Understanding the aerosol information content in multi-spectral reflectance measurements using a synergetic retrieval algorithm

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Abstract

The multi-wavelength SYnergetic AErosol Retrieval algorithm SYNAER (Holzer-Popp et al., 2002) is used to retrieve aerosol parameters from the Advanced Along Tracking Scanning Radiometer (AATSR) and the Scanning Imaging Absorption Spectrometer for Atmospheric CHartographY (SCIAMACHY). An information content analysis (Holzer-Popp et al., 2008) was performed to quantify the number of independent pieces of information can be retrieved from the combined reflectance measurements of aerosols by both instruments. In particular, the capability of SYNAER to discern various aerosol types is assessed. The focus of this work is further placed on an information content analysis with emphasis to the aerosol type classification. This analysis is applied to synthetic reflectance measurements for 40 predefined aerosol mixtures of different basic components, given by sea salt, mineral dust, biomass burning and diesel aerosols, water soluble and water insoluble aerosols. The range of aerosol parameters considered through the 40 mixtures covers the natural variability of tropospheric aerosols. In this work the capability of the multi-wavelength algorithm to discern aerosol types is investigated. After the information content analysis performed in Holzer-Popp et al. (2008) there was a necessity to compare derived degrees of freedom with retrieved aerosol optical depth for different aerosol types, which is the main focus of this paper. This information content depends on the aerosol optical depth, the surface albedo spectrum and the observation geometry. This theoretical analysis is performed for a large number of scenarios with various geometries and surface albedo spectra for ocean, soil and vegetation. When the surface albedo spectrum and its accuracy is known under cloud-free conditions, reflectance measurements used in SYNAER is able to provide for 2 to 4 degrees of freedom that can be attributed to retrieval parameters: aerosol optical depth, aerosol type and surface albedo.
1 Introduction

Several satellite instruments measuring backscattered solar radiation are currently used to monitor atmospheric aerosols. But there exist only few of retrieval methods which are capable to retrieve and classify different aerosol types. The characterization of aerosols using satellite observations is challenging due to their variability in many respects, such as composition, size, particle shape and vertical distribution. In order to determine as many relevant aerosol parameters as possible, radiometric and polarimetric observations in a broad wavelength range with many viewing angles and a high spatial and spectral resolution would be optimal (Chowdhary et al., 2001). However, such measurements are technically challenging.

In recent years the satellite monitoring capabilities to derive maps of aerosol optical depth (AOD) have increased tremendously. A good overview of different satellite retrieval principles for deriving AOD is presented in Kaufman et al. (1997a) and a review of achieved AOD retrieval capabilities is given in Kaufman et al. (2002). Examples of satellite retrieval of additional aerosol optical properties include the Angstrom coefficient (e.g. AATSR dual view, Veefkind et al., 1999) and the separation into fine and coarse mode aerosols (e.g. MODIS multi-spectral collection 5 (Levy et al., 2007); fine mode AOD only by POLDER polarized multi-spectral (Deuzé et al., 2001). Further examples of aerosol characterisation use a choice from pre-defined aerosol types (e.g. MISR multi-angle, Kahn et al., 2005), or deliver the single scattering albedo (MODIS deep blue (Hsu et al., 2004), or derived quantities such as particle number concentrations (e.g. parameterization based on MERIS multi-spectral measurements (von Hoyningen-Huene et al., 2003; Kokhanovsky et al., 2006).

In this study the information content of measurements of the synergetic algorithm SYNAER for AATSR and SCIAMACHY is investigated. These instruments were conceived to improve our global knowledge and understanding of a variety of issues of importance for the chemistry and physics of the Earth atmosphere and potential changes resulting from either anthropogenic behaviour or natural phenomena. While not being
the prime focus, aerosols are an important science target of these instruments. Both of the instruments are flown on the European platform ENVISAT which was launched on 1 March 2002. AATSR data have a resolution of 1 km at nadir, and are derived from measurements of reflected and emitted radiation taken at seven wavelengths: 0.55 µm, 0.66 µm, 0.87 µm, 1.6 µm, 3.7 µm, 11 µm and 12 µm. SCIAMACHY has a nadir and an additional limb viewing mode. Its nadir pixel size is 60 × 30 km² and it has a complete extended spectral range covering 240 to 1750 nm and 1940 to 2380 nm partly with a spectral resolution between 0.2 and 1.5 nm. In the latest calibration version the cross-correlation of spectrally and spatially integrated reflectances measured by both instruments and against another radiometer MERIS (Medium Resolution Imaging Spectrometer) onboard ENVISAT was found to satisfy high accuracy requirements with deviations on the order of 1% (Kokhanovsky et al., 2007).

At the German Remote Sensing Data Center (DFD) the aerosol retrieval method SYNAER was developed (Holzer-Popp et al., 2002a) which delivers boundary layer aerosol optical depth and type over both land and ocean, the latter as percentage contribution of 9 representative components based on the OPAC (Optical Parameters of Aerosols and Clouds, Hess et al., 1998) dataset to AOD. The SYNAER method consists of two parts. In the first part the AATSR radiometer data are used to retrieve aerosol optical depth and surface reflectance for a selected aerosol type. In the second part the spectrometer data are then used to select the most plausible aerosol type. As the estimation of the aerosol type is the most innovative part of SYNAER, a study provided an analysis of the information content of the second SYNAER part with regard to aerosol composition following (Holzer-Popp et al., 2008). Consequently, the focus of this analysis was on exploiting the spectrometer measurements explicitly using the results of the first retrieval step, namely aerosol optical depth at 0.55 µm and surface reflectance at 0.55, 0.67 and 0.87 µm for each aerosol mixture. In the analysis of the information content 9 basic components (water soluble, water insoluble with high and low hematite content, sea salt accumulation and coarse mode, anthropogenic soot, biogenic soot and mineral dust with high and low hematite content) were used to
define a set of 40 mixtures (see Table 1), which was then applied to radiative transfer calculations of simulated SCIAMACHY spectra.

In this study the information content of reflectance measurements in the wavelength bands used in SYNAER is investigated. The number of Degrees of Freedom of the Signal (DFS) and the separable aerosol components are quantified by applying an information content analysis (Sect. 2) to synthetic reflectance spectra for a large number of scenarios with various aerosol models, observation geometries and surface types. The information content theory (Rodgers, 2000) was applied in an unusual way, namely to independently assess the information content of the existing retrieval method and discern the input of different aerosol types in the measurements. This new point of view on the retrieval problem allows to derive some facts about capabilities and limitations of SYNAER to estimate aerosol composition. The results of the information content analysis are immediately applicable to the SYNAER algorithm, since the DFS analysis is applied to the synthetic reflectance data stored in the Look-Up Tables (LUT) of SYNAER. The results of the DFS analysis depend on the aerosol parameter ranges covered by the set of aerosol models considered. The basic assumption made in this study is that the aerosol models cover the natural variability of tropospheric aerosol. The number of DFS obtained is representative for the number of aerosol parameters that can be retrieved independently from reflectance measurements provided that the surface albedo spectrum is accurately known and the presence of clouds can be completely excluded or corrected, see Holzer-Popp et al. (2002).

This introduction is followed by the description of used method for information content analysis. An analysis of the information content of the (additional) second retrieval step of SYNAER with regard to aerosol composition including realistic noise in the retrieval is made (Sect. 2). The number of Degrees of Freedom of the Signal (DFS) is quantified by applying Singular Value Decomposition Analysis to synthetic reflectance spectra (Sect. 3.1) for a large number of scenarios with various aerosol models, observation geometries and surface types. Section 3.2 gives an overview of the derived results for DFS and its interpretation. Section 3.3 deals with the distinction between aerosol...
types in the retrieval. The weights associated with the DFS provide a graphical view on the aerosol retrieval. This concept is used to investigate the cross correlations of the retrieved aerosol types. The paper concludes with a discussion and conclusions in Sect. 4.

2 Analysis of information content

The method used to examine and analyse the information content is the singular value decomposition (SVD). The following theoretical description is based on the inverse methods methodology (Rodgers, 2000). SVD is a useful tool to identify the dominant parts of the observations. This allows identifying the number of parameters which can be retrieved from observations and analysing the separability of the variables retrieved. Generally, the number of observations does not equal the degrees of freedom because not all observations are uncorrelated.

For any remote measurement, we can define relationship between real state of the atmosphere and measurement:

$$y = F(x, b) + \varepsilon$$  \hspace{1cm} (1)

where $y \in \mathbb{R}^m$ is the measurements vector of dimension $m$, i.e. reflectances at $m$ wavelengths; $x \in \mathbb{R}^n$ is the state vector of dimension $n$; $b$ is the vector containing all the other parameters necessary to define the radiative transfer through the atmosphere to the spacecraft, $F : \mathbb{R}^n \rightarrow \mathbb{R}^m$ is the forward model that describes the physics of the measurements that map from the state space to the measurements space and $\varepsilon \in \mathbb{R}^m$ is the measurement error vector.

In this work some aspects of principal component analysis were used. Principal component analysis is a powerful tool that helps to clarify the number of parameters that can be retrieved from a given set of observations. This approach is particularly useful for the analysis of the large measurement sets where a direct physical analysis is difficult due to high number of measured and retrieved parameters. In this study...
there is an attempt to infer information about the correlation or independence of retrieved types of aerosol parameters. A similar analysis for different aerosol parameters was accomplished in Veihelmann at al. (2007), where the principal component analysis was applied, which works as follows: the set of \( n \) simulated reflectance measurements is stored in the measurement matrix \( Y \) with elements \( y_{nm} \), where the column vectors are the \( n \) reflectance vectors from the state space \( R^n \) and the index \( m \) indicates the wavelength band. The measurement matrix \( Y \) is normalized such that for each wavelength, the mean value of all measurements is zero and the standard deviation is unity. The covariance matrix \( A = YY^T \) is diagonalized according to \( A = V^T D V \) such that the row vectors of the matrix \( V \) form an orthonormal set of eigenvectors. Each reflectance measurement can be decomposed into a weighted sum of some basic components:

\[
y_m = \hat{y}_m + \delta = \sum_{k}^{k_{\text{max}}} w_{mk} v_k + \delta
\]  

Where \( \hat{y}_m \) are the elements of the reconstructed measurement matrix with an error \( \delta \), with weights \( w_{mk} \) being the elements of the matrix \( W \). Naturally, when a measurement is reconstructed using all \( K \) basic components (\( k_{\text{max}} = K \), in Eq. 2), the error \( \delta \) is zero. The sum in Eq. (2) can be truncated at \( k_{\text{max}} < K \) without any loss of information as long as the error \( \delta \) is smaller than the error due to instrument noise.

The matrix \( V \) transforms the measurement matrix \( Y \) into the space of so called weights. \( D \) consists of eigenvalues of matrix \( A \). These eigenvalues of the transformed \( Y \) can be interpreted as a measure for the importance (DFS) for each aerosol component. In this study, a very similar analysis method is performed. For the implementation of the technique of identifying different aerosol types see Sect. 3.3.

The measurement vector for this theoretical analysis of the SYNAER retrieval consists of simulated spectra at 10 (\( m=10 \)) wavelengths for 40 (\( n=40 \)) different aerosol mixtures with a given surface type. The state vector consists of 40 different aerosol mixtures composed by 9 basic components. The method rests on the assumption, that

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A linear approximation of $F$ is sufficiently exact at some reference state $x_0$:

$$y - F(x_0) = \frac{\partial F}{\partial x}(x - x_0) + \varepsilon = K \cdot (x - x_0) + \varepsilon$$

(3)

where $K$ is the weighting function matrix of dimension $m \times n$. Each element of $K$ is the partial derivative of a forward model element with respect to a state vector element:

$$k_{ij} = \frac{\partial F(x)_i}{\partial x_j}; \forall i = 1..m, \forall j = 1..n$$

(4)

$F$ maps the state space into the measurement space according to the Forward Model. It is necessary to have some prior information about the state, to constrain the solution.

The information content can be condensed into the Degrees of Freedom for Signal (DFS). DFS can be interpreted as the number of independent linear combinations of the state vector that can be independently retrieved from the measurements. It is given by:

$$\text{DFS} = \sum \frac{\lambda_i^2}{1 + \lambda_i^2}$$

(5)

where $\lambda_i$ are the singular values of $(S_\varepsilon)^{-1/2} K (S_a)^{1/2}$.

$S_\varepsilon$ and $S_a$ correspond to measurement covariance matrix and a priori covariance matrix. The measurement covariance matrix $S_\varepsilon$ has a diagonal form, with diagonal elements equal to the relative error of measured reflectance spectrum values. The structure of the a priori covariance matrix $S_a$ is shown on Fig. 1. The elements of this matrix are derived from Table 1 using an ordinary definition of covariance:

$$S_a^{ij} = \frac{1}{n} \sum (r_i - \bar{r})(s_j - \bar{s})$$

(6)

where $r_i, s_j$ are the percentage contributions of the 9 basic components for each aerosol mixture from Table 1; $\bar{r}, \bar{s}$ are the mean values of $r_i, s_j, i = 1..n, j = 1..n$; $n$ is the total number of mixtures.
3 Results

In this section the results of the DFS analysis are shown and discussed for a large number of scenarios. The capabilities of the multi-wavelength algorithm are assessed using the number of DFS as well as the weights of the measurement matrix.

3.1 Synthetic reflectance data

For a fast application in aerosol retrieval precalculated radiative transfer tables are used. For this study radiative transfer simulations are based on the Look-Up Tables (LUT) which includes simulations for many different aerosol cases for various aerosol types, including biomass burning, desert dust, weakly absorbing and water soluble aerosols. The aerosol models cover a range of optical parameters, as well as a range of atmospheric scenarios with varying AOD. Altogether, more than 2500 simulated reflectances with different geometry and aerosol parameters are taken into account.

3.2 Overview for number of degrees of freedom for signal

The singular values used in definition of DFS drop fast with increasing order: for most geometries and surface types, more than 70% of the reflectance measurements can be reproduced within the measurement error when including 2 to 5 singular values; singular values of higher orders are then not relevant for most reflectance measurements since their contribution to the reflectance is dominated by instrument noise (Holzer-Popp et al., 2008).

Further to the earlier study, the number of DFS calculated as explained at the end of Sect. 2 depends on the observation geometry, the surface albedo and the choice of the noise threshold. In order to give an overview of the information content of reflectance measurements, histograms of the number of DFS for various scenarios are shown. In Fig. 2 histograms of the number of DFS are plotted for the observation geometry for varying solar elevation angles (SEA), applying surface albedo spectrum for soil. The
measurement error in this case is equal $10e^{-6}$. Histograms for the number of DFS of all aerosol models are shown for a series of geometries with sun elevation angles ranging from 12.5° to 90°. The information content of measurements tends to be higher with increasing angle. In most cases the number of DFS varies between 2 and 5.

Optical depth dependence of the number of DFS is depicted in Fig. 3 for the observation geometry with AOD, ranging from 0 to 0.7, SEA equal to 42.5° and surface type soil. From the point of view for DFS, soil case signals are weaker in comparison with vegetation case, as the DFS values for soil in average are smaller than for vegetation case. However, the principal findings of the former result also applicable in this case. There is an accumulation point (DFS=4) about AOD=0.16, from which the distribution of histograms are quite similar to each other. This means that further increase of AOD does not contribute to any additional aerosol information in the retrieval. In this case the variance of the measurement error covariance matrix is of order $10e^{-6}$.

In Fig. 4 the histogram of the number of DFS is plotted for the observation geometry with solar elevation angle 42.5°, surface albedo spectrum for vegetation and varying measurement observation error. For the typical observation error variance of order $10e^{-6}$ obtained DFS varies between 3 and 4. When an error of $\sigma^2_\varepsilon=6e^{-7}$ is assumed, there are 4 degrees of freedom for most of the aerosol measurements (yellow line). If this noise value is relaxed by assuming a lower error in observations (with the observation error values of $\sigma^2_\varepsilon=5e^{-7}$ (green line), $\sigma^2_\varepsilon=4e^{-7}$ (blue line), $\sigma^2_\varepsilon=3e^{-8}$ (purple line)), a further increase of degrees of freedom is monitored. The choice of such values for observation error variance is based on the attempt to explore the dependency of DFS from observation error in large-step series of the error ($10e^{-6}$, $6e^{-7}$, $3e^{-8}$) and in small-step series of the observation error ($4e^{-7}$, $5e^{-7}$, $6e^{-7}$).

### 3.3 Distinction between aerosol types

The capability of the SYNAER algorithm to discern aerosol types is investigated using the distribution of the different aerosol retrieval scenarios in the space of weights. The first two weights from Eq. (2): $w_{m1}$ and $w_{m2}$ indicate, whether aerosol models can be
discerned or not, for cases where at least two DFS are available. If three DFS are available, the first three weights have to be taken into account in order to decide, whether aerosol models can be discerned or not. Figure 5a shows the variation of the AOD in the space of the first two weights for all 40 aerosol mixtures from Table 1. Solid lines connect models with identical aerosol type but variable aerosol optical depth ranging from 0 to 0.7, while all other parameters, such as observation angle, albedo, aerosol type are constant. When the solid lines in this plot construct a larger angle between each other, using DFS interpretation from Sect. 2, Eq. (5) it can be interpreted as uncorrelated measurements of aerosol mixtures with larger DFS number. The separability is also defined by a minimum distance to noise measurements, e.g. from the figure AOD>0.15. The independent retrieval becomes more pronounced when the AOD increases. It appears that the major groups of the aerosol mixtures can be separated rather well in most cases with AOD>0.15. Mineral dust aerosol with high and low hematite content are also represented with two separate bundles. The measurements from Fig. 5a containing independent information about desert dust and continental aerosol form the fact that these aerosol types are near-orthogonal in the space of weights. But this does not require that either desert dust or continental aerosol generate the basis in this space. In the same manner such retrieval parameters as surface type and AOD also can not be explicitly assigned to some DFS value.

But the domain of biomass burning aerosols (red) overlaps with the domain of polluted aerosols (violet). This overlap is less pronounced in the space of second and third weights (Fig. 5b), where the same 40 predefined aerosol mixtures are represented. So for DFS≥3 here also separation becomes possible.

A similar analysis was made separately for each predefined SYNAER surface type. The distinction of domains for different aerosol types is based not only on the angle between AOD solid lines, but also depends on curvature of AOD lines, for example in Fig. 6a, in the case of soil surface type, some of the violet lines (polluted maritime aerosol) at the beginning have the same tendency as the other types of aerosol lines, but for larger values of AOD violet lines have a completely different curvature. The
analysis over this surface albedo corresponds to cases with not very large values of DFS, as compared with the maximum DFS case conditions seen in vegetation surface type. Distinguishing between aerosol types in this case is difficult. For comparison, the distribution of aerosol models in the space of first two weights for the sand surface type is given (Fig. 6b). In this case it is quite difficult to say anything about distinguishing of aerosol types – all domains are mixed in a nontrivial way. This result corresponds well to the retrieval limitations of SYNAER over bright surfaces such as sand or snow (Holzer-Popp et al., 2008). On the other hand one of the most favourable results is shown on Fig. 6c, where the analysis for meadow surface type is made. Domains of different aerosol models are well distinguished. Such plots have been investigated for various typical observation geometries and various surface type spectra. The differences between absolute values and starting point value for the solid lines on these figures (6a, b and c) are caused by the differences between measurement values which form the structure of analysing matrices for each surface type case.

4 Discussion and conclusions

The information content of SYNAER simulated reflectance measurements has been investigated using DFS analysis. This analysis has been performed with a total of about 2500 synthetic SCIAMACHY reflectance measurements in wavelength bands between 400 nm to 700 nm. The number of DFS for reflectance measurements varies between 2 and 6, depending on AOD, surface type, observation angle and noise. The number of DFS reported here are consistent with the results of a preliminary short theoretical study on the information content (Holzer-Popp et al., 2008). Derived DFS from that study can now be assigned in appropriate way to the different types of aerosol. The weights of all aerosol models have been employed to investigate the capability of the SYNAER algorithm to distinguish different aerosol types. Consider the angle between solid lines in Fig. 5 as an index of discernment for aerosol models. Desert dust, continental, sea salt and polluted aerosol can be discerned well from each other.
Desert dust can be discerned from other types of aerosol with the best index. Some aerosol cases for biomass burning cannot be distinguished from polluted aerosol in the space of the first two weights. This ambiguity depends on the number of DFS and is less pronounced if three or more degrees of freedom of the signal can be assigned to aerosol. However, in the most typical SYNAER measurement cases, with sufficient solar angle and appropriate surface type, more than two DFS are available and then a third weight can be used in order to distinguish aerosol types.

Results indicate that major groups of physical aerosol types can be well separated from other retrieval parameters. However, when two DFS are available, sometimes is not possible to separate biomass burning aerosol from polluted aerosols. The problem is solved when three or more DFS are available. The results of the information content analysis can be used in order to determine the number of DFS for a given single spectrum. This quantity can be provided as additional diagnostic output of the aerosol retrieval using the SYNAER algorithm. There is no one-to-one correspondence between individual aerosol or surface parameters and degrees of freedom. In fact this work is an attempt to infer information about the correlation or independence of retrieved aerosol parameters.

The main results of this work will be further used in assimilation procedure of satellite data from SYNAER in chemical transport model. The main focus will be concentrated on tuning of error covariance matrices in assimilation using DFS retrieval information.

References


Table 1. Pre-defined external aerosol mixtures of the basic components which are used in SYNAER. Adapted from Holzer-Popp et al. (2008). WA = watersoluble, IN = insoluble, SS = sea salt, SO = soot, MI = mineral dust.

<table>
<thead>
<tr>
<th>No.</th>
<th>Name</th>
<th>WA</th>
<th>IN</th>
<th>SS</th>
<th>SO</th>
<th>MI</th>
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<tbody>
<tr>
<td>1</td>
<td>Pure water-soluble</td>
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<td></td>
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<tr>
<td>2</td>
<td>Continental</td>
<td>95</td>
<td>5</td>
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<td>85</td>
<td>15</td>
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<td>15</td>
<td>85</td>
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<td>18</td>
<td>Biomass Burning</td>
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Fig. 1. Graphical representation of the correlation between 40 predefined aerosol mixtures. The maximum correlation elements are on the main diagonal of the matrix (self correlation). There is also strong correlation between first and second halves of the 40 aerosol mixtures because of similarity between these two subsets. Standard matrix normalization procedure (dividing by maximum element) was used.
Fig. 2. Histogram for various scenarios (Y-Axis) of the number of DFS of reflectance measurements for retrieval with different sun elevation angle (SEA) for a case with surface albedo spectra over soil.
Fig. 3. Histogram for various scenarios (Y-Axis) of the number of DFS of reflectance measurements for aerosol models as a function of Aerosol Optical Depth (AOD) for a case with surface albedo spectra for soil.
**Fig. 4.** Histogram for various scenarios (Y-Axis) of the number of DFS of SYNAER reflectance measurements using different observation errors for spectrum measurements. The black histogram corresponds to observational measurement variance $\sigma^2=10e^{-6}$, yellow corresponds to $\sigma^2=6e^{-7}$, green line: $\sigma^2=5e^{-7}$, blue line: $\sigma^2=4e^{-7}$, violet line: $\sigma^2=3e^{-8}$. Large-step series of the error: $10e^{-6}$, $6e^{-7}$, $3e^{-8}$ and small-step series of the observation error: $4e^{-7}$, $5e^{-7}$, $6e^{-7}$ correspondingly.
**Fig. 5a.** Weights for the first and second eigenvalue component for 40 aerosol mixtures for all measurement scenarios. Retrieval scenarios with the same parameters but with varying optical depth are connected with solid lines. The domain of diesel and biomass burning (red) overlaps with the domains of polluted aerosol (dark blue and violet). Other domains: maritime (light blue), continental (black) and desert dust (sienna) are quite good distinguishable.
Fig. 5b. Distribution of retrieval in the space of second and third weights for 40 aerosol mixtures for all measurement scenarios. Retrieval scenarios with the same parameters but with varying optical thickness are connected with solid lines. There are five domains marked with different colours: the domain of diesel and biomass burning (red), the domain of polluted aerosol (dark blue and violet). Other domains: maritime (blue), continental (black) and desert dust (sienna). In this case black and red lines are not separated.
Fig. 6a. Distribution of retrieval in the space of first and second weights for 40 aerosol mixtures only for the surface type soil.
**Fig. 6b.** Distribution of aerosol models in the space of first and second weights for 40 aerosol mixtures for the surface type sand.
**Fig. 6c.** Distribution of aerosol models in the space of first and second weights for 40 aerosol mixtures for the surface type meadow.