Uncertainty characterization of AOD for the AATSR dual and single view retrieval algorithms

P. Kolmonen¹, A.-M. Sundström², L. Sogacheva¹, E. Rodriguez¹, T. Virtanen², and G. de Leeuw¹,²

¹Finnish Meteorological Institute, Erik Palmenin Aukio 1, 00560 Helsinki, Finland
²Department of Physics, University of Helsinki, Gustav Hällströmin katu 2a, 00560 Helsinki, Finland

Received: 6 March 2013 – Accepted: 18 April 2013 – Published: 29 April 2013

Correspondence to: P. Kolmonen (pekka.kolmonen@fmi.fi)

Published by Copernicus Publications on behalf of the European Geosciences Union.
Abstract

The uncertainty associated with satellite-retrieved aerosol properties is needed when these data are used to constrain chemical transport or climate models by using data assimilation. Global uncertainty as provided by comparison with independent ground-based observations is usually not adequate for that purpose. Rather the per-pixel uncertainty is needed. In this work we describe how these are determined in the AATSR dual and single view aerosol retrieval algorithms (ADV and ASV) which are used to retrieve aerosol optical properties from reflectance measured at the top of the atmosphere. AATSR is the Aerosol Along-Track Scanning Radiometer which flies on the European Space Agency Environmental Satellite ENVISAT. In addition, issues related to multi-year retrievals are described and discussed. The aerosol optical depth (AOD) retrieved for the year 2008 is validated versus ground-based AERONET sun photometer measurements with good agreement ($r = 0.85$). The comparison of the AOD uncertainties with those provided by AERONET shows that they behave well in a statistical sense. Other considerations regarding global multi-year aerosol retrievals are presented and discussed.

1 Introduction

Atmospheric aerosols have a strong effect on the Earth climate due to their reflection and absorption of solar radiation (direct effect) and because they can act as cloud condensation nuclei and thus affect cloud properties (indirect effect). Aerosol particles also have an adverse effect on human health and are important for heterogeneous chemical processes in the atmosphere. To assess the effects of aerosols, their spatial and temporal distributions need to be known. Accurate information can be obtained from ground-based measurements, but these are representative for only a limited area. Information on regional and global scales can be obtained from satellite data. Algorithms have been developed to retrieve information from the radiation at the top of
the atmosphere (TOA) measured by satellite-based instruments, i.e. radiometers and spectrometers. This information can be used to constrain chemical transport models by data assimilation (e.g. Benedetti et al., 2009) or to evaluate model results. Such combination of measurements and models aims to provide the best possible information on the occurrence and concentrations of aerosol particles.

For the assimilation of satellite-retrieved aerosol properties in transport models the data must meet a number of requirements which have been studied extensively by, e.g., Hyer et al. (2011). One of these is a thorough understanding of the uncertainty characteristics. Global uncertainties as provided by comparison with independent ground-based observations are usually not adequate for that purpose. Rather the per-pixel uncertainty is needed. This is mainly because of the large variation of the reflectance of the underlying surface. For instance, the TOA reflectance over a highly reflecting surface is more intense than over a dark surface but the aerosol signal over adjacent pixels would be the same and, thus, more difficult to entangle from the total TOA signal. Hence, the retrieval uncertainty depends on the underlying surface. Another critical issue for data assimilation is the possible bias in the data. Data outliers can lead the assimilation to erroneous results.

In global climate modelling the assimilation of the retrieved aerosol properties differs slightly. Huneeus et al. (2012) show that a uniform uncertainty in the satellite-retrieved data needs to be used to avoid unwanted bias in the model results. Satellite retrievals can be used, however, as reference for global models, and well-defined retrieval uncertainty is very much needed for this purpose.

In this paper the retrieval of aerosol properties using TOA radiances measured by the Advanced Along-Track Scanning Radiometer (AATSR), flying on the European Space Agency (ESA) environmental satellite ENVISAT, is described, including uncertainty characterisation. AATSR is the third in a series of along track scanning radiometers. They were originally designed to measure Sea Surface Temperature (SST) with high accuracy and precision. The instrument offers two views, one near-nadir and the other one at 55° forward, which together with the multiple wavelengths renders the instrument
suitable for the retrieval of aerosol properties. The centre wavelengths of the AATSR channels are 0.555, 0.659, 0.865, 1.61, 3.70, 10.85, and 12.00 µm.

A number of algorithms have been developed for aerosol retrieval over land using AATSR data. The retrieval algorithms described in this paper for use over land and water build on those developed by Veefkind et al. (1998) and Veefkind and de Leeuw (1998), respectively. The dual-view algorithm (ADV) for aerosol retrieval over land was originally developed by Veefkind et al. (1999). It differs significantly from the Swansea algorithm by North et al. (1999); Grey et al. (2006), or the Oxford-RAL algorithm (Thomas et al., 2009) in the way the surface reflectance is handled. ADV uses both views to eliminate the surface reflectance from the TOA signals as described below. In the Swansea algorithm, a surface reflectance model is used which makes it possible to retrieve aerosol properties and surface reflectance simultaneously (North et al., 1999). The Oxford-RAL algorithm relies on information from the retrieval of another instrument: the land surface bi-directional reflectance product of MODIS (Moderate resolution Imaging Spectrometer).

The over-ocean retrieval is based on modelling of the TOA reflectance and then minimizing the discrepancy between the measured and modelled reflectance. The ASV (AATSR Single-View) algorithm, described below, currently utilizes only one of the AATSR views.

In this paper we describe recent improvements and extensions of the ADV and ASV algorithms. The principles of the ASV and ADV methods have been introduced in several earlier publications (Veefkind and de Leeuw, 1998; Veefkind et al., 1999; Curier et al., 2009), but this information is necessarily duplicated to some extent in Sects. 2 and 3, to provide context for recent modifications and improvements of the algorithms and extensions, e.g., to include uncertainty estimation (Sects. 2.3 and 3.4) and to remove outliers (Sect. 4.2). With AATSR and its predecessor instrument ATSR-2, a 17 yr aerosol data set can be retrieved. Issues related to producing the time series are introduced and discussed in Sect. 4.3. AOD data for one year and their uncertainties are evaluated by comparison with AERONET data in Sect. 5.
2 ADV algorithm for over land retrieval

2.1 Formal background of the dual-view algorithm

The AATSR dual-view algorithm ADV uses the TOA reflectance at 3 wavelengths in both the nadir and forward views for retrieval of aerosol properties over land (Veefkind et al., 1999, 2000; Robles González, 2003; Curier at al., 2009). These properties include aerosol optical depth (AOD) for three wavelengths (nominally 0.555, 0.659 and 1.61 µm). In addition, an aerosol model is retrieved.

The aerosol model is a mixture of four aerosol components each of which is described by a log-normal size distribution defined by an effective radius and a standard deviation (see Sect. 2.2), and a complex refractive index. Two of the aerosol components define small particles and the other two coarse particles. One of the small particle components is non-absorbing while the other one is strongly absorbing. By mixing these two components the absorption of the small particles can arbitrarily be set. The coarse particle components are sea salt and desert dust. Desert dust is composed of non-spherical particles; the other three components are assumed to consist of spherical particles. The aerosol components are adopted from the ESA Aerosol CCI (Climate Change Initiative) project\(^1\) (Holzer-Popp et al., 2013; de Leeuw et al., 2013). The properties of the components are described in Table 1. The aerosol model used in the retrieval is determined by first mixing the small and large components separately, and then mixing the ensuing small and coarse modes. The mixing ratios are selected during the retrieval process by fitting the aerosol model to the reflectance measured at three (four over ocean) wavelengths, except for the dust fraction which is selected from an aerosol climatology based on the median of 13 global models as described in (Holzer-Popp et al., 2013). The mixing ratio of non-absorbing and absorbing fine components is retrieved semi-freely. The mixing ratio can have any value in the range

\(^1\)http://www.esa-aerosol-cci.org/
of ±0.3 from the AEROCOM climatology value. The fine–coarse mixture is retrieved completely independent of the climatology.

The algorithm is based on a number of assumptions:

- TOA reflectance $\rho$ is of the form (Veefkind et al., 2000)

$$\rho(\mu_0, \mu, \phi, \lambda) = \rho_a(\mu_0, \mu, \phi, \lambda) + \frac{T(\mu_0, \mu, \phi, \lambda)\rho_g(\mu_0, \mu, \phi, \lambda)}{1 - s(\lambda)R_s(\lambda)}, \quad (1)$$

where $\rho_a$ is the reflectance due to the atmosphere, $\rho_g$ is the surface reflectance, $T$ is the product of downward and upward atmospheric transmittance, $s$ is the atmospheric backscatter ratio, and $R_s$ is the surface albedo. Reflectance and transmittance parameters: $\mu_0$ is the solar zenith angle, $\mu$ is the viewing (satellite) zenith angle, $\phi$ is the relative azimuth angle between the sun and the satellite, and $\lambda$ is the wavelength. Note that, for method development purposes, multiple scattering between the surface and the atmosphere is assumed to be angle-independent i.e. surface albedo $R_s$ is used in the numerator of Eq. (1) instead of surface reflectance $\rho_g$. It has been suggested that multiple scattering in the surface-atmosphere system will lead to isotropically distributed scattering (Wanner et al., 1997) which supports the use of surface albedo instead of reflectance.

- Atmospheric reflectance

$$\rho_a(\mu_0, \mu, \phi, \lambda) = \rho_R(\mu_0, \mu, \phi, \lambda) + \rho_{aer}(\mu_0, \mu, \phi, \lambda), \quad (2)$$

where $\rho_R$ is reflectance due to Rayleigh scattering and $\rho_{aer}$ is reflectance due to aerosols.

- Reflectance due to aerosols is computed using the modified linear mixing method by Abdou et al. (1997) assuming external mixture of the aerosol particles. The method as adapted to ADV for two aerosol components is

$$\rho_{aer} = b_1 \frac{\omega_{mix}}{\omega_1} e^{-\tau_1|\omega_1 - \omega_{mix}|} \rho_1 + b_2 \frac{\omega_{mix}}{\omega_2} e^{-\tau_2|\omega_2 - \omega_{mix}|} \rho_2, \quad (3)$$

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where $\omega$ is the single scattering albedo (SSA) and $\tau$ is AOD. Subscripts 1 and 2 refer to two aerosol components while mix refers to their mixing ratio. Reflectance due to an aerosol component is $\rho$, and SSA mixture is

$$\omega_{\text{mix}} = b_1 \omega_1 + b_2 \omega_2.$$  \hfill (4)

For the weighting coefficients $b_1 + b_2 = 1$. The modified linear mixing method is applied to better account for the effects of mixing two aerosol components with different absorbing properties. This is done by introducing the single scattering albedo into linear mixing. If the SSAs of the aerosol components are identical, Eq. (3) simplifies to

$$\rho_{\text{aer}} = b_1 \rho_1 + b_2 \rho_2.$$  \hfill (5)

The needed aerosol transmittance is computed using linear mixing.

The ratio of the surface reflectance measured in the forward and nadir views, $k$, is independent of wavelength (Flowerdew and Haigh, 1995):

$$k = \frac{\rho^f_g(\mu_0, \mu, \phi, \lambda)}{\rho^n_g(\mu_0, \mu, \phi, \lambda)},$$  \hfill (6)

where $\rho^f_g$ and $\rho^n_g$ are the forward and nadir surface reflectance, respectively. The $k$ ratio is evaluated for the measured reflectance in the 1.61 $\mu$m wavelength band using equation

$$k = \frac{\rho^f_g(\mu_0, \mu, \phi, 1.61 \mu\text{m})}{\rho^n_g(\mu_0, \mu, \phi, 1.61 \mu\text{m})}.$$  \hfill (7)

The aerosol contribution at this wavelength is relatively small (except in the presence of coarse particles such as dust or sea spray aerosol).
– The $k$ ratio is not reliable for bright surface reflectance. For this reason, if the measured nadir reflectance at 1.61 µm is above 0.45, retrieval is not done.

– The 0.865 µm channel is excluded from the retrieval because the $k$ ratio assumption is usually not valid as there is a strong reflectance by vegetation at this wavelength (Robles González et al., 2000).

With these assumptions Eq. (1) can be written separately for the forward and nadir views. Then, by combining these equations while keeping in mind that the multiple scattering is assumed to be angle independent, relation

$$\frac{\rho_n(\mu_0, \mu, \phi, \lambda) - \rho_a^n(\mu_0, \mu, \phi, \lambda)}{\rho_g^n(\mu_0, \mu, \phi, \lambda)T^n(\mu_0, \mu, \phi, \lambda)} = \frac{\rho_f(\mu_0, \mu, \phi, \lambda) - \rho_a(\mu_0, \mu, \phi, \lambda)}{\rho_g^f(\mu_0, \mu, \phi, \lambda)T^f(\mu_0, \mu, \phi, \lambda)}$$

(8)

can be made formally. The key aspect of the dual-view algorithm is to introduce the $k$ ratio in Eq. (8) to obtain

$$\frac{\rho_n(\mu_0, \mu, \phi, \lambda) - \rho_a^n(\mu_0, \mu, \phi, \lambda)}{T^n(\mu_0, \mu, \phi, \lambda)} = \frac{\rho_f(\mu_0, \mu, \phi, \lambda) - \rho_a(\mu_0, \mu, \phi, \lambda)}{kT^f(\mu_0, \mu, \phi, \lambda)}.$$  

(9)

Now all the needed knowledge about surface reflectance is in the $k$ ratio.

### 2.2 Computational aspects of ADV

Modeled values of the atmospheric reflectance $\rho_a$ and transmittance $T$ must be determined in order to use Eq. (9) for the retrieval of aerosol properties. These values, together with other information, can be computed using radiative transfer (RT) methods. RT methods provide a way to solve the forward problem of the retrieval which for the case of atmospheric reflectance can be stated as: for given atmospheric conditions (aerosol and gas concentrations) determine the amount of incoming solar radiation that is reflected from the atmosphere towards a satellite instrument. Note that the surface reflectance contribution is omitted here as the ADV algorithm formally eliminates it.
During a retrieval the forward problem must be solved numerous times which is time consuming. The most common technique to overcome this is to perform the radiative transfer calculations for a set of fixed variables before the retrieval. The calculated values are arranged into a multi-dimensional array that is called a look-up-table (LUT). During the retrieval the actual values for the required variables can be quickly obtained by interpolation between values available from the LUT. The chosen RT algorithm that is used with ADV is DAK (Doubling Adding KNMI), Haan et al. (1987). To ensure reliable LUT values, the RT algorithm is limited to solar zenith angles smaller than 75°.

LUTs are computed for each aerosol component. The size distribution of an aerosol component is described by a log-normal number size distributions of the form

$$\frac{dN}{d\ln r} = \frac{N_0}{\ln \sigma \sqrt{2\pi}} \exp \left( -\frac{\ln^2(r/r_g)}{2\ln^2 \sigma} \right),$$

where \( r \) is the particle radius, \( r_g \) is the geometric mean radius, \( \sigma \) is the standard deviation \( \sigma \) (Heintzenberg, 1994). The total number of aerosol particles \( N_0 \) depends on the aerosol load. Aerosol optical properties are computed by applying Mie calculations (Mie, 1908) except for non-spherical dust particles where the T-matrix method is used (Mischenko and Davis, 1994). These calculations require knowledge of the aerosol particle size distribution and refractive index which for the the aerosol components used here are given in Table 1.

The LUTs are computed for discrete sun zenith, viewing zenith and relative azimuth angles, for each AATSR wavelength, and for a number of reference AOD levels. Currently, 15 discrete values ranging from 0 to 90° are used for the zenith angles and 19 discrete values between 0 and 180° are used for the azimuth angles. Typically ten AOD levels ranging from 0.05 to 4.0 at \( \lambda = 0.500 \mu m \) are used. Transmittance and reflectance for Rayleigh (gas) scattering are computed in standard atmospheric conditions. To ensure that the result of the radiation transfer computations are not influenced by refraction effects due to the earth curvature, the maximum values for the sun and viewing zenith angles has been set to 75°.
Equation (9) shows that the computational task is to find the aerosol component mixture and reference AOD level that solve the equation for all three AATSR wavelengths simultaneously. Due to measurement and modeling errors this task is impossible in practice. Instead, the task can be converted to a least-squares type of problem

$$\arg_{b_{\text{fine}}, b_{\text{naf}}, L} \min \sum_{i=1}^{N_\lambda} \left[ \frac{\rho^m_i(L_i) - \rho^n_a(b_{\text{fine}}, b_{\text{naf}}, L, \lambda_i)}{T^n(b_{\text{fine}}, b_{\text{naf}}, L, \lambda_i)} - \frac{\rho^f_m(L_i) - \rho^f_a(b_{\text{fine}}, b_{\text{naf}}, L, \lambda_i)}{kT^f(b_{\text{fine}}, b_{\text{naf}}, L, \lambda_i)} \right]^2, \quad (11)$$

where the subscript m now indicates the measured TOA reflectance. The fraction of the fine mode particles is $b_{\text{fine}} \in (0,1)$, the non-absorbing component in fine particle mixture is $b_{\text{naf}} = b_{\text{naf},A} \pm 0.3$ with $b_{\text{naf}} \in (0,1)$, and the reference AOD level is $L \in (1,10)$. The mixture $b_{\text{naf},A}$ is the AEROCOM a priori value. Note that the dust fraction is not retrieved but the AEROCOM climatology value is used. The angle arguments $(\mu_0, \mu, \phi)$ have been omitted for brevity. The number of wavelengths $N_\lambda = 3$.

The reference AOD level $L$ is here used instead of AOD as it is the parameter that is applied in the actual solving of Eq. (11). This parameter is used when AOD, aerosol reflectance, and transmittance are determined from the aerosol LUTs.

Equation (11) also shows that the modeled atmospheric reflectance and transmittance are functions of the decision arguments $b_{\text{fine}}, b_{\text{naf}}$ for aerosol component mixtures and $L$ for the reference AOD level. The task is now to find the decision arguments $(b_{\text{fine}}, b_{\text{naf}}, L)$ that minimize the least-squares sum. The modified linear mixing method introduced in Eq. (3) is applied with all mixtures for the computation of reflectance.

The minimization problem Eq. (11) can be optimized by applying mathematical optimization methods. Here the chosen method is Levenberg-Marquardt (see for example Gill et al., 1999). It is a trust-region type method which is well-suited for least-squares problems, and is meant for unconstrained optimization. The latter feature causes additional considerations as the decision arguments are all box-constrained. This is handled in the evaluation of the least-squares sum where strict barrier functions are used to constrain the solution (Gill et al., 1999).
Another feature of the Levenberg–Marquardt method is that it is a local optimizer. It will converge efficiently to the nearest local minimum. To increase the probability of finding the globally best solution an initial search is done in a limited discrete set of decision parameters: ten mixtures $b_{\text{fine}}, b_{\text{naf}}$, and ten AOD levels $L$. The results of the search are then used as the initial guess for the Levenberg-Marquardt method.

When all decision parameters have been set during the retrieval the resulting AOD $\tau$ can be computed from the LUTs:

$$\tau(\lambda) = b_{\text{fine}} [b_{\text{naf}} \tau_{\text{naf}}(\lambda, L) + (1 - b_{\text{naf}}) \tau_{\text{af}}(\lambda, L)] + (1 - b_{\text{fine}}) [b_{\text{dust}} \tau_{\text{dust}}(\lambda, L) + (1 - b_{\text{dust}}) \tau_{\text{ss}}(\lambda, L)],$$

(12)

where the abbreviations are: naf – non-absorbing fine component, af – absorbing fine component, and ss – sea salt coarse component. Dust fraction $b_{\text{dust}}$ is the above mentioned AEROCOM a priori value.

### 2.3 Uncertainty estimation for ADV

The effect of AATSR measurement error on the retrieved AOD is described. First the uncertainty for the retrieved aerosol model decision parameters, which include the fine mode fraction $b_{\text{fine}}$, the absorbing/non-absorbing fine particle mixture $b_{\text{naf}}$, and the AOD level $L$, is determined. Then these uncertainties are used to determine the final uncertainty in the retrieved AOD.

The other possible sources for errors arise from modeling. These include uncertainty in the aerosol model selection (fine mode fraction, absorbing/non-absorbing fine particle mixture, dust fraction), LUT interpolation errors, and radiative transfer computation errors.

The formal treatment is based on the general equation formalism by Tarantola (1987) (pp. 77–82). First, denote the parameters in the least squares problem (11) by

$$x = \{b_{\text{fine}}, b_{\text{naf}}, L, r\},$$

(13)
and the problem equations by

\[
f_i(x) = \frac{\rho_m^n(\lambda_i) - \rho_a^n(b_{\text{fine}}, b_{\text{naf}}, L, \lambda_i)}{T^n(b_{\text{fine}}, b_{\text{naf}}, L, \lambda_i)} - \frac{\rho_m^f(\lambda_i) - \rho_a^f(b_{\text{fine}}, b_{\text{naf}}, L, \lambda_i)}{kT^f(b_{\text{fine}}, b_{\text{naf}}, L, \lambda_i)}, \tag{14}
\]

where \( r = \{\rho_m^n(\lambda_i), \rho_m^f(\lambda_i)\} \ \forall i \in (1, 3) \) is the measured nadir and forward reflectance. Index \( i \) refers to the wavelengths; \( i = \{1, 2, 3\} \). This kind of formulation of the problem enables the determination of uncertainty in the decision parameters based on the measurement error. The formulation could take into account the effect of a priori information for \( b_{\text{fine}}, b_{\text{naf}} \) and \( L \) but this is neglected as the only error is assumed to come from the measurement.

Equation (14) can be solved in a least-squares sense using a quasi-Newton method. The maximum likelihood point can be found using iteration

\[
x_{n+1} = C_X F_n^T (C_T + F_n C_X F_n^T)^{-1} f(x_n), \tag{15}
\]

where

\[
F_n = \left( \frac{\partial f}{\partial x} \right)_{x_n}. \tag{16}
\]

The a posteriori covariance is

\[
C_X' = (F_{\infty}^T C_T^{-1} F_{\infty} + C_X^{-1})^{-1}, \tag{17}
\]

where \( x_{\infty} \) is the solution of the minimized Eq. (14). Note that even though the ADV solution is not computed using the iteration scheme above it is still possible to determine the a posteriori covariance.

The Jacobian matrix \( F \) is of the form

\[
F = \begin{pmatrix}
\frac{\partial f_1}{\partial b_1} & \frac{\partial f_1}{\partial b_2} & \frac{\partial f_1}{\partial L} \\
\frac{\partial f_2}{\partial b_1} & \frac{\partial f_2}{\partial b_2} & \frac{\partial f_2}{\partial L} \\
\frac{\partial f_3}{\partial b_1} & \frac{\partial f_3}{\partial b_2} & \frac{\partial f_3}{\partial L}
\end{pmatrix} \tag{18}
\]
All the partial derivatives are computed numerically as the evaluation of these values requires interpolation from the aerosol LUTs and analytical differentiation is not possible.

The covariance $C_T$ includes only measurement errors. For AATSR this error is taken to be 5% of the measured signal for the whole spectrum (Thomas et al., 2009). The principal difficulty is that in Eq. (14) there are two measured values $\rho^p_n(\lambda_i)$ and $\rho^f_m(\lambda_i)$. The formulation in Eq. (17) takes into account the uncertainty of only one value in the covariance matrix. However, because the nadir and forward relative measurement errors are equal, the larger of the computed absolute measurement errors is used. It would be useful to study individually the effect of the nadir and forward measurement error on the aerosol model parameters in the future. In addition, when all errors are considered to be Gaussian in nature, modelling errors could be simply added to the measurement errors (Tarantola, 1987). Another simplification here is that measurement errors do not correlate. Thus, $C_T$ is diagonal. This assumption does not hold for the a posteriori covariance $C_X$. The uncertainty in the aerosol model parameters will be correlated and these correlations include potentially interesting knowledge of the retrieval.

The a priori covariance matrix for the aerosol model defining parameters $C_X$ is neglected at the moment because the uncertainty contribution of the measurement error to these very parameters is the motivation of this exercise.

AOD is determined for each of the three wavelengths simultaneously, using the aerosol model defined by the three optimized decision parameters: $b_{fine}$, $b_{naf}$, and $L$. First, for all four aerosol components that are used the corresponding AOD is interpolated from their LUTs by using the AOD level parameter $L$. Then, simultaneously, the fine aerosol components are mixed based on the non-absorbing and absorbing AOD using $b_{naf}$, and the coarse aerosol component is obtained from mixing the sea salt and dust AOD using the dust fraction. The final AOD is then obtained from the fine and coarse AOD using $b_{fine}$; see Eq. (12). This is achieved as follows.
Denote the AOD interpolation/mixing operator by $p$. Then for wavelength $i$ the AOD is

$$\tau_i = p_i(b_{\text{fine}}, b_{\text{naf}}, L).$$  \hspace{1cm} (19)

The covariance of AOD is then (Meyer, 1975)

$$C_{\text{AOD}} = PC_{X'}P^t,$$  \hspace{1cm} (20)

where $P$ is the Jacobian of the interpolation/mixing operator:

$$P = \begin{pmatrix}
\frac{\partial p_1}{\partial b_1} & \frac{\partial p_1}{\partial b_2} & \frac{\partial p_1}{\partial L} \\
\frac{\partial p_2}{\partial b_1} & \frac{\partial p_2}{\partial b_2} & \frac{\partial p_2}{\partial L} \\
\frac{\partial p_3}{\partial b_1} & \frac{\partial p_3}{\partial b_2} & \frac{\partial p_3}{\partial L} \\
\end{pmatrix}.$$  \hspace{1cm} (21)

The uncertainty estimate for AOD can be finally found in the diagonal of $C_{\text{AOD}}$. The uncertainty of the dust fraction, which is not a retrieved parameter, could be added to $C_{X'}$ if this uncertainty was assumed to be Gaussian.

### 3 ASV algorithm for over ocean retrieval

The basic principle of the ASV algorithm is to minimize the discrepancy between the TOA measured and modelled reflectance at wavelengths of 0.555, 0.659, 0.865 and 1.61 µm. The modelled reflectance is described below. The aerosol modelling follows the description given for the ADV algorithm. The aerosol model is based on the three mixtures that are introduced with Eq. (11).
3.1 The modelled TOA reflectance over ocean

The TOA reflectance $\rho$ over ocean is given by (Veefkind and de Leeuw, 1998):

$$\rho = \rho_a + T \downarrow \rho_{s,\text{dir}}/(1 - s \rho_{s,\text{dir}}) T \uparrow + t \downarrow \rho_{s,\text{dif}} T \uparrow$$

$$+ T \downarrow \rho_{s,\text{dif}} T \uparrow + t \downarrow \rho_{s,\text{iso}} T \uparrow,$$

(22)

where $\rho$ is the top-of-the-atmosphere reflectance, $s$ is the atmospheric backscatter ratio, $T$ is the direct transmittance and $t$ is the diffuse transmittance upwards ($\uparrow$) and downwards ($\downarrow$). The terms $\rho_a$ and $\rho_s$ are the atmospheric and surface reflectance, respectively, and the other terms come from the ocean surface model which is described in the next section. The multiple scattering between surface and atmosphere has been included only for the direct down–direct up case as it becomes negligible when diffuse transmittance is applied. Note that geometric and wavelength dependencies in Eq. (22) are omitted for brevity. The terms in Eq. (22) from left to right describe:

- Reflectance due to scattering in the atmosphere by aerosols and molecules.
- Photons transmitted downward, reflected by the ocean surface, and transmitted up.
- Photons scattered along the downward path, reflected by the ocean surface, and transmitted up.
- Photons transmitted downward, reflected by the ocean surface, and scattered towards the satellite instrument.
- Photons scattered along the downward path, reflected by the ocean surface, and scattered towards the satellite instrument.

Each of the terms in Eq. (22) contains contributions of specular (Fresnel) reflection, oceanic white caps and subsurface scattering.
3.2 Ocean reflectance modelling

The ocean surface reflectance is modelled as the sum of specular (Fresnel) reflectance (Cox and Munk, 1954) and reflectance by subsurface scattering. The Fresnel part is described by the geometric situation while the subsurface scattering is a function of chlorophyll concentration. The surface reflectance is a sum of four components based on atmospheric transmittance (see Eq. 22). The reflectance in these components is given by the Eqs. (23)–(26).

\[
\rho_{\text{s,dir}}(\mu_0, \mu, \phi, \lambda) = \rho_{\text{glint}}(\mu_0, \mu, \phi, \lambda) + \rho_{\text{chl}}(C, \lambda),
\]

where \(\rho_{\text{glint}}\) is the sun glint and \(\rho_{\text{chl}}\) is the subsurface reflectance due to chlorophyll with concentration \(C\), and it is assumed here to be Lambertian (Veefkind and de Leeuw, 1998). In practice the reflectance due to sun glint is not taken into account because pixels flagged as sun glint in the AATSR L1 data are not used in the retrieved. Geometric reflectance is determined by the cosine of solar zenith angle, \(\mu_0\), the cosine of viewing zenith angle, \(\mu\), and the relative azimuth angle, \(\phi\). Reflectance depends on the wavelength \(\lambda\). Subsurface reflectance is modelled after Morel (1988) for case I waters as

\[
\rho_{\text{s,dir}}(\mu_0, \mu, \phi, \lambda) = \rho_{\text{Fresnel}}(\mu_0) + \rho_{\text{chl}}(C, \lambda),
\]

\[
\rho_{\text{s,dir}}(\mu_0, \mu, \phi, \lambda) = \rho_{\text{Fresnel}}(\mu_0) + \rho_{\text{chl}}(C, \lambda),
\]

\[
\rho_{\text{s,iso}}(\mu_0, \mu, \phi, \lambda) = 0.066 + \rho_{\text{chl}}(C, \lambda).
\]

In these equations \(\rho_{\text{Fresnel}}\) is the Fresnel reflectance, and the factor 0.066 has been adapted from Ivanov (1975). The possible error caused by the approximate value is minimal because the contribution of the term described by Eq. (26) to the TOA reflectance is small. All of the above components include the contribution of the whitecap reflectance determined by the fraction of the ocean surface covered by whitecaps. The whitecap fraction \(W\) is a function of wind speed \(U\) (m s\(^{-1}\)) (Monahan and
O’Muircheartaigh, 1980):

\[ W = 3.84 \times 10^{-6} \times U^{3.41}. \]  

(27)

### 3.3 ASV in practice

In the ASV retrieval the same aerosol look-up-tables are used as for the ADV retrieval. There is no distinction between land and ocean retrieval with respect to aerosol components. AEROCOM a priori values and retrieval itself decide the aerosol composition for any given pixel.

As was mentioned above, the ASV method is based on minimizing the difference between the TOA measured and modelled reflectance at the four AATSR wavelengths simultaneously. This leads to a minimization scheme which is considerably different from that for ADV (Eq. 11). The largest physical difference is that only one of the AATSR views is used. Currently the forward view is employed because it is less hindered by sun glint than the nadir view. The minimization in the ASV problem, following the ADV notation, is

\[
\arg_{b_{\text{fine}}, b_{\text{naf}}, L} \min \sum_{i=1}^{N_{\lambda}} \left[ \rho_{\text{m}}^{f}(\lambda_{i}) - \rho^{f}(b_{\text{fine}}, b_{\text{naf}}, L, \lambda_{i}) \right]^2,
\]  

(28)

with the modifications that \( N_{\lambda} = 4 \), as the 865 nm wavelength is also used, and \( \rho^{f} \) from Eq. (22) is now the modelled atmospheric and ocean surface reflectance. Subscript \( m \) indicates the measured TOA reflectance.

### 3.4 Uncertainty estimation for ASV

The effect of AATSR measurement error on the retrieved AOD described for the ADV algorithm in Sect. 2.3 can straightforwardly be applied to ASV by replacing Eq. (14) with the ASV minimization from Eq. (28):

\[
f_{i}(x) = \rho_{\text{m}}^{f}(\lambda_{i}) - \rho^{f}(b_{\text{fine}}, b_{\text{naf}}, L, \lambda_{i}),
\]  

(29)
and performing the computations as described in the ADV uncertainty characterization.

### 3.5 Cloud screening

Clouded pixels have to be excluded from retrieval as they mask the other atmospheric contributions to the measured TOA reflectance. The tests that are described here were designed for the use with ATSR-2 data. For AATSR cloud flags are included in the reflectance data (AATSR Handbook, 2007). However, these flags were found to be too restrictive because a significant amount of pixels that otherwise provide good AOD values, as determined from comparison with ground-based sun photometer data, are flagged as cloud-contaminated.

Therefore, three separate cloud detection tests are used. These tests are based on the work of Saunders and Kriebel (1988) and Koelemeijer et al. (2001). To automate the cloud screening, AATSR orbits are divided into scenes of 512 × 512 pixels. Reflectance in each of the scenes is histogrammed and the histograms are used for the automatic determination of thresholds for the cloud tests as described by Robles González (2003). The cloud tests are:

1. **The gross cloud test.** In the AATSR 12 µm brightness temperature channel clouds appear cooler than the underlying surface during day time. If the brightness temperature for a pixel is below threshold, the pixel is flagged as cloudy.

2. **Generally, clouds are brighter than the underlying surface.** If the reflectance of the 0.659 µm channel for a pixel is higher than threshold, the pixel is flagged as cloudy.

3. **Ratio of the 0.865 and 0.659 µm reflectance.** If the ratio is around one for a pixel, the pixel is flagged as cloudy. The distance from unity that governs cloud flagging is determined by the automation.

These tests are applied for both AATSR views. If any of the tests indicates that a pixel is clouded, it will be excluded from the retrieval.
4 The adaptation of ADV and ASV for global multi-year retrievals

The ADV algorithm is suitable for retrieving the optical properties of aerosols over land as was demonstrated for several different areas (Veefkind et al., 2000; Robles González et al., 2000; Robles González and de Leeuw, 2008; Kokhanovsky et al., 2009; Sundström et al., 2012). However, for the application to very large data sets, such as for global long-term retrieval, the time needed for retrieval computations was too long and processing of large data sets was very time consuming. The main reason was that three parameters need to be optimized during the retrieval process: the AOD reference level and the two mixtures of the aerosol components (see Eq. 11).

Where the original retrieval were made for each individual pixel (1 × 1 km$^2$ at nadir), it was decided that larger retrieval tasks should be made for enhanced default pixels (superpixel), i.e. 0.1 × 0.1°. This is the level 2 (L2) result grid. The L2 results are also available in a 10 × 10 km$^2$ sinusoidal grid. The retrieved results are additionally given at level 3 (L3) which is averaged over a 1 × 1° grid. L3 results include all AATSR orbits, usually 14, for each day.

The added advantage of using a larger area for retrieval is that some statistical measures indicating the reliability of the retrieval can be computed using the ensemble of measured TOA reflectance values over the area.

In this section the methods for averaging the AATSR measured TOA reflectance over the superpixel are described. Also the choice of aerosol models is discussed.

4.1 Averaging of measured reflectance for ADV and ASV

The natural assumption when averaging TOA measured reflectance is that reflectance due to the atmosphere is sufficiently uniform over the averaged area. Here the term sufficient describes situations where no sharp spatial gradients in aerosol properties occur inside the area. Reflectance due to atmospheric gases is assumed to be uniform.

For the surface reflectance, however, this assumption can generally not be made. The complications in the averaging of the measured TOA reflectance are caused by
the $k$ ratio approach of the ADV. The $k$ ratio is determined by applying Eq. (7) and using the nadir and forward view surface reflectance at 1.61 µm. It would be unrealistic to assume that surface reflectance is constant over the larger pixel area. Reformulation of Eq. (9):

$$\frac{\left[\rho^f(\mu_0, \mu, \phi, \lambda) - \rho_a^f(\mu_0, \mu, \phi, \lambda)\right]}{T^f(\mu_0, \mu, \phi, \lambda)} = k$$

shows that the value of $k$ strongly affects the results of a retrieval. If the $k$ ratio for the superpixel are is computed by simply averaging of all values within the pixel, the results may not be representative for any of the original pixels. As an example, consider an area where half of the larger area is covered with pixels having a high $k$ ratio and the other half having a low value. When the $k$ ratios are averaged the end result would be wrong for all of them. Furthermore, as both of the AATSR views are employed, in simple averaging of reflectance one cannot be certain that corresponding nadir/forward pixels are used when the $k$ ratio is determined. This could lead to situations where, in principle, nadir and forward view reflectance come from different pixels.

The chosen approach to average measured reflectance is to find pixels which are representative for an area, and at the same time occur in both the nadir and forward views. In ADV this is achieved by using the following method:

1. At least 50% of the pixels belonging to the superpixel area must pass the cloud screening tests. This step ensures that enough information is present for the following steps.

2. Produce a histogram of the measured reflectance at 1.61 µm separately for nadir and forward reflectance. Typically seven bins are used ranging from zero to the maximum of the measured reflectance. The near-infrared channel is used here because the effect of aerosols is small. That is, the measured reflectance is considered in first approximation to have contributions from the surface only.
3. Choose the nadir/forward bins that have the maximum number of reflectance values.

4. Find out which pixels that are in the chosen bins are mutual to nadir and forward views.

5. If there are more that ten values left, average the chosen reflectance values and use them in the retrieval. If less than ten values are left, the surface reflectance in the area is considered to vary too much and retrieval is not executed.

The number of bins in the histogram determination is a compromise between loss of data and degeneration towards simple averaging. If too many bins were used, there would be too few pixels for averaging of the reflectance. This situation would be potentially poor in a statistical sense since only few pixels would represent the whole area. If too few bins were used, too wide a range of reflectance values would be accepted. This would allow pixels that could lead to a situation where the whole representative search of the $k$ ratio approach would become meaningless.

The over ocean ASV algorithm utilizes the above described reflectance averaging for the sake of uniformity. A simple average could be also used for the ASV as it can be assumed that the ocean surface reflectance is quite smooth over the $0.1 \times 0.1^\circ$ superpixel area.

The other test for the averaged reflectance measures the uniformity of the atmospheric reflectance. The standard deviation of the reflectance at 0.555 $\mu$m is used as a measure for the uniformity. The 0.555 $\mu$m channel is utilized here as it is sensitive to both aerosol and cloud conditions. If the standard deviation of the TOA reflectance is too large for a superpixel, results are judged to be unreliable. Retrieval is still done but the results include the standard deviation which can then be applied by the end user to exclude unreliable areas. This test can be seen also as an additional spatial cloud screening but can also invalidate the superpixel in a case of large aerosol gradients such as in the presence of strong sources. Based on validation the threshold for too large standard deviation of the reflectance has been chosen to be 0.009.
4.2 Post processing – additional cloud screening

For each pixel retrieved with ADV a cloud post-processing test is applied to determine and discard the pixels that might potentially include cloud edges or residual sub-(super)pixel clouds. This processing also enables the removal of outliers that would potentially harm the assimilation of the retrieved aerosol properties in atmospheric models.

Each pixel retrieved is analyzed together with the eight surrounding pixels in a 0.2 × 0.2° area. If, in addition to the tested pixel, less than 3 pixels are retrieved in the area, the tested pixel is considered to be “contaminated” and discarded. If, besides the tested pixel, at least 3 more pixels are retrieved and the AOD for the tested pixel is smaller than 0.5, the tested pixel passes the cloud processing test. If AOD > 0.5, an additional standard deviation test is applied. If the standard deviation of the AOD in the area is larger than 0.25, the tested pixel is discarded.

The numbers presented above are a compromise between global coverage and acceptable validation results. However, for certain areas with high AOD (e.g. India, China), and for case studies of natural high AOD episodes (e.g. dust storms, volcanic eruptions) different values can be used.

4.3 The 17 yr time series using the ATSR-2 and AATSR instruments

Global and regional changes in aerosol conditions could potentially be investigated using the 17 yr (1995–2012) data record of aerosol properties provided by the combined ATSR-2 (Along-Track Scanning Radiometer 2) and AATSR instruments. These two instruments have similar characteristics. However, to detect trends the reliability of the data over this long time must be ensured. Issues which need to be taken into account include the detection and removal of bias caused by systematic instrument errors, instrument degradation and the transition from the ATSR-2 to the AATSR instruments.

The bias issue can be handled in two ways. First, both ATSR-2 and AATSR instruments have on-flight calibration and, in addition, corrections have been made for the L1
reflectance data. The L1 correction has been done by the L1 data ground processing center (RAL Space at Rutherford Appleton Laboratory, UK) by correcting the so-called drift in the measured reflectance (Smith, 2008). Second, because both the nadir and forward views of the instruments are provided by the same camera (i.e. the on-board camera is tilted to produce the nadir and forward scans), it is straightforward to do the formal calculus using Eq. (1) for both views and prove that the addition of systematic error, common to both views, does not affect the final results. This indicates that when the ADV algorithm is used over land, the bias caused by instrument systematic errors could be neglected. Over ocean this does not apply as only one of the views is currently used for the ASV retrieval.

The ATSR-2–AATSR continuation requires more research to verify that the combined time series produced with the ADV/ASV algorithms is reliable. Fortunately there is some overlap in the observation of the two instruments which enables to conduct the research.

5 Results

Results from the validation of the retrieved AOD against reference measurements in the year 2008 are presented in Sect. 5.1. Uncertainty estimates are evaluated in Sect. 5.2.

5.1 AERONET comparison

The most widely used validation reference for satellite-retrieved AOD is the ground-based sun photometer measurement network AERONET (Holben et al., 1998). However, the AATSR and AERONET wavelengths are not the same. Therefore, the AERONET AOD at at 0.555 $\mu$m has been obtained by interpolation from the AODs at 0.440 and 0.670 $\mu$m. Furthermore, the AOD observations need to be collocated in time and location. This was done by considering AERONET observations within ±1/2 h of the AATSR overpass. Spatially, AATSR values within a 0.25×0.25° area around an
AERONET station were averaged. The validation included 198 AERONET stations. The comparison between the retrieved and reference AOD at 0.555 µm for year 2008 is shown in Fig. 1.

Despite some scatter in the comparison, the overall correlation $r = 0.85$ is very good. Some underestimation can be seen in the linear fit (slope 0.92). This must be confirmed with multi-year validation. The mean error is 0.02 and $\text{RMSE} = 0.01$.

To assess the regional performance of the retrieval, an analysis of the discrepancy between the AATSR-retrieved and AERONET AODs was made for individual AERONET stations. Here, discrepancy is defined as AERONET AOD subtracted from retrieved AATSR AOD. In the analysis at least three comparisons at a station were required to compute the average discrepancy. The discrepancies are shown in the map in Fig. 2 where they were averaged over areas of $1^\circ \times 1^\circ$. Several AERONET stations may contribute to an area, especially in Europe and North America where the station network is dense.

Figure 2 shows that discrepancy is low for Europe and North America while areas with bright surface and/or dust are underestimated. Coastal stations, usually based on a small island, show slight overestimation. This may require in future some adjustments in the ocean surface modeling which was described in Sect. 3.2.

### 5.2 Evaluation of the uncertainty estimation

The uncertainties are shown in Fig. 3, as a plot of AATSR-retrieved AOD versus AERONET AOD. For presentation clarity a small time period of two months (January and February 2008) is shown. Generally, the uncertainty seems to behave as expected. The uncertainty increases as the AOD values are higher, because the increased atmospheric reflectance due to aerosols results in higher values of the TOA reflectance, and thus the measurement error which is relative (5% of the measured reflectance).

Figure 4 shows a global map of the AOD at 0.555 µm for autumn 2008 on a $1^\circ \times 1^\circ$ (level 3) grid. These data were used to evaluate to what degree the AOD uncertainty is correlated with the AOD value. The result is shown in Fig. 5. Some correlation can
be seen but it is overshadowed by a large amount of scatter. The scatter can be explained by the fact that surface reflectance affects the determined AOD uncertainty. High surface reflectance leads to high measurement error.

The AOD uncertainty can also be compared with the discrepancy between AATSR and AERONET AOD (seen in Fig. 1). This comparison is shown in Fig. 6 as a histogram. The uncertainty and discrepancy agree quite well in a statistical sense. 74% of the uncertainty – discrepancy comparison is within one standard deviation. There is a small bias indicating that on average the uncertainty has values that are larger than the discrepancy. The mean of the comparison is 0.02 with standard deviation of 0.07.

6 Discussion and conclusions

The ADV/ASV algorithm for retrieving the properties of atmospheric aerosols was described. Emphasis was on the uncertainty characterization of the retrieved AOD as this is an important aspect for the use of the AOD data for assimilation in chemical transport models and for model evaluation.

The validation results (Figs. 1 and 2) show that the retrieved AODs compare favourably with the AERONET reference data. Some areas require further study for the enhancement of the results. Large discrepancies in these areas might be due to the basic assumptions in the algorithm which do not strictly apply (e.g. the k ratio, the use of external mixtures for aerosol particles), the used aerosol modelling is not flexible enough, or residual cloud contamination. The validation presented here is based on AERONET reference data over land. Data over ocean are available from, e.g., the marine aerosol network (MAN, see e.g. Smirnov et al., 2009), but for the chosen year 2008 there are insufficient data for statistical evaluation.

The uncertainty characterization currently takes into account the propagation of the measurement error through the retrieval process. For over land areas this works reasonably well as the effect of surface reflectance on the results is correctly handled. Over ocean, however, the obtained uncertainty is rather small. This is due to the low surface
reflectance leading to low measured TOA reflectance. A more correct uncertainty over ocean could be computed by adding a sea surface modeling error. This error has been reported to be about 10% for a similar kind of ocean surface model as is used in the ASV algorithm (Sayer et al., 2009).

When the AOD uncertainty is compared with the discrepancies in the AERONET validation (Fig. 6) a statistical similarity between the uncertainty and the discrepancy can be seen. The two entities are not, however, directly comparable. The uncertainty is affected not only by the reflectance of aerosols but also by the reflectance of the underlying surface whereas the discrepancy can have various reasons.

One of the shortcomings of the current ADV algorithm is the exclusion of bright surface. It is not yet clear why the $k$ ratio assumption does not hold for bright surface areas. One possible way to overcome this issue would be to implement the surface treatment from North et al. (1999), which has been shown to behave reliably in high surface reflectance conditions.

The ENVISAT satellite ceased to provide data in April 2012. This does not, however, mean that the presented retrieval algorithms are now obsolete. On one hand, the processing of the whole 17 yr ATSR-2–AATSR data will provide a time series for studies of global changes in aerosol conditions and it will act as a valuable reference for global climate model studies. On the other hand, the developed algorithms can be applied to data from the AATSR-like Sea and Land Surface Temperature Radiometer (SLSTR) instrument on the ESA/GMES Sentinel-3 mission which is planned for launch in April 2014.

The conclusion from the present study is that, although more work is still needed, results of the current ADV/ASV retrieval algorithm compare favourably with independent ground-based reference data and are suitable for characterizing local or global aerosol conditions and, in addition, can be used for data assimilation purposes.

Acknowledgements. This work was funded by the European Space Agency – Climate Change Initiative (ESA CCI) and the Monitoring Atmospheric Composition and Climate – Interim
Implementation (MACC II) projects. The authors wish to acknowledge the AERONET project for providing the ground-based reference data.

**References**


Grey, W., North, P., and Los, S.: Computationally efficient method for retrieving aerosol optical depth from ATSR-2 and AATSR data, Appl. Optics, 45, 2786–2795, 2006. 4042
Ivanov, A. P.: Physical Properties of Hydro-optics, Nauka i Tekhnika, Minsk, 1975. 4054


Table 1. The Aerosol CCI aerosol components. Listed are the geometric radius $r_g$, standard deviation $\sigma$, refractive index $n$, and the aerosol layer height (alh).

<table>
<thead>
<tr>
<th>component</th>
<th>$r_g$ (µm)</th>
<th>$\sigma$</th>
<th>$n$</th>
<th>alh (km)</th>
</tr>
</thead>
<tbody>
<tr>
<td>non-absorbing fine</td>
<td>0.07</td>
<td>1.700</td>
<td>1.40–0.003i</td>
<td>0–2</td>
</tr>
<tr>
<td>absorbing fine</td>
<td>0.07</td>
<td>1.700</td>
<td>1.50–0.040i</td>
<td>0–2</td>
</tr>
<tr>
<td>sea salt</td>
<td>0.788</td>
<td>1.822</td>
<td>1.40–0.000i</td>
<td>0–1</td>
</tr>
<tr>
<td>dust</td>
<td>0.788</td>
<td>1.822</td>
<td>1.56–0.002i</td>
<td>2–4</td>
</tr>
</tbody>
</table>
Fig. 1. Comparison of AOD at 0.555 μm between ADV/ASV retrieved and AERONET in the year 2008.
Fig. 2. Map of the AOD discrepancy (AERONET AOD subtracted from retrieved AATSR AOD) analysis by AERONET stations in the year 2008. The colored 1° × 1° patches indicate the absolute average AOD discrepancy. The 198 AERONET stations are marked with red dots.
Fig. 3. Comparison of AERONET and AATSR AOD at 0.555 µm for the period of January–February 2008. The per pixel uncertainty is also shown with error bars.
Fig. 4. Average level 3 AOD at 0.555 μm for the autumn months (September, October, November) 2008.
Fig. 5. The global comparison of the level 3 AOD with the level 3 AOD uncertainty.
Fig. 6. Histogram of the comparison of AERONET validation discrepancy $\Delta \tau_{\text{validation}} = \tau_{\text{AATSR}} - \tau_{\text{AERONET}}$ with the computed uncertainty $\Delta \tau_{\text{uncertainty}}$. The shown results were determined at 0.555 µm.