Remote sensing of ice crystal asymmetry parameter using multi-directional polarization measurements – Part 1: Methodology and evaluation with simulated measurements

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Abstract

We present a new remote sensing technique to infer the average asymmetry parameter of ice crystals near cloud top from multi-directional polarization measurements. The method is based on previous findings that (a) complex aggregates of hexagonal crystals generally have scattering phase matrices resembling those of their components and (b) scattering phase matrices systematically vary with aspect ratios of crystals and their degree of microscale surface roughness. Ice cloud asymmetry parameters are inferred from multi-directional polarized reflectance measurements by searching for the closest fit in a look-up table of simulated polarized reflectances computed for cloud layers that contain individual hexagonal columns and plates with varying aspect ratios and roughness values. The asymmetry parameter of the hexagonal particle that leads to the best fit with the measurements is considered the retrieved value. For clouds with optical thickness less than 5, the cloud optical thickness must be retrieved simultaneously with the asymmetry parameter, while for optically thicker clouds the asymmetry parameter retrieval is independent of cloud optical thickness. Evaluation of the technique using simulated measurements based on the optical properties of a number of complex particles and their mixtures shows that the ice crystal asymmetry parameters are generally retrieved to within 5%, or about 0.04 in absolute terms. The retrieval scheme is largely independent of calibration errors, range and sampling density of scattering angles and random noise in the measurements. The approach can be readily applied to measurements of past, current and future airborne and satellite instruments that measure multi-directional polarized reflectances of ice-topped clouds.

1 Introduction

Cloud feedbacks remain among the principal sources of uncertainty in assessing the sensitivity of the Earth’s climate (Hartmann et al., 1992; Soden and Held, 2006; Waliser et al., 2009). A continuing area of uncertainty in modeling clouds and consequently...
their feedbacks is prescribing the radiative properties of clouds and ice clouds in particular (Stephens et al., 1990; Stackhouse and Stephens, 1991; Fu et al., 1998; Fu, 2007). The fundamental radiative properties of ice clouds for global climate model projections can be represented in terms of optical thickness, effective ice crystal size and the first moment of the scattering phase function, commonly referred to as the asymmetry parameter (Coakley and Chylek, 1975; Fu and Liou, 1993; Yang et al., 2000; Fu, 2007). Reasonably stringent global constraints of two of these three parameters, namely ice cloud optical thickness and effective ice crystal size, have been obtained for more than three decades from measurements of instruments on polar-orbiting and geostationary satellite platforms, such as the Moderate Resolution Imaging Spectroradiometer (MODIS, Platnick et al., 2003), the Geostationary Operational Environmental Satellite (GOES, Lindsey and Grasso, 2009) and the Spinning Enhanced Visible and Infrared Imager (SEVIRI, Roebeling et al., 2006). However, to our knowledge, no remote sensing technique exists to date to directly infer the asymmetry parameter of ice crystals. Such measurements are crucial to better constrain values used for climate models. Vogelmann and Ackerman (1995) estimated that asymmetry parameters must be known to within 2–5% to constrain computed shortwave fluxes to within about 5%. Furthermore, a remote sensing technique to obtain ice asymmetry parameter could help to improve operational retrievals of ice cloud optical thickness and effective radius, which substantially depend on the scattering properties of the ice crystal model used in the retrieval algorithms (Rolland et al., 2000; Yang et al., 2008a; Zhang et al., 2009; Baum et al., 2011; van Diedenhoven et al., 2012).

Ice crystal asymmetry parameters at visible wavelengths have been inferred indirectly from combinations of flux measurements and radiative transfer model calculations (e.g., Platt et al., 1980; Stephens et al., 1990; Francis et al., 1994; Mitchell et al., 1996), yielding values ranging from about 0.7 to about 0.85. More direct in situ measurements made with the Cloud Integrating Nephelometer (CIN, Gerber et al., 2000)

\(^1\)We use “ice clouds” as shorthand for all clouds that have tops which are radiatively dominated by ice.
and the Polar Nephelometer (Gayet et al., 1997) generally show values around 0.75, with little dependence on location and temperature (e.g., Auriol et al., 2001; Garrett et al., 2001, 2003, 2005; Baran et al., 2005; Gayet et al., 2006, 2012, see Garrett, 2008 for an overview). However, these in situ observed asymmetry parameters provide poor spatial coverage and may be substantially affected by ice shattering on the probes (Korolev et al., 2011), or undersampling of the phase function in the forward scattering direction (Gerber et al., 2000) or both. Global polarization measurements from the Polarization and Directionality of the Earth’s Reflectances (POLDER) instrument are generally found to be consistent with roughened ice crystals, which in turn generally have relatively low asymmetry parameters (<0.8). In contrast, using surface observations, Sassen et al. (2003) reported frequent sightings of halos within ice clouds that imply pristine ice crystals, which generally have high asymmetry parameters.

Theoretical ice scattering properties have been calculated for a wide range of particle shapes (e.g., Macke et al., 1996; Hess et al., 1998; Yang and Liou, 1998; Zhang et al., 2004; Liu et al., 2006; Um and McFarquhar, 2007, 2009, 2011; Nousiainen et al., 2011; Baum et al., 2011; Ishimoto et al., 2012), yielding asymmetry parameters ranging from about 0.65 to above 0.95. General conclusions that can be deduced from these theoretical studies are: (1) complex aggregates of crystals generally have scattering phase matrices resembling those of their components (e.g., Fu, 2007; Um and McFarquhar, 2007, 2009); and (2) scattering phase matrices systematically vary with aspect ratios (ratio of length to width) of crystals (or crystal components in aggregates) and their degree of randomization (e.g., Fu, 2007; Yang and Fu, 2009). For pristine, simple particles, such as smooth hexagonal columns, the phase function often shows strongly contrasted features such as halos that are the created by ray caustics (Minnaert, 1954). Such features can be suppressed by increasing microscale crystal surface roughness (Macke et al., 1996), increasing the number of impurities within ice crystals (Hess et al., 1998), or increasing large-scale complexity of ice aggregates (Ishimoto et al., 2012).

Based on the two aforementioned generalizations of ice crystal scattering properties, here we present a remote sensing technique to infer ice crystal asymmetry.
parameter from multi-directional polarization measurements. In short: by assuming individual hexagonal ice columns and plates to serve as proxies for more complex shapes and aggregates, a best fit to multi-directional polarization measurements is sought by varying the aspect ratios and roughness parameters of columns and plates, and the asymmetry parameter of the corresponding hexagonal column or plate is considered to be representative (i.e., the retrieved value) of the asymmetry parameter of the ice crystal ensemble at the top of the observed cloud.

Several attempts have been made previously to deduce ice crystal shape from polarization measurements, mostly applied to measurements of the Polarization and Directionality of the Earth’s Reflectances (POLDER) instrument (e.g., Chepfer, 1998; C.-Labonnote et al., 2000; Chepfer et al., 2001; Masuda et al., 2002; Knap et al., 2005; Sun et al., 2006; Baran and C.-Labonnote, 2006). Most of these attempts included only a limited collection of ice crystal habits and/or aspect ratios and many of them did not include roughened ice crystals. To our knowledge, our application is the first to include a virtually continuous selection of aspect ratios and roughness values. Moreover, while previous results were difficult to relate to physical and radiative properties of ice crystals, here we directly relate the retrieved particle aspect ratio and roughness parameter to the ice crystal asymmetry parameter. A similar approach was recently applied to a subvisual cirrus cloud (Ottaviani et al., 2012a) and thick tropical clouds (van Diedenhoven et al., 2012), as well as over a snow surface (Ottaviani et al., 2012b).

Here in Part 1 of a two-part paper, the retrieval method is described and evaluated using simulated measurements. The simulated measurements are based on instrument characteristics of the airborne Research Scanning Polarimeter (RSP Cairns et al., 1999). In Part 2 we apply the method to measurements obtained by RSP during the The Cirrus Regional Study of Tropical Anvils and Cirrus Layers – Florida Area Cirrus Experiment (CRYSTAL-FACE) and evaluate results using other remote sensing and in situ data.
First, the retrieval method is presented in detail in Sect. 2. After evaluating the method against simulated measurements in Sect. 3, conclusions are discussed in Sect. 4.

2 Methodology

The asymmetry parameter $g$ is defined as the first moment of the normalized scattering phase function $P_{\text{tot}}$ (Macke et al., 1996):

$$g = \int_{0}^{\pi} P_{\text{tot}}(\Theta) \cos(\Theta) \sin(\Theta) d\Theta$$

(1)

where $\Theta$ is scattering angle. In the geometric optics regime the asymmetry parameter is a linear combination of the asymmetry parameters of the refractive + reflective and diffractive contributions to the phase function, $g_{\text{ref}}$ and $g_{\text{dif}}$, respectively (Macke et al., 1996):

$$g = \frac{1}{2\omega_{0}} [(2\omega_{0} - 1)g_{\text{ref}} + g_{\text{dif}}].$$

(2)

where $\omega_{0}$ is the single scattering albedo, which is mainly determined by the ice effective radius and the imaginary part of the refractive index (Mitchell and Arnott, 1994; Fu et al., 1998). The asymmetry parameter of the diffractive contribution to the phase function is essentially unity for ice clouds at visible and short-wave infrared wavelengths, as a consequence of particles being large relative to wavelength. The refractive + reflective contribution to the phase function depends on the shape of the ice particles and their microscale surface roughness (Macke et al., 1996; Yang and Liou, 1998). As explained above, we adopt hexagonal ice columns and plates with varying aspect ratio and microscale roughness as proxies for more complex shapes and aggregates to infer the
asymmetry parameter. Together with ice crystal effective radius \( (e.g., \text{Nakajima and King, 1990}) \), the total asymmetry parameter can be estimated for any wavelength using Eq. (2).

Ice crystal asymmetry parameters are inferred from measured polarized reflectances \( R_p \) defined as

\[
R_p = \frac{\pi \sqrt{Q^2 + U^2}}{\mu_0 F_\odot},
\]

where \( \mu_0 \) is the cosine of the solar zenith angle, \( F_\odot \) is the solar irradiance, and \( Q \) and \( U \) are the second and third Stokes parameters, respectively \( (\text{van de Hulst, 1957}; \text{Chepfer, 1998}; \text{Baran and C.-Labonnote, 2006}) \). To produce a look-up-table (LUT) containing \( R_p \) values for clouds consisting of hexagonal plates and columns with varying aspect ratios and roughness parameters, forward calculations are made using a plane-parallel doubling-adding code \( (\text{Hansen and Travis, 1974}; \text{De Haan et al., 1987}) \). The cloud is represented in the model by a single uniform layer without considering cloud geometrical thickness. Rayleigh scatterers and absorbing atmospheric gases are not included. Randomly oriented ice crystals are assumed \( (\text{Zhou et al., 2012}) \). To account for the highly peaked scattering phase functions, we use the \( \delta \)-\( M \) approximation \( (\text{Wiscombe, 1977}) \) for multiply-scattered light, whereas the contribution of single-scattered light is calculated analytically \( (\text{using the TMS-method described by Nakajima and Tanaka, 1988}) \). A completely black, non-polarizing surface is assumed for the lower boundary condition.

To produce the LUT, a database of optical properties for hexagonal plates and columns is calculated using the Geometrics Optics (GO) code developed by Macke et al. \( (1996) \). This ray tracing code takes microscale surface roughness of ice crystals into account in a statistical manner by perturbing, for each interaction with a ray, the normal of the crystal surface from its nominal orientation by an angle varied randomly with uniform distribution between \( 0^\circ \) and \( \delta \cdot 90^\circ \), where \( \delta \) is referred to as the roughness parameter \( (\text{see Macke et al., 1996}, \text{for a full description of the treatment of...}) \).
Yang et al. (2008b) found that this approach is an efficient, yet accurate treatment of microscale roughness. The aspect ratio of columns is varied between 1 and 50 with 26 geometrically increasing steps. The aspect ratios of plates are the inverse of those for columns, for a total of 51 aspect ratios. The roughness parameter is varied between 0 and 0.7 in steps of 0.05. Roughness parameters exceeding 0.7 are not considered because for these values the probability of unphysical scattering events strongly increases, resulting in progressively larger loss of accuracy of the GO calculations. Sizes are varied so that the projected areas of the particles, assuming random orientation, correspond to the projected areas of spheres with radii of 5, 7, 10, 14, 20, 28, 40, 56, 80, 113, 160, 226 and 320 µm. A normalized gamma size distribution $N$ of the form

$$N(D) = N_0 D^{\mu_p} e^{-\lambda_p D},$$

is applied (Mitchell, 1991; Heymsfield et al., 2002), where $D$ is the maximum particle dimension and $\mu_p$ and $\lambda_p$ are the shape and slope parameters of the size distribution. Here, $N_0$ is a normalization factor. Refractive indices for ice are taken from Warren and Brandt (2008) and are weighted by spectral response function of RSP’s 864-nm channel and the incoming solar spectrum, yielding a refractive index of 1.3038 with a negligible imaginary part.

Figure 1 shows the asymmetry parameter of the phase function of hexagonal plates and columns in the database as a function of aspect ratio and roughness parameter. Here, $\mu_p = 1.5$ and $\lambda_p = 100 \text{ cm}^{-1}$ (Heymsfield et al., 2002), but we note that the asymmetry parameter is not affected substantially by the size in the geometric optics regime (Macke et al., 1996). As previously shown by Macke et al. (1996), Fu (2007), Yang and Fu (2009) and others, the asymmetry parameter increases with increasing deviation of the aspect ratio from unity, and decreases with increasing roughness. Thus, the lowest asymmetry parameters around 0.71 are obtained for particles with an aspect ratio of unity and extreme roughness of 0.7, while asymmetry parameters exceeding 0.93 are found for smooth thin plates with aspect ratios near 0.02. Asymmetry roughness).
parameters increase with aspect ratio owing to the increase of parallel surface areas leading to greater probability of light passing through the particle with low orders of refraction + reflection and a minimal change of direction (Yang and Fu, 2009). For the same reason, the increase of asymmetry parameter with increasing deviation of aspect ratio from unity is slightly weaker for columns than for plates owing to the larger parallel surfaces of plates (cf. Macke et al., 1996; Yang and Fu, 2009).

Figure 2 illustrates the dependence of the single scattering degree of linear polarization (DoLP) function on aspect ratio and roughness parameter. As noted by Knap et al. (2005); Baran and C.-Labonnote (2006) and others, the DoLP function for randomly oriented smooth columns shows positive features at scattering angles around 130° and negative values at scattering angles larger than 160°, while these features decrease in strength or disappear completely with an increasing roughness parameter (Fig. 2b). Similar dependence of the DoLP function on roughness has been reported for more complex particles by, Um and McFarquhar (2009) and Baum et al. (2010), among others. As seen in Fig. 2a, the DoLP function of a slightly roughened column increases with increasing aspect ratio, especially at scattering angles smaller than about 140° (cf. Chepfer, 1998). The dependence of the DoLP function of plates on both aspect ratio and roughness parameter is similar (not shown). In the range of scattering angles typically observed by downward looking remote sensing instruments (about 90–175° depending on geometry) the DoLP shows distinctively different variations (Fig. 2) as a function of aspect ratio and roughness parameter. This suggests that these two parameters can be estimated from such polarization measurements and that, as a consequence (cf. Fig. 1), the asymmetry parameter can be inferred.

For the inference of ice crystal asymmetry parameter, we aim to minimize the relative root-mean-squared difference (RRMSD) between polarization measurements at the considered angles and the corresponding simulated values from our look-up-table. For a given combination of aspect ratio $AR_i$ and roughness parameter $\delta_j$, the RRMSD is formally defined as
where $R_{p, \text{meas}}$ is the measured polarized reflectance as a function of single scattering angle $\Theta$ and $R_{p, \text{LUT}}$ is the corresponding quantity in the LUT. In the current retrieval approach the RRMSD is simply calculated for all combinations of aspect ratios and roughness parameters that are included in the LUT and the retrieved values correspond to the minimum value of the RRMSD. To optimize such a retrieval, more efficient minimization approaches could be used (Rodgers, 2000).

For cloud optical thicknesses $\tau_{\text{cloud}}$ larger than about 5 the polarized reflectance saturates and does not depend on $\tau_{\text{cloud}}$ (Chepfer et al., 2001). For optically thinner clouds, the LUT must also include the correct apparent cloud optical thickness (apparent cloud optical thickness is defined as the optical thickness yielding a total reflectance that matches measurements under the assumption of a particular ice model). Since the apparent optical thickness also depends on the assumed ice asymmetry parameter (Zhang et al., 2009), it needs to be determined for all aspect ratio and roughness combinations in the LUT before applying Eq. (5). Here, we obtain the apparent optical thickness by minimizing the differences between measured and simulated total reflectances at 864 nm at the viewing angle closest to nadir. For cases with $\tau_{\text{cloud}} \geq 5$, the asymmetry parameter can be retrieved using Eq. (5) assuming a large cloud optical thickness (e.g., $\tau_{\text{cloud}} = 50$), and the correct cloud optical thickness can be determined afterwards. Whether $\tau_{\text{cloud}}$ is above or below five is estimated by using threshold values of total reflectance generated by a first-guess ice model.
3 Results

The retrieval approach is evaluated here by applying it to synthetic measurements. These synthetic measurements are calculated using the radiative transfer model described in the previous section, but using optical properties of ice crystals with more complex shapes than the individual columns and plates assumed in the LUT. We aim to infer the asymmetry parameters of the complex ice crystals to within 5% (or ∼0.04), which is the upper range of the required accuracy of global ice cloud asymmetry parameter estimated by Vogelmann and Ackerman (1995).

A solar zenith angle of 41° and relative azimuth angle of 10° is used for the simulated measurements (corresponding to some of the RSP data used in part 2). RSP measures at 152 viewing angles between ±60°. In the following, we limit the measurements to contain scattering angles in the range 100–165°, which are frequently observed by RSP. The sampling of scattering angles of the RSP at this geometry is about 0.8°. First we apply the proposed retrieval approach to simulated measurements assuming clouds consisting of bullet rosettes, other complex habits and mixtures of complex habits. Then, the sensitivity of the method to measurements noise, calibration errors, the available scattering angle range and the angular sampling is explored.

3.1 Bullet rosettes

Ice crystals resembling bullet rosettes are often observed in mid-latitude cirrus and aged anvil cirrus clouds (Iaquinta et al., 1995; Lawson et al., 2006; Um and McFarquhar, 2007; Baran, 2009; Baum et al., 2011). Optical properties of bullet rosettes are calculated using the same GO code described above (Macke et al., 1996). Following Um and McFarquhar (2007), bullet rosettes are constructed with 6 identical branches consisting of 13 planes each with a bullet tip angle of 28°. Ten different bullet aspect ratios between 2 and 11 are considered, where aspect ratio is defined as the ratio of the total bullet length (including tip) and its width. As with the hexagonal ice crystals used in the LUT, the roughness parameter varies between 0 and 0.7 in steps of 0.05. Projected
areas cannot be analytically calculated for bullet rosettes and we therefore calculated
the scattering properties of bullet rosettes that have volumes that are the same as
spheres with radii of 5, 7, 10, 14, 20, 28, 40, 56, 80, 113, 160, 225 and 320 µm. This
volume equivalent spherical size definition is different to the projected area definition
that was used in Sect. 2. Since the results do not substantially depend on size distri-
bution, because the bullet geometry does not vary with size, we nonetheless use the
same size distribution that was introduced in Sect. 2. Simulations are made for the
864 nm band of RSP, but similar results are expected at wavelengths from the visible
to short-wave infrared. A total of 150 combinations of roughness parameter and bullet
aspect ratio is included in the sample.

Figure 3 shows the asymmetry parameters of the bullet rosettes versus those re-
trieved from the simulated \( R_p \) using the proposed method. Here, a cloud optical thick-
ness of 5 is assumed in the simulated measurements. Retrieved values are generally
within 5% of the true values, although they are biased high, especially for small asym-
metry parameters. Figure 4a shows the mean differences between retrieved and true
asymmetry parameters and their standard deviations as a function of cloud optical
thickness. Generally results are quite consistent over all optical thickness values with
mean biases of about 0.02 ± 0.01, with the second number representing the standard
deviation. Slightly larger standard deviations are obtained for optically thin clouds. In
these retrievals the apparent cloud optical thickness is determined first before retriev-
ing the asymmetry parameter. As discussed in Sect. 2, when \( \tau_{\text{cloud}} \gtrsim 5 \), polarized re-
fectances are considered to be saturated and asymmetry parameters can be retrieved
by applying Eq. (5) and assuming any large cloud optical thickness. To illustrate this,
Fig. 4a also shows results of retrieved asymmetry parameters for \( \tau_{\text{cloud}} \geq 5 \) using the
LUT with \( \tau_{\text{cloud}} = 50 \). These results are seen to be similar to those in which \( \tau_{\text{cloud}} \) is
retrieved simultaneously with the asymmetry parameter.

The bias in retrieved asymmetry parameter leads to a 10–40% bias in retrieved
cloud optical thickness, especially for optically thin clouds (Fig. 4b). However, the bias
in scaled optical thickness \( \tau^* = \tau (1 - g) \) (van de Hulst, 1957; King, 1987) is much
smaller, as expected (Zhang et al., 2009). Figure 4c shows that mean differences between aspect ratios of the individual bullets and retrieved values are about 20 ± 40% for \( \tau_{\text{cloud}} > 5 \), but increase to 60 ± 50% for optically thinner clouds. The crystals are consistently retrieved as column-like. Biases in retrieved roughness parameter shown in Fig. 4d are about −0.05 ± 0.08 for clouds with \( \tau_{\text{cloud}} > 5 \) and about 0.03 ± 0.08 for \( \tau_{\text{cloud}} < 5 \). The general positive bias of retrieved asymmetry parameters is consistent with the findings of Um and McFarquhar (2007) that the asymmetry parameters of bullet rosettes are about 2% lower than those of the individual bullets, presumably owing to the increased variation in refraction + reflection angle combinations in the more complex rosettes versus those in the individual bullets (cf. Macke et al., 1996). This effect is apparently only partly mitigated by the effect of biases in aspect ratio and roughness parameter in the retrievals.

### 3.2 Complex habits

Next we apply the proposed method to simulated measurements assuming a selection of hexagonal and complex ice crystal habits: droxtals (Zhang et al., 2004), columns, plates, bullet rosettes, aggregates of columns, hollow columns (Yang and Liou, 1998), hollow bullet rosettes (Yang et al., 2008c) and aggregates of plates (Baum et al., 2011). Details about the geometries of these crystals are given in the cited references. The scattering properties of the individual particles are computed using the discrete dipole approximation for particles with a small size parameter (defined as the ratio of the particle circumference to the incident wavelength) or an improved geometric optics method (IGOM) for particles with a large size parameter (Yang and Liou, 1998; Bi et al., 2009; Xie et al., 2011). Microscale crystal surface roughness is taken into account with an approximate method similar to that in the GO code described in Sect. 2 (Yang et al., 2008a). As in Baum et al. (2011), smooth, moderately roughened and severely roughened particles are considered with a degree of surface roughness \( \sigma \) of 0, 0.03 and 0.5, respectively (see Yang et al., 2008a, for the definition of \( \sigma \)). Since some of the ice habit geometries vary with size, a range of size distributions is applied by varying \( \lambda_p \) in
Eq. (4) from 20 to 200 cm$^{-1}$ with increments of 20 cm$^{-1}$ and using the relation between $\mu_p$ and $\lambda_p$ determined by Heymsfield et al. (2002) from in situ measured ice size distributions, namely $\mu_p = \lambda_p^{0.64} - 2$ (with $\lambda_p$ in units of cm$^{-1}$). A total of 270 combinations of habit, roughness and size is included in the sample.

For a cloud optical thickness of 5, retrieved asymmetry parameters are seen in Fig. 5 to be highly correlated with the true values, with a mean bias of 0.004 ± 0.018. For particle shapes with geometries independent of size, which is the case for aggregates and droxtals, the results for different size distributions are clustered together. The biases and standard deviations are seen in Fig. 6a to be nearly independent of cloud optical thickness. Furthermore, the biases in the retrievals are significantly smaller than those obtained for the case of bullet rosettes (Fig. 4), but the standard deviations are greater. Plates and their aggregates are generally identified correctly as plates in the retrieval. Even when the habit is misinterpreted as being thin columns for some combinations of size and roughness, the retrieved asymmetry parameters still agree with the true values within 5%. The other particles are consistently and correctly identified as column-like. Interestingly, the method finds that the polarized reflectances of clouds consisting of hollow columns and hollow bullet rosettes most closely resemble those consisting of columns with high aspect ratio (>15). This result makes sense since the walls of the hollow parts of the crystals are thin, resembling columns with high aspect ratios. For all particles the retrieved roughness parameters increase with increasing roughness of the particles assumed in the simulated measurements, as expected. Mean biases in the retrieved cloud optical thickness, shown in Fig. 6b, are near zero for $\tau_{\text{cloud}} > 5$, with standard deviations of about 10%, while for thin cloud ($\tau_{\text{cloud}} \sim 1$) the cloud optical thickness is retrieved within about 15 ± 25%. As found for the simulated measurements assuming bullet rosettes (Fig. 4b), the mean bias in scaled optical thickness is near zero for all cloud optical thickness values.
3.3 Habit mixtures

The proposed method is next applied to simulated measurements using optical properties of mixtures of ice crystal habits. We use mixtures compiled by Baum et al. (2005a,b, 2011) to be consistent with ice water contents and median mass diameters measured by in situ probes during numerous field campaigns. The mixtures consist of combinations of the hexagonal and complex habits described in Sect. 3.3 and the same three degrees of crystal roughness are used. Four mixtures are considered: the general habit mixture compiled for the MODIS collection-5 ice properties retrieval algorithm (Baum et al., 2005a,b), a more recent general habit mixture (Baum et al., 2011) and those corresponding to tropical deep convection clouds and mid-latitude cirrus (Baum et al., 2011). A total of 120 combinations of habit mixture, roughness and size is included in the sample.

In Fig. 7 it is seen that asymmetry parameters of the particle mixtures span from 0.8 to about 0.87, and most asymmetry parameters are again retrieved within 5%. However, asymmetry parameters for the tropical deep convection mixture, which is dominated by aggregates of plates, are systematically overestimated by about 0.05 when no roughness is applied. The retrieval algorithm interprets these mixtures as very thin plates with aspect ratios less than 0.1. The same is true for three results for smooth collection–5 mixtures with large sizes, which are dominated by bullet rosettes, columns and plates. Thus, when smooth, very thin plates are retrieved by the algorithm, such retrieved asymmetry parameters should be treated with caution and probably rejected.

As for the complex habits (Fig. 6), the bias of the retrieved asymmetry parameter of the particle mixtures is slightly positive and fairly independent of the cloud optical thickness (Fig. 8a). Also, again, the retrieved cloud optical thickness is biased towards greater values (Fig. 8b), but essentially no bias is obtained in the retrieval of scaled optical thickness.
3.4 Sensitivity to noise, calibration, angular range and sampling

Next, the sensitivity of the asymmetry parameter retrieval approach to random noise, calibration errors and the available scattering angles are evaluated. For this analysis, we use the simulated measurements assuming optical properties of complex habits described in Sect. 3.2.

Pseudo-random structures can appear on the multi-angle total and polarized reflectance measurements owing to, for example, instrument noise, errors in stray-light correction and misalignment of scenes targeted at different angles (Cairns et al., 2003; Fougnie et al., 2007). Such errors are estimated to be of the order of 3% for instruments such as POLDER (Fougnie et al., 2007) and lower for the RSP (Cairns et al., 2003). To investigate the influence of such errors on our retrieval of asymmetry parameters, we add Gaussian noise with increasing standard deviation to simulated data. As seen in Fig. 9a, the bias and standard deviation are essentially unaffected by random noise with standard deviations of up to about 20% of the signal. For noise contributions larger than a threshold of about 20% the retrieval results rapidly degrade. Note that these simulations assume the angular sampling corresponding to the RSP, which, for the assumed geometry, lead to 84 samples within the 100–160° scattering angle range considered. Since the influence of Gaussian noise is expected to scale as $\sqrt{N_s}$, where $N_s$ is the number of sampling points, requirements of measurements of instruments with less angular sampling will be more stringent than those for the RSP. For example, POLDER has about 10 times fewer viewing angles than the RSP, requiring the noise level to be about $\sqrt{10}$ times lower or a threshold of about 6%. Note that POLDER generally is expected to meet this requirement (Fougnie et al., 2007).

Determination of the absolute calibration of instruments measuring total and polarized reflectance can be challenging, especially with the absence of on-board calibration sources and with aircraft-mounted instruments that undergo frequent and substantial changes in temperature, humidity, among others. The nearly linear dependence seen in Fig. 9b indicates that every additional 10% calibration offset added to the simulated
data leads to an additional 0.003 near-linear increase in bias for the retrieved asymmetry parameter. Furthermore, the standard deviation increases by about 0.002 for every additional 10% offset. Since most calibration errors are expected to equally affect total and polarized reflectance measurements, offsets are added to both total and polarized reflectances here. However, similar results are obtained when only offsets are added to the polarized reflectances, and an equivalent negative bias trend is obtained when negative offsets are applied to the simulated data (not shown).

The range of scattering angles observed by an instrument depends on the instrument viewing angle range and the solar and relative azimuth angles. The previous analysis assumes scattering angles between 100° and 165° to be available. Figure 10a illustrates the performance of the proposed method when narrower scattering angle ranges are available. All considered scattering angle ranges are centered on 132.5°. Figure 10a shows the bias is nearly unaffected by the available scattering angle range. The standard deviation, however, does substantially increase with decreasing angular range, but this is mostly owing to an increasing underestimation of only the asymmetry parameters of pristine individual plates, which represent a small subset of the simulated dataset and therefore do not affect the mean bias substantially. When the available scattering angle range is below 25°, also the asymmetry parameters of aggregates of plates are substantially underestimated, leading to a greater increase in the standard deviation.

As discussed above, these simulations are based on the RSP instrument profile with a relatively dense angular sampling (84 samples at ~0.8° intervals). Figure 10b shows retrieval results for simulations with decreasing amount of roughly angular equidistant samples available in the 100–160° scattering angle range. Surprisingly, the results are little affected by angular sampling, even when only 2 samples (at 100° and 160°) are available. Similar results are obtained for simulated measurements assuming habit mixtures and bullet rosettes, although some substantial increase in standard deviation is observed when measurements are degraded from 3 to 2 samples in the case of bullet rosettes (not shown).
The results shown in Figs. 9 and 10 indicate that the proposed method can be readily applied to measurements of other available instruments, such as POLDER, which have a more limited angular sampling and range and a possibly stronger noise contribution and calibration uncertainties than the RSP.

4 Conclusions

This first part of a two-part paper uses simulated measurements to evaluate, to the best of our knowledge, the first remote sensing method of inferring the asymmetry parameter of ice clouds. We demonstrate that multi-directional polarized reflectance measurements at visible or near-infrared wavelengths contain exploitable information about the aspect ratio and microscale surface roughness of components of ice crystals, which, in turn, determine the ice crystal asymmetry parameter. By assuming individual hexagonal columns and plates to be adequate proxies of more complex ice crystals occurring in most natural clouds, ice cloud asymmetry parameters are inferred by matching observed multi-directional polarized reflectance measurements to a look-up table of simulated polarized reflectances for columns and plates with varying aspect ratios and roughness parameters. The asymmetry parameter of the hexagonal particle that leads to the best fit with the measurements is considered the retrieved value.

The application of the method is demonstrated using simulated measurements of clouds consisting of first only bullet rosettes, then other complex habits and finally their mixtures. Instrument characteristics of the airborne Research Scanning Polarimeter (RSP) are assumed for the simulated measurements. Generally, asymmetry parameters of the ice crystals and mixtures assumed in the simulated measurements are retrieved to within 5%, or about 0.04 in absolute terms. Most retrieved values are biased high, especially for bullet rosettes. Since polarized reflectances depend on cloud optical thickness for clouds with \( \tau_{\text{cloud}} \lesssim 5 \), cloud optical thickness needs to be retrieved simultaneously with the asymmetry parameter for such clouds. For \( \tau_{\text{cloud}} > 5 \), the true cloud optical thickness is not required to retrieve the asymmetry parameter.
A sensitivity study shows that the proposed method is largely independent of calibration errors, range and sampling density of scattering angles and random noise in the measurements.

Our results demonstrate that the proposed approach to retrieve asymmetry parameters of ice clouds can be readily applied to RSP measurements and other current and past instruments, such as the satellite-based POLDER instruments and the airborne Multiangle SpectroPolarimetric Imager (AirMSPI, Diner et al., 2007), as well as on those of possible future instruments, such as the next-generation POLDER instruments (3MI), APS (Mishchenko et al., 2007), MSPI (Diner et al., 2007) and SPEX (van Harten et al., 2011). Application to polarization measurements in wavelength bands that include strong water vapor absorption, such as the 1.88 µm and 1.39 µm bands in the RSP and APS designs, respectively, allow the retrieval of ice crystal asymmetry parameters of subvisual cirrus, as demonstrated by Ottaviani et al. (2012a). Furthermore, the method can be easily adapted to degree of linear polarization measurements obtained by future dual-polarization polar nephelometers that are capable of sampling ice clouds.

Application of the presented approach to the available POLDER data (and future satellite data) has the potential to provide a global database of ice cloud asymmetry parameter that may substantially reduce uncertainties in radiative properties in climate models and improve the retrieval of other ice cloud properties, such as ice crystal sizes and cloud optical thickness. Furthermore, when combined with other observations, possible correlations between retrieved asymmetry parameters and cloud type, cloud-top temperature, ice crystal size or aerosol populations may be deduced in order to improve our understanding of ice cloud formation processes under varying conditions.

Acknowledgements. This material is based upon work supported by the NASA ROSES program under grant number NNX11AG81G and by the NASA Radiation Science Program managed by Hal Maring in support of the SEAC4RS field experiment.
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**Fig. 1.** Asymmetry parameters of plates and columns at 864 nm as a function of their aspect ratio and microscale roughness.
Fig. 2. Degree of linear polarization at 864 nm as a function of scattering angle for hexagonal columns. Colors indicate DoLP functions for varying aspect ratios (AR, a) and roughness parameters (δ, b).
Fig. 3. Asymmetry parameters of bullet rosettes versus the asymmetry parameters retrieved with the proposed method from simulated data with a cloud optical thickness of 5. The solid line shows the 1-1 line. Dotted lines indicate the targeted 5 % accuracy limits.
**Fig. 4.** Mean biases (solid lines) and standard deviations (shaded areas) of retrieved asymmetry parameters (a), optical thickness (b), aspect ratio (c) and roughness parameter (d) as a function of cloud optical thickness assumed in the simulated data using bullet rosettes. The dashed line and line-shaded area in (a) shows results where $\tau_{\text{cloud}} = 50$ is assumed in the LUT. The dotted line in (b) shows the mean bias of the scaled optical thickness (defined in text).
Fig. 5. As for Fig. 3, but for simulated data assuming various ice crystal habits indicated by symbols. Black, green and red colors are results for simulated data assuming smooth, moderately rough, and severely rough particles, respectively. For each combination of roughness and habit, 10 different size distributions are applied (see text).
Fig. 6. Mean biases (solid lines) and standard deviations (shaded areas) of retrieved asymmetry parameters (a), optical thickness (b) as a function of cloud optical thickness assumed in the simulated data using complex habits. The dotted line and line-shaded area in (b) shows the mean bias and standard deviation, respectively, of the scaled optical thickness.
Fig. 7. As for Fig. 5, but for simulated data assuming various ice crystal habit mixtures. Circles denote the MODIS collection-5 mixture of Baum et al. (2005a,b) and the other symbols denote mixtures of Baum et al. (2011).
Fig. 8. As for Fig. 6, but for simulated data assuming various ice crystal habit mixtures.
Fig. 9. Dependence of mean bias and standard deviation of retrieved asymmetry parameters from simulated data assuming various complex habits on noise level (a) and calibration error (b). See text for details.
Fig. 10. As Fig. 9 but showing dependence of results on angular range (a) and number of scattering angles sampled (b). In (a) maximum and minimum values of the included scattering angles for three example angular ranges are indicated. See text for details.