of the inferred CO$_2$ emission (as computed via the linear fit of the model to the observations) is required to be less than 25%. This uncertainty not only depends on the random error of the observations but also on their systematic error.

<table>
<thead>
<tr>
<th>Case</th>
<th>Number of “good” overpasses</th>
<th>CO$_2$ emission error (Mean ± Standard Deviation)</th>
<th>Systematic error (bias)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Random error (precision)</td>
<td></td>
</tr>
<tr>
<td>S1_H0_A</td>
<td>22</td>
<td>6.5 ± 2.4</td>
<td>11.8 ± 4.4</td>
</tr>
<tr>
<td>S1_H1_A</td>
<td>22</td>
<td>7.1 ± 2.7</td>
<td>13.0 ± 4.9</td>
</tr>
<tr>
<td>S1_H1_AB</td>
<td>18</td>
<td>6.6 ± 2.0</td>
<td>12.0 ± 3.6</td>
</tr>
<tr>
<td>S2_H0_A</td>
<td>19</td>
<td>8.1 ± 2.1</td>
<td>15.0 ± 3.9</td>
</tr>
<tr>
<td>S2_H1_A</td>
<td>17</td>
<td>8.3 ± 1.5</td>
<td>15.3 ± 2.7</td>
</tr>
<tr>
<td>S2_H1_AB</td>
<td>13</td>
<td>9.8 ± 1.9</td>
<td>18.2 ± 3.5</td>
</tr>
<tr>
<td>S3_H0_A</td>
<td>10</td>
<td>6.1 ± 0.9</td>
<td>19.4 ± 2.7</td>
</tr>
<tr>
<td>S3_H1_A</td>
<td>9</td>
<td>6.6 ± 0.8</td>
<td>21.2 ± 2.6</td>
</tr>
<tr>
<td>S3_H1_AB</td>
<td>21</td>
<td>5.3 ± 1.2</td>
<td>17.0 ± 4.0</td>
</tr>
</tbody>
</table>
Table 6. Regional cumulative error distribution results summarizing the percentages of errors less than a given value as shown in Figs. 22 and 23.

<table>
<thead>
<tr>
<th>Region ID</th>
<th>Region Name</th>
<th>Latitude (deg)</th>
<th>Longitude (deg)</th>
<th>Percentage of $X_{CO_2}$ retrievals with systematic error $&lt; 0.3$ ppm</th>
<th>Percentage of $X_{CH_4}$ retrievals with systematic error $&lt; 2$ ppb</th>
</tr>
</thead>
<tbody>
<tr>
<td>USA</td>
<td>USA</td>
<td>+20 – +49</td>
<td>-130 – -70</td>
<td>69.8</td>
<td>87.7</td>
</tr>
<tr>
<td>EUR</td>
<td>Europe</td>
<td>+35 – +60</td>
<td>-15 – +30</td>
<td>66.7</td>
<td>81.1</td>
</tr>
<tr>
<td>CHI</td>
<td>China</td>
<td>+20 – +50</td>
<td>+80 – +125</td>
<td>96.2</td>
<td>99.5</td>
</tr>
<tr>
<td>AUS</td>
<td>Australia</td>
<td>-45 – -10</td>
<td>+110 – +160</td>
<td>99.7</td>
<td>99.9</td>
</tr>
<tr>
<td>CAN</td>
<td>Canada</td>
<td>+49 – +70</td>
<td>-140 – -50</td>
<td>97.9</td>
<td>100.0</td>
</tr>
<tr>
<td>SIB</td>
<td>Siberia</td>
<td>+50 – +80</td>
<td>+60 – +130</td>
<td>88.9</td>
<td>99.4</td>
</tr>
<tr>
<td>AMA</td>
<td>Amazonia</td>
<td>-30 – +15</td>
<td>-90 – -30</td>
<td>97.1</td>
<td>89.2</td>
</tr>
<tr>
<td>CAF</td>
<td>Central Africa</td>
<td>-20 – +20</td>
<td>-25 – +50</td>
<td>83.6</td>
<td>60.2</td>
</tr>
</tbody>
</table>

4825
**Table 7.** Error parameterization regression functions X0–X7. The “Valid range” indicates the approximate range of values for which the parameterization is valid.

<table>
<thead>
<tr>
<th>Function</th>
<th>Definition</th>
<th>Explanation</th>
<th>Valid range</th>
</tr>
</thead>
<tbody>
<tr>
<td>X0</td>
<td>1.0</td>
<td>Constant offset</td>
<td></td>
</tr>
<tr>
<td>X1</td>
<td>SZA – 50.0</td>
<td>SZA in [deg]</td>
<td>0–80</td>
</tr>
<tr>
<td>X2</td>
<td>ALBN – 0.1</td>
<td>Albedo NIR band [–]</td>
<td>0.03–0.7</td>
</tr>
<tr>
<td>X3</td>
<td>ALBS – 0.1</td>
<td>Albedo SWIR-1 band [–]</td>
<td>0.03–0.7</td>
</tr>
<tr>
<td>X4</td>
<td>AOD – 0.2</td>
<td>Aerosol Optical Depth at 550 nm [–]</td>
<td>0–0.6</td>
</tr>
<tr>
<td>X5</td>
<td>COD – 0.05</td>
<td>Cirrus Optical Depth (NIR) [–]</td>
<td>0–0.6</td>
</tr>
<tr>
<td>X6</td>
<td>CTH – 10.0</td>
<td>Cirrus Top Height [km]</td>
<td>2–20</td>
</tr>
<tr>
<td>X7</td>
<td>AOD · INC_SZA · INC_ALB</td>
<td>where AOD as for X4 and INC_SZA = cos(84)/cos(SZA+9)·SZA/75</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>INC_ALB = (1.01/(ALBS+0.01)−1)·0.01</td>
<td></td>
</tr>
</tbody>
</table>
Table 8. Error parameterization regression coefficients C0–C7 for the regression functions listed in Table 7, each corresponding to one of the 10 parameterized quantities Q. Row CO₂.RE (CH₄.RE) contains the coefficients for the XCO₂ (XCH₄) random error. Row CO₂.SE (CH₄.SE) contains the coefficients for the XCO₂ (XCH₄) systematic error. Rows AK_CO₂.P0 to AK_CO₂.P2 list the coefficients for the XCO₂ averaging kernel polynomial coefficients P0, P1, and P2. Rows AK_CH₄.P0 to AK_CH₄.P2 list the coefficients for the XCH₄ averaging kernel polynomial coefficients P0, P1, and P2.

<table>
<thead>
<tr>
<th>Q</th>
<th>C0</th>
<th>C1</th>
<th>C2</th>
<th>C3</th>
<th>C4</th>
<th>C5</th>
<th>C6</th>
<th>C7</th>
</tr>
</thead>
<tbody>
<tr>
<td>CO₂.RE</td>
<td>1.29121</td>
<td>-0.00220</td>
<td>-0.07275</td>
<td>-1.97335</td>
<td>-1.00620</td>
<td>0.34586</td>
<td>-0.00150</td>
<td>38.86071</td>
</tr>
<tr>
<td>CO₂.SE</td>
<td>0.30786</td>
<td>0.01191</td>
<td>1.97716</td>
<td>-1.55154</td>
<td>-1.40282</td>
<td>0.70400</td>
<td>-0.03020</td>
<td>-73.46152</td>
</tr>
<tr>
<td>CH₄.RE</td>
<td>9.47532</td>
<td>-0.02678</td>
<td>-7.84754</td>
<td>-11.52154</td>
<td>-7.88635</td>
<td>15.80352</td>
<td>0.01702</td>
<td>275.25335</td>
</tr>
<tr>
<td>CH₄.SE</td>
<td>1.41086</td>
<td>0.05545</td>
<td>9.17830</td>
<td>-6.77504</td>
<td>-9.15046</td>
<td>5.52796</td>
<td>-0.48784</td>
<td>-335.04555</td>
</tr>
<tr>
<td>AK_CO₂.P0</td>
<td>0.25206</td>
<td>-0.00660</td>
<td>-0.97822</td>
<td>1.37264</td>
<td>-0.01718</td>
<td>-0.47370</td>
<td>-0.00132</td>
<td>2.50772</td>
</tr>
<tr>
<td>AK_CO₂.P1</td>
<td>1.34678</td>
<td>0.01515</td>
<td>3.96544</td>
<td>-4.98547</td>
<td>0.32270</td>
<td>0.24450</td>
<td>-0.00951</td>
<td>-15.62410</td>
</tr>
<tr>
<td>AK_CO₂.P2</td>
<td>-0.60245</td>
<td>-0.00851</td>
<td>-2.98224</td>
<td>3.62314</td>
<td>-0.29681</td>
<td>0.22898</td>
<td>0.01084</td>
<td>12.78807</td>
</tr>
<tr>
<td>AK_CH₄.P0</td>
<td>0.93580</td>
<td>-0.01024</td>
<td>-0.68970</td>
<td>-0.13586</td>
<td>0.03922</td>
<td>1.10047</td>
<td>0.00156</td>
<td>-1.59493</td>
</tr>
<tr>
<td>AK_CH₄.P1</td>
<td>-0.13742</td>
<td>0.02801</td>
<td>1.88213</td>
<td>0.18662</td>
<td>-0.20388</td>
<td>-2.84238</td>
<td>-0.01870</td>
<td>11.16231</td>
</tr>
<tr>
<td>AK_CH₄.P2</td>
<td>0.18796</td>
<td>-0.01763</td>
<td>-1.15321</td>
<td>-0.03191</td>
<td>0.19001</td>
<td>1.68905</td>
<td>0.01708</td>
<td>-10.43191</td>
</tr>
</tbody>
</table>
Fig. 1. CarbonSat nadir radiance (top panels), solar irradiance (2nd row), sun-normalized radiance (3rd row) and signal-to-noise ratio (bottom panels) spectra for vegetation albedo and a Solar Zenith Angle (SZA) of 50° ("VEG50 scenario").
Fig. 2. Typical BESD/C Jacobian matrix. For an explanation of each spectrum (= column of Jacobian matrix) see Table 2.
Fig. 3. Illustration of the CarbonSat BESD/C Vegetation Chlorophyll Fluorescence (VCF) pre-processing step. (a) Nadir radiance spectrum ($L$, SZA 40°, vegetation albedo, black line) and solar irradiance ($F$, red) normalized to their values at 749 nm. The difference is primarily due to VCF emission at the surface of 2.4 mW/m$^2$/nm/sr at 755 nm resulting in a difference of the slope and a “filling-in” of the solar Fraunhofer lines (most clearly visible at the two strong Fraunhofer lines located at 749.7 and 751.3 nm). (b) Simulated CarbonSat sun-normalized radiance ($I = L/F \cdot \pi$) measurement (black, with measurement error (grey vertical bars) and fitted VCF Jacobian – red, also shown separately in (c)). The retrieved VCF is 2.404 ± 0.245 mW/m$^2$/nm/sr (1-sigma).
Fig. 4. Results of the Dedicated VCF (DVCF) retrieval pre-processing step. Top: Retrieved VCF (y-axis) versus true VCF (x-axis) for 180 difference scenarios as defined by VCF emission, SZA and aerosol and cirrus optical depth (see blue text for details). The linear correlation coefficient between the retrieved and the true VCF is $r = 0.99$. The standard deviation of the difference between the retrieved and the true VCF is $0.19 \text{ mW/m}^2\text{ nm}^{-1}\text{ sr}^{-1}$. The random error (single observation precision) is $0.233 \text{ mW/m}^2\text{ nm}^{-1}\text{ sr}^{-1}$ on average (standard deviation $0.031 \text{ mW/m}^2\text{ nm}^{-1}\text{ sr}^{-1}$). Bottom: Relative difference between retrieved and true VCF as a function of the true VCF.
Fig. 5. Scenarios defined for the error parameterization. (a) Shows the model atmosphere Cirrus Optical Depth (COD) as green line for all 360 scenarios. The red line shows the a priori COD as used for BESD/C retrieval. The retrieved COD is shown as black line and black dots. Also listed are the scenario identifier indicating surface albedo – DES = desert, SAS = sand/soil, VEG = vegetation, WAT = water; see (d) – and Solar Zenith Angle – SZA, 00 = 0°, 25 = 25°, etc.; see (e). (b) As (a) but for Cirrus Altitude (Cloud Top Height – CTH). (c) As (a) but for Aerosol Optical Depth (AOD) at 765 nm (NIR band).
Fig. 6. BESD/C retrieval and error parameterization results. Shown are the unfiltered BESD/C results for all 360 scenarios (see Fig. 5) as light red solid line. The quality filtered BESD/C results are shown as red diamonds. The filtered results correspond to those retrievals where the retrieved AOD(NIR) + COD < 0.3. To model the quality filtered BESD/C results, an error parameterization scheme has been developed and the corresponding results are shown in black. Results are shown for the following parameters: (a) $XCO_2$ random error, (b) $XCO_2$ systematic error, (c) $XCH_4$ random error, and (d) $XCH_4$ systematic error.
Fig. 7. Zoom into Fig. 6 for the three SZA 50° scenarios corresponding to surface albedos sand/soil (SAS), vegetation (VEG) and water (WAT). As can be seen, the error parameterization tends to overestimate random errors except for very low albedo scenes (WAT), where the random errors are typically underestimated. As can also be seen, the error parameterization tends to produce a low bias (too negative systematic error), especially for the SAS and VEG albedo scenes, and does not capture the full variability of the biases for very low albedo scenes (WAT).
Fig. 8. As Fig. 6 but for the $X_{\text{CO}_2}$ and $X_{\text{CH}_4}$ averaging kernels at $p/p_o = 1.0$ (a and b) and $p/p_o = 0.5$ (c and d), where $p$ is the pressure level (altitude) and $p_o$ is surface pressure.
Fig. 9. $\text{XCO}_2$ and $\text{XCH}_4$ random (a and c) and systematic (b and d) retrieval errors for a single satellite overpass over Germany assuming a swath width of 500 km. Gaps are due to the limited swath width, (thick) clouds and other filtering criteria as explained in the main text. The errors have been computed using the error parameterization scheme. Some of the input data which have been used for computing these errors are shown in Fig. 10.
Fig. 10. As Fig. 9 but for the following parameters: (a) Surface albedo in the SWIR-1 band, (b) AOD in the NIR band, and the cirrus parameters COD (c) and CTH (d).
Fig. 11. As Fig. 9 but for “proxy” (PR) retrievals. As can be seen by comparison with Fig. 9, the random errors are larger (as two quite noisy retrievals are combined) but the systematic errors are much smaller, as many errors are common for CO₂ and CH₄ and therefore cancel if the ratio of the retrieved columns is computed.
Fig. 12. From left to right: Modeled biospheric $XCO_2$ component (in ppm), anthropogenic (fossil) $CO_2$ emissions (in Mt$CO_2$ per gridcell and per year, where one grid cell is $10km \times 10km$), and modeled anthropogenic (fossil) $XCO_2$ component (in ppm; see main text for details). Each row corresponds to a different day in summer around local noon (from top to bottom: “scenario” S1, S2, S3). The days have been selected to represent different conditions (wind speed and direction, $CO_2$ emissions). The target region used for emission inversion is shown by the white rectangles. The city center of Berlin is indicated by the black diamond located in the center of the target region. Note that for the data shown in the middle and last row the minimum value has been subtracted (i.e. the lowest value in the target region is zero) for better comparison with the inversion results shown in Figs. 14–17.
Fig. 13. $XCO_2$ random error (single measurement precision) around Berlin (zoom in Fig. 9a).
\textbf{Fig. 14.} Inversion results for scenario S1. Top left: CarbonSat $X_{CO_2}$ systematic error “H0” computed by neglecting additional aerosols correlated with the Berlin CO$_2$ emission plume. Top right: simulated CarbonSat $X_{CO_2}$ observation computed as systematic error plus modeled anthropogenic (model “A”) $X_{CO_2}$. Also listed are the number of CarbonSat observations in the target region (Nobs), the anthropogenic CO$_2$ emission (“E”), and the random error (“RE”) and the systematic error (“SE”) of the inferred Berlin CO$_2$ emissions (both in MtCO$_2$ yr$^{-1}$ and in percent). Middle row: as top row but for systematic error “H1” computed considering additional aerosols perfectly correlated with the Berlin emission plume. Bottom row: as middle row but assuming that biospheric $X_{CO_2}$ “disturbs” the inversion but cannot be modeled (model “AB”).
Fig. 15. Difference between systematic errors H1 and H0, i.e. H1–H0 (see Table 4). As can be seen by comparison with the results shown in Figs. 15–17, the bias due to additional aerosols in the Berlin CO$_2$ emission plume has been computed such that it perfectly correlates with the CO$_2$ emission plume (worst case). The amplitude of the error is about 0.07 ppm for scenario S1 and about 0.04 ppm for scenarios S2 and S3. Note that for each of the three maps an offset has been subtracted such that the minimum value is zero for each map.
**Fig. 16.** As Fig. 14 but for scenario S2.
Fig. 17. As Fig. 14 but for scenario S3.
**Fig. 18.** Estimation of random (top) and systematic (bottom) CO$_2$ emission errors for CarbonSat Berlin overpasses obtained from analyzing the entire one year data set of simulated CarbonSat XCO$_2$ retrievals for case S1_H1_A (see Table 4). Shown are the results for a swath width of 240 km (black) and 500 km (green) and for all days (overpasses) where the number of CarbonSat observations at and around the Berlin CO$_2$ emission plume is sufficiently large to obtain a CO$_2$ emission random error of less than 25%. This number is 22 for a swath width of 240 km and 39 for a swath width of 500 km (see “N good overpasses”). Also listed are a several figures of merit obtained from a statistical analysis to summarize the results (middle right for the random error; bottom right for systematic error). For example the random error of the inferred emission is less than 20% for 86% for all overpasses for a swath width of 240 km. The mean random error is 7.1 MtCO$_2$ yr$^{-1}$ (13.0%) and the standard deviation is 2.7 MtCO$_2$ yr$^{-1}$ (4.9%). Table 5 summarized the results of this analysis for all nine cases.
Fig. 19. Spatially averaged (5° × 5°) errors for July for a swath width of 240 km. For this figure all quality-filtered cloud-free observations over snow and ice free land surfaces have been averaged.
Fig. 20. Number of quality-filtered CarbonSat observations over snow and ice free land surfaces for January (a), April (b), July (c) and October (d) within each 5° × 5° grid cell for a swath width of 240 km in units of 1000 observations per grid cell. The total number of observations per month is: 33.15 × 10^6 for January, 40.40 × 10^6 for April, 46.28 × 10^6 for July, and 43.24 × 10^6 for October.
Fig. 21. As Fig. 19 and 20 but for the parameters SZA (a), AOD in the NIR band (b), COD (c), surface albedo in the NIR band (d), surface albedo in the SWIR-1 band (e) and CTH (f).
Fig. 22. Regional cumulative error distributions for the four regions United States of America (USA), Europe (EUR), China (CHI) and Australia (AUS) for July. Also listed for each region is the percentage of the individual CarbonSat observations in that region with a systematic error (SE) less than a given value (red for $X_{CO_2}$, green for $X_{CH_4}$).
Fig. 23. As Fig. 22 but for the four regions Canada (CAN), Siberia (SIB), Amazonia (AMA) and Central Africa (CAF).